

Question Classification

using hierarchical classifiers and
support vector machines

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Seminar Question Answering

Hierarchical Classifiers



Question
Classification

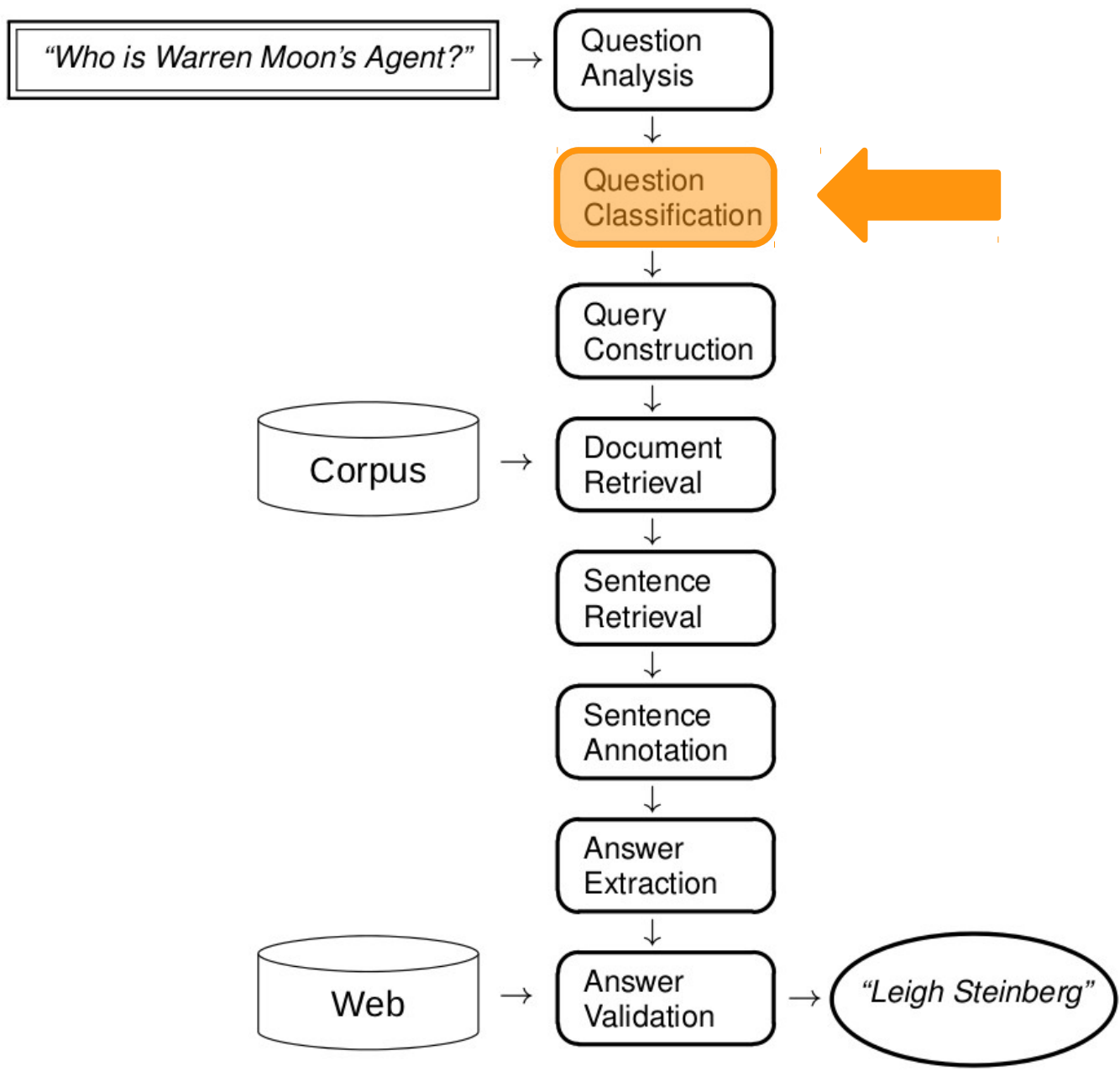
Support Vector
Machines

Hierarchical Classifiers



Question
Classification

Support Vector
Machines



Question Classification

„What Canadian city has the largest population?“

→ **LOCATION:city**

„Who was the first man on the moon?“

→ **HUMAN:individual**

„What does 'USA' stand for?“

→ **ABBREV:exp,**
LOCATION:country

Question Categories

Class	#	Class	#
ABBREV.	9	description	7
abb	1	manner	2
exp	8	reason	6
ENTITY	94	HUMAN	65
animal	16	group	6
body	2	individual	55
color	10	title	1
creative	0	description	3
currency	6	LOCATION	81
dis.med.	2	city	18
event	2	country	3
food	4	mountain	3
instrument	1	other	50
lang	2	state	7
letter	0	NUMERIC	113
other	12	code	0
plant	5	count	9
product	4	date	47
religion	0	distance	16
sport	1	money	3
substance	15	order	0
symbol	0	other	12
technique	1	period	8
term	7	percent	3
vehicle	4	speed	6
word	0	temp	5
DESCRIPTION	138	size	0
definition	123	weight	4

Manual classification

Question starts with ...

Class

Who / Whom



Person

Where



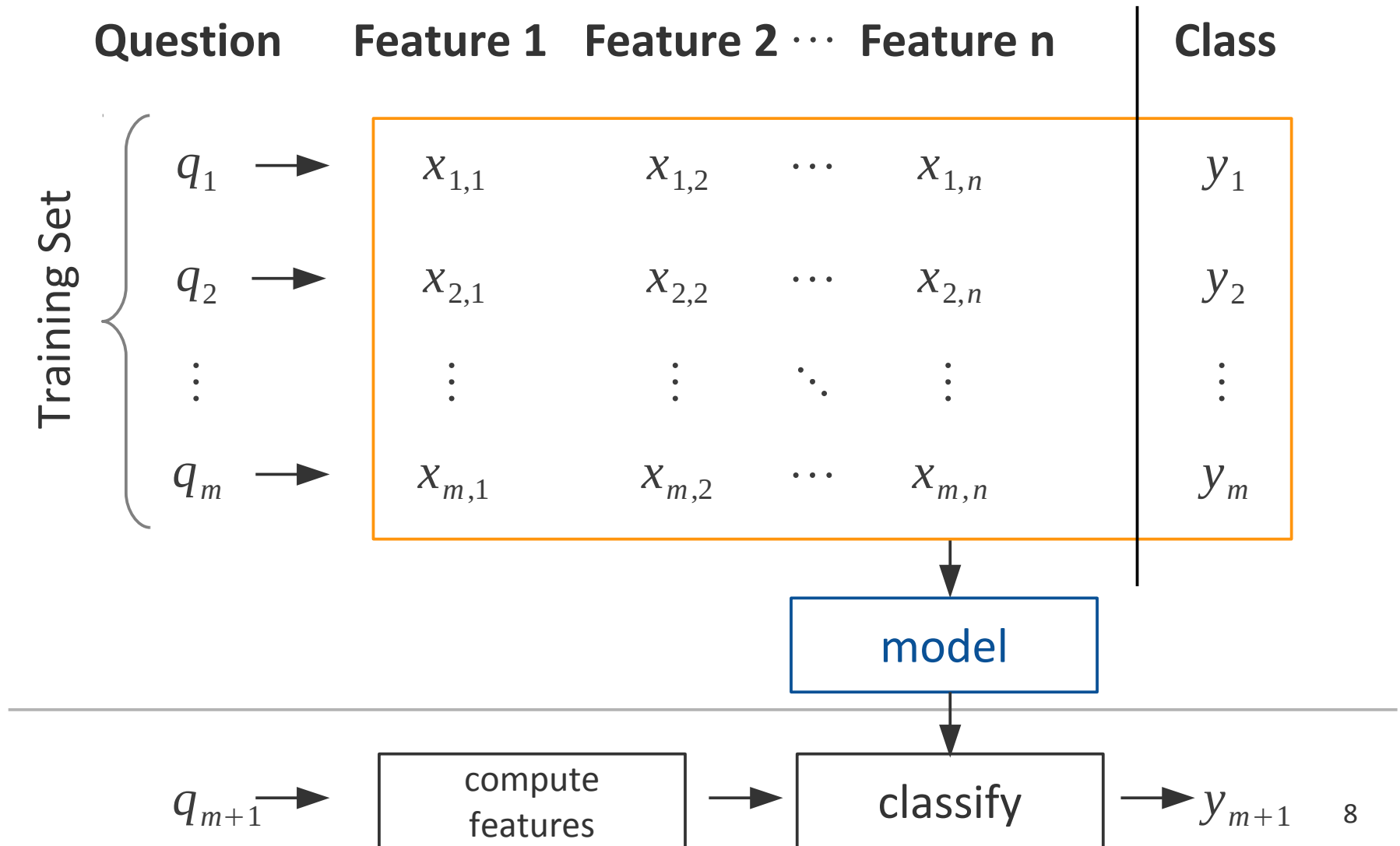
Location

Which / What



class by **head noun phrase**

Classification and Machine Learning



Hierarchical Classifiers



Question
Classification

Support Vector
Machines

Approach 1: Classifier

Question features

$$\mathbf{x}_i = [x_{i,1}, x_{i,2}, \dots, x_{i,n}]^T$$



Input confusion set

e.g. {abbr, entity, desc,
human, loc, num}



Classifier

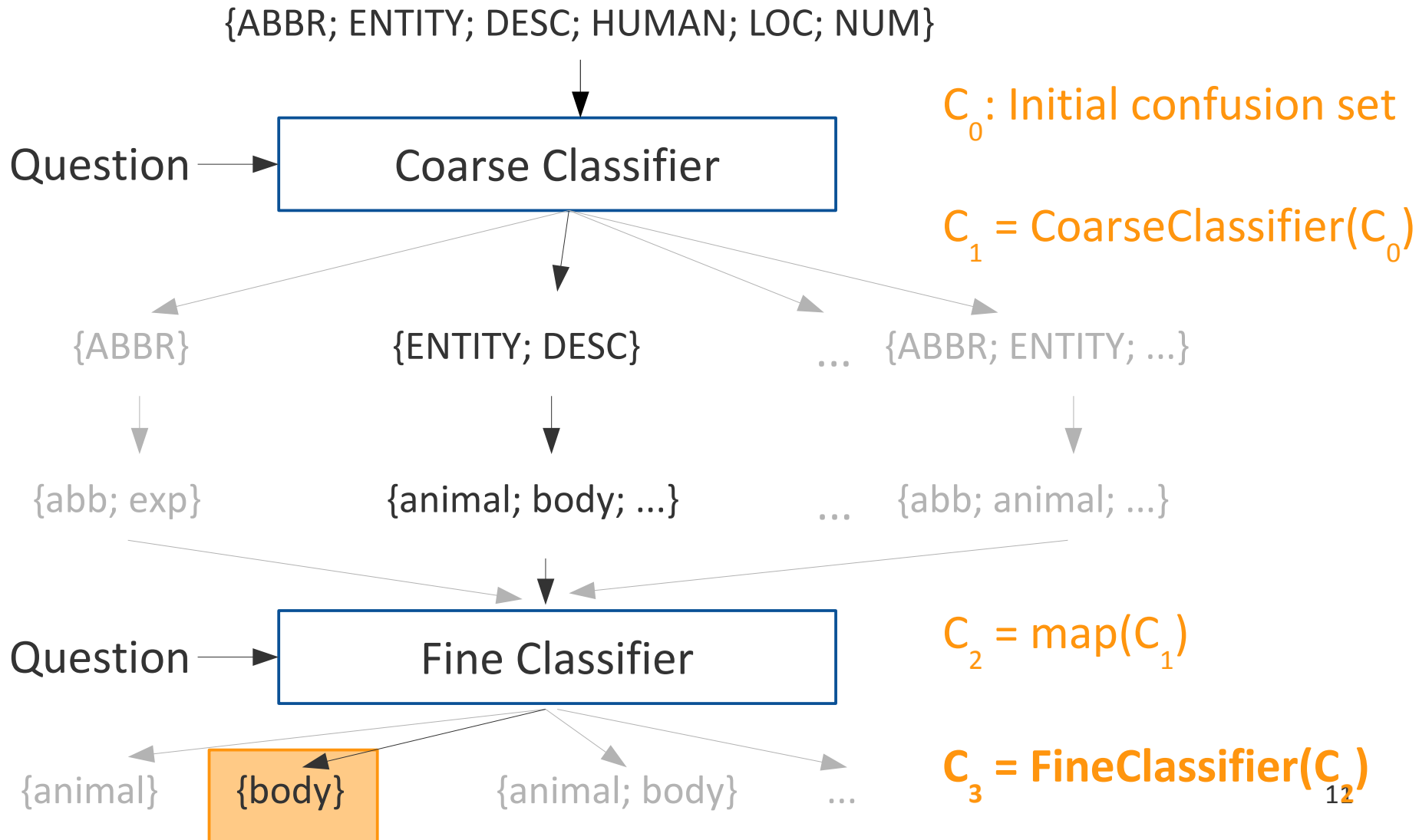
1. Compute density for each of the input classes (Winnow algorithm)
2. Sort classes by density
3. Output top k classes (k based on density threshold, max. 5)



Result confusion set

e.g. {entity, desc}

Hierarchical Classifier



Features

Simple features

(„sensors“)

basic

- words

syntactic

- part-of-speech tags
- (head) chunks

semantic

- named entities
- semantically related words

Complex features

- conjunctive (n-grams)
- relational features

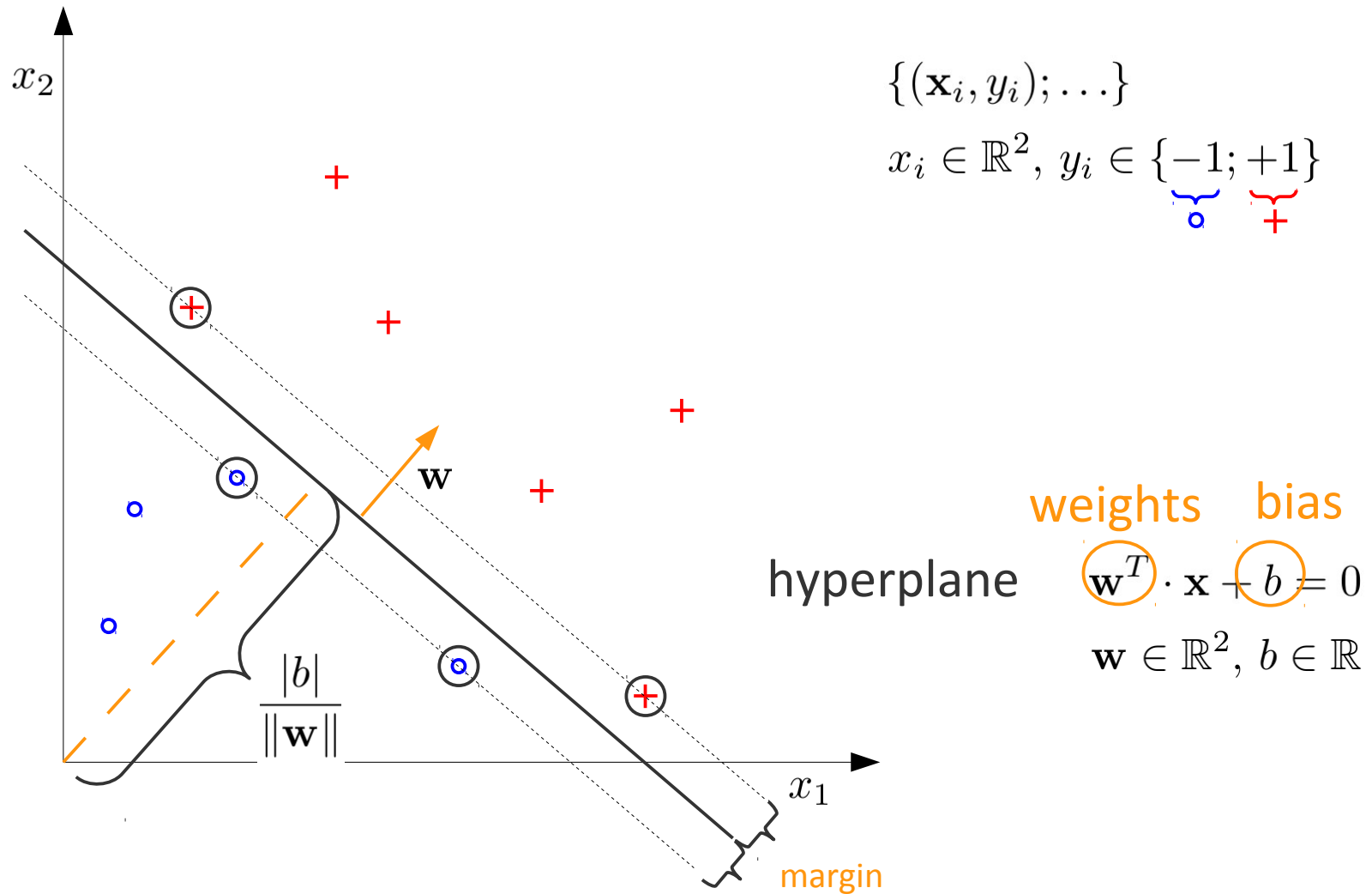
Hierarchical Classifiers



Question
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Linear Support Vector Machines



Linear Support Vector Machines

$$\text{hyperplane } \mathbf{w}^T \cdot \mathbf{x} + b = 0$$

1

training

find \mathbf{w} , b so the that hyperplane separates the data and the **margin** is maximal

2

classification

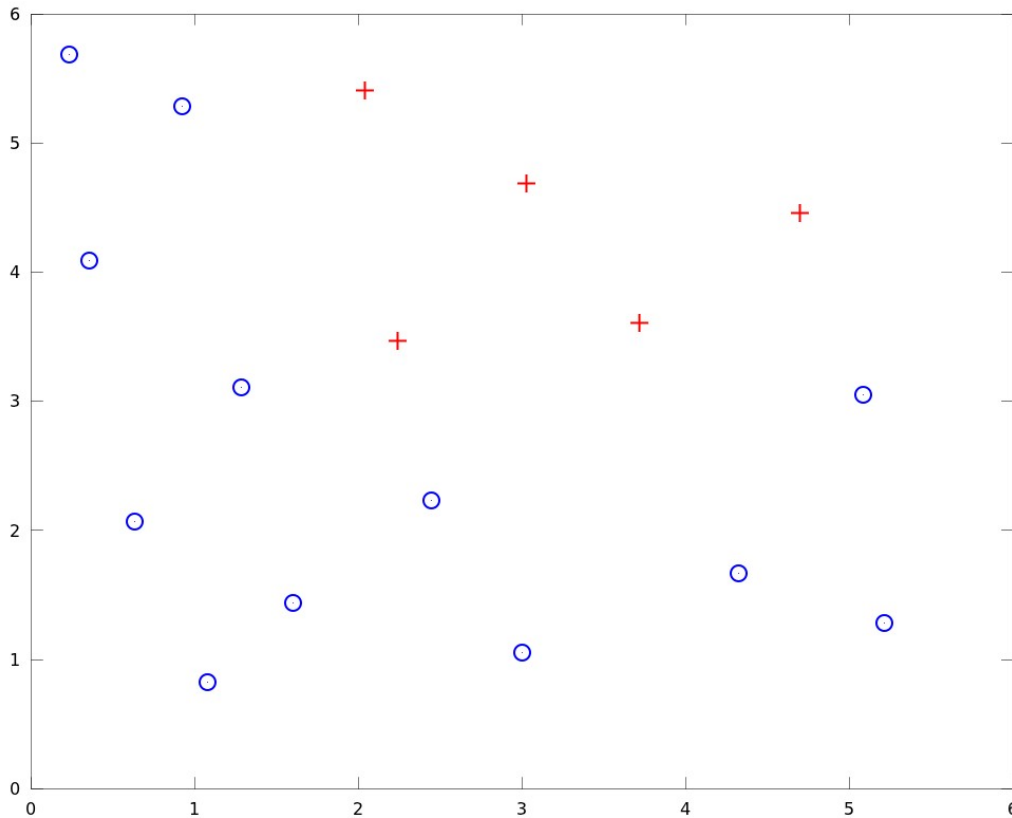
$$f(\mathbf{x}) = \begin{cases} +1 & \text{if } \mathbf{w}^T \cdot \mathbf{x} + b \geq 0 \\ -1 & \text{otherwise} \end{cases}$$

requires **dot product**
(for pairs for feature vectors)

$$\mathbf{x}^T \cdot \mathbf{y} = \sum_{i=0}^{i < d} x_i y_i$$

for $\mathbf{x}, \mathbf{y} \in \mathbb{R}^d$

Nonlinear Support Vector Machines



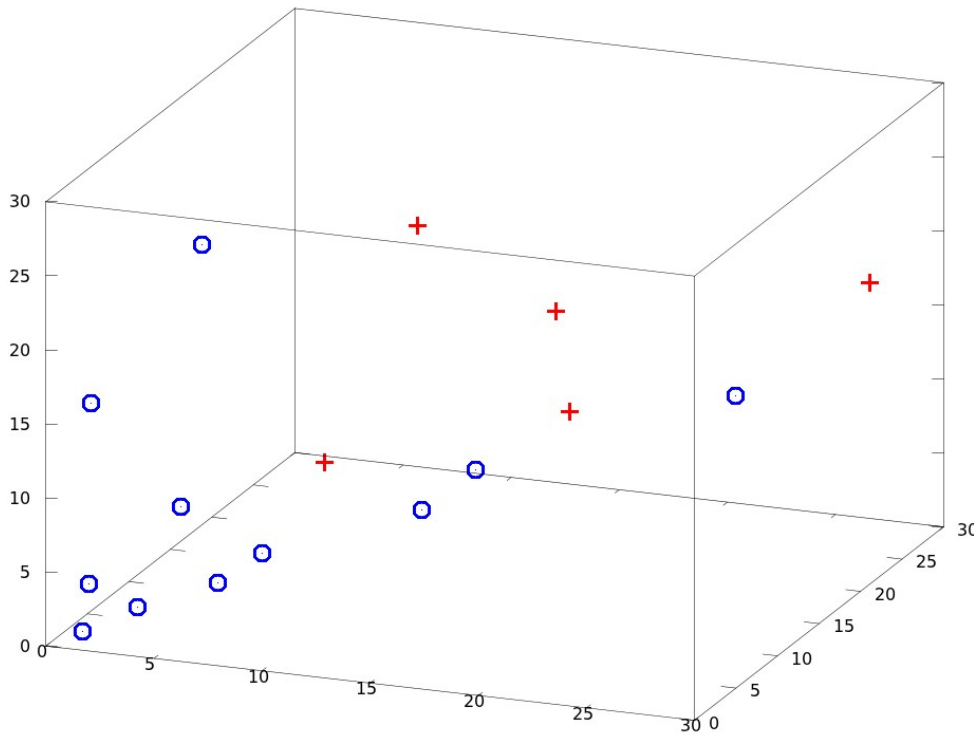
$$\{(\mathbf{x}_i, y_i); \dots\}$$

$$x_i \in \mathbb{R}^2, y_i \in \{-1; +1\}$$

$$\Phi : \mathbb{R}^2 \rightarrow \mathbb{R}^3$$

$$\Phi(\mathbf{x}) = \begin{bmatrix} x_1^2 \\ \sqrt{2}x_1x_2 \\ x_2^2 \end{bmatrix}$$

Nonlinear Support Vector Machines



$$\{(\mathbf{x}_i, y_i); \dots\}$$

$$x_i \in \mathbb{R}^2, y_i \in \{-1; +1\}$$

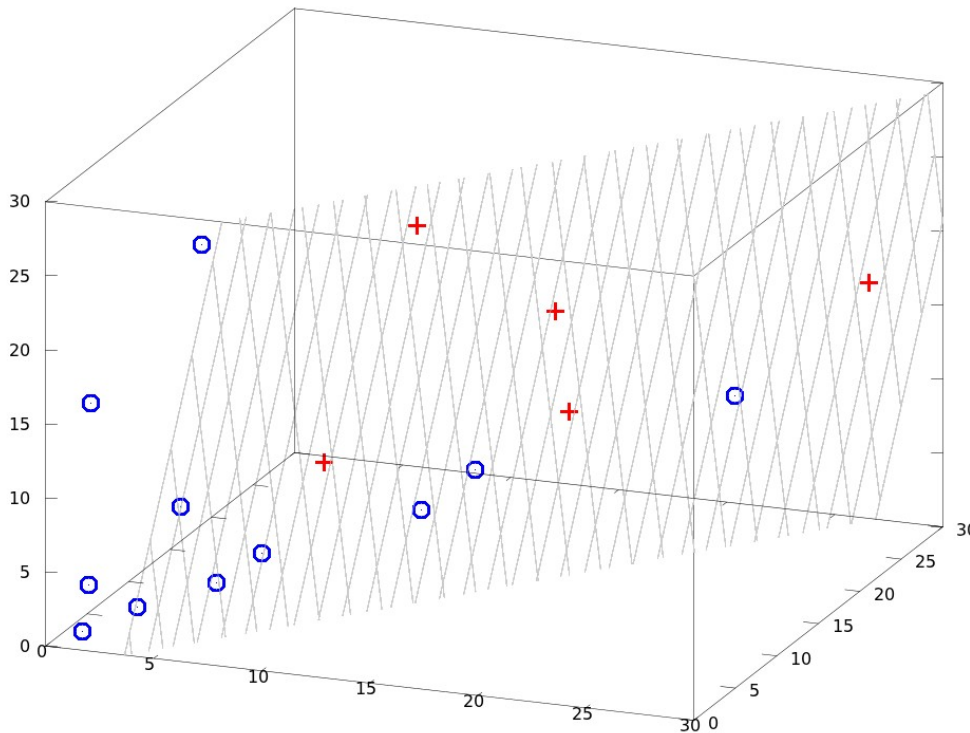
∘ +



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Nonlinear Support Vector Machines



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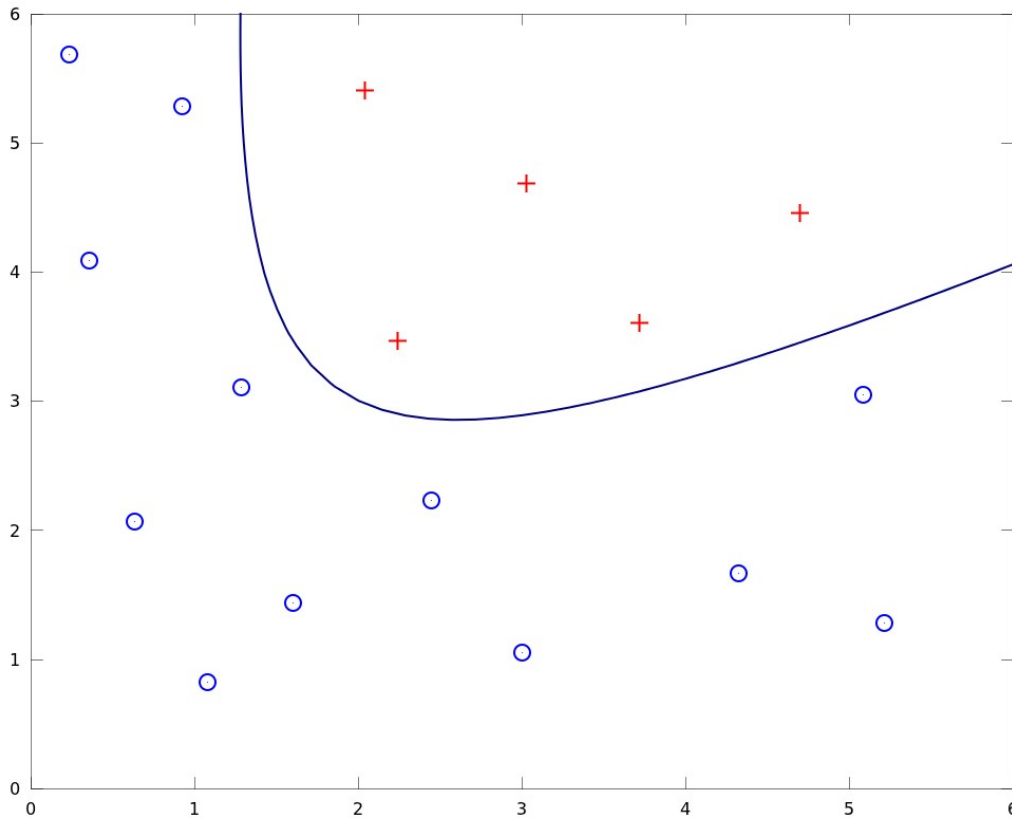
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$$\Phi(\mathbf{x}) = \begin{bmatrix} x_1^2 \\ \sqrt{2}x_1x_2 \\ x_2^2 \end{bmatrix}$$

$$\mathbf{w}^T \cdot \mathbf{x} + b = 0$$

Nonlinear Support Vector Machines



$$\{(\mathbf{x}_i, y_i); \dots\}$$

$$x_i \in \mathbb{R}^2, y_i \in \{-1; +1\}$$

$$\Phi : \mathbb{R}^2 \rightarrow \mathbb{R}^3$$

$$\Phi(\mathbf{x}) = \begin{bmatrix} x_1^2 \\ \sqrt{2}x_1x_2 \\ x_2^2 \end{bmatrix}$$

The Kernel Trick

How to compute this **efficiently**?

- Remember: we need **dot products**

kernel \swarrow \searrow $\Phi : \mathbb{R}^d \rightarrow \mathcal{H}$

$$\begin{aligned}
 K(\mathbf{x}, \mathbf{y}) &= \Phi(\mathbf{x})^T \cdot \Phi(\mathbf{y}) \\
 &= \begin{bmatrix} x_1^2 \\ \sqrt{2}x_1x_2 \\ x_2^2 \end{bmatrix}^T \cdot \begin{bmatrix} y_1^2 \\ \sqrt{2}y_1y_2 \\ y_2^2 \end{bmatrix} \\
 &= x_1^2y_1^2 + 2x_1x_2y_1y_2 + x_2^2y_2^2 \\
 &= (x_1y_1)^2 + 2(x_1y_1)(x_2y_2) + (x_2y_2)^2 \\
 &= (x_1y_1 + x_2y_2)^2 \\
 &= \boxed{(\mathbf{x} \cdot \mathbf{y})^2}
 \end{aligned}$$

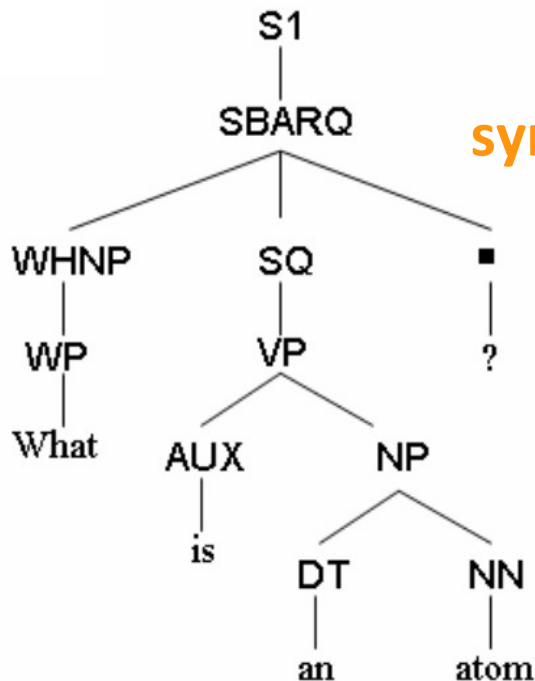
$$\Phi : \mathbb{R}^2 \rightarrow \mathbb{R}^3$$

$$\Phi(\mathbf{x}) = \begin{bmatrix} x_1^2 \\ \sqrt{2}x_1x_2 \\ x_2^2 \end{bmatrix}$$

Features

„Which univerity did the president graduate from?“

„Which president is a graduate of the Harvard University?“

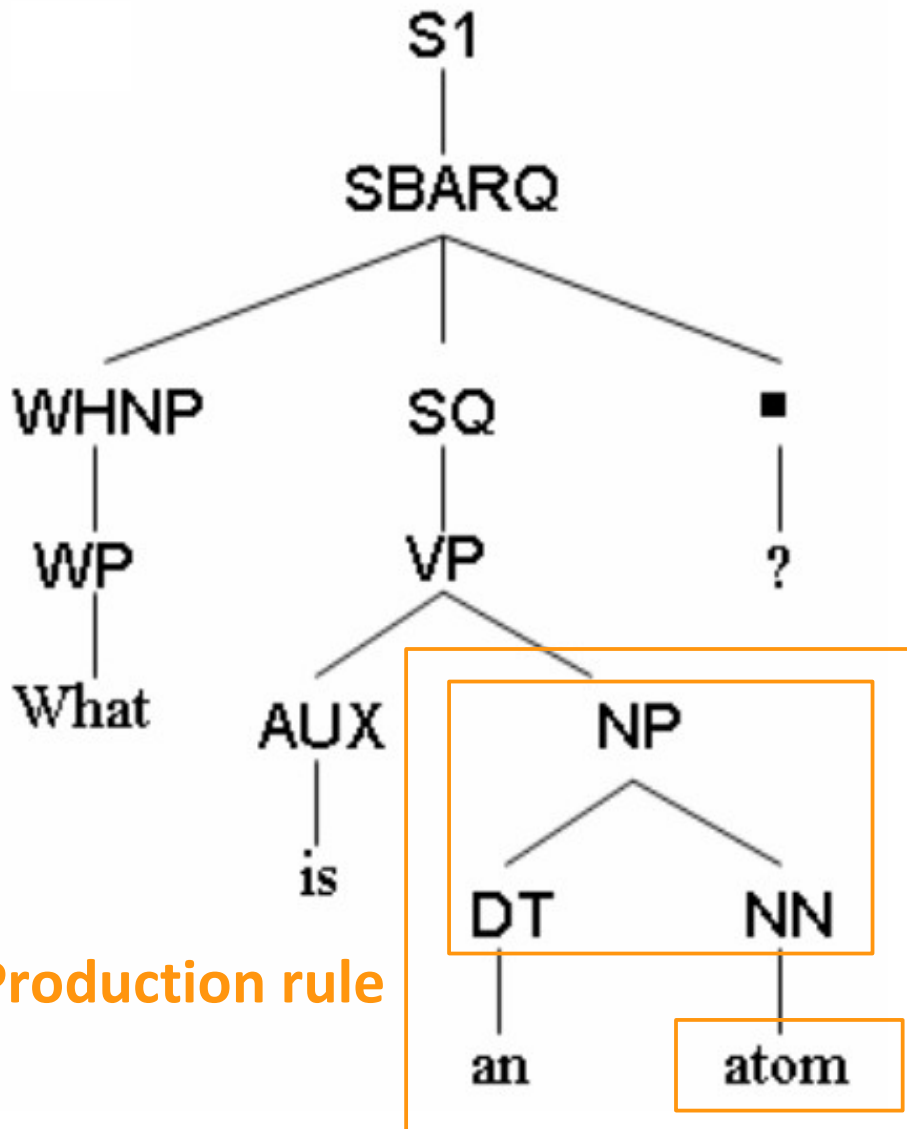


syntax tree

tree kernel

$$K(T_1, T_2) = \mathbf{v}(T_1) \cdot \mathbf{v}(T_2)$$

Tree Fragments



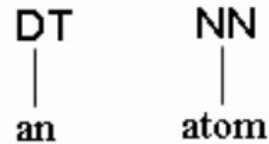
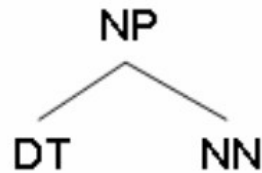
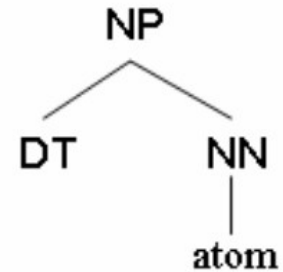
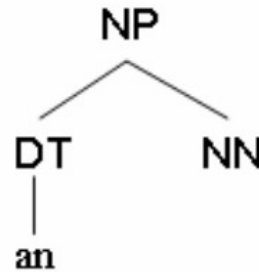
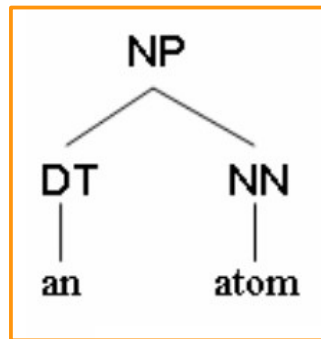
Production rule

Tree fragment

- at least one production rule / terminal symbol
- no incomplete production rule

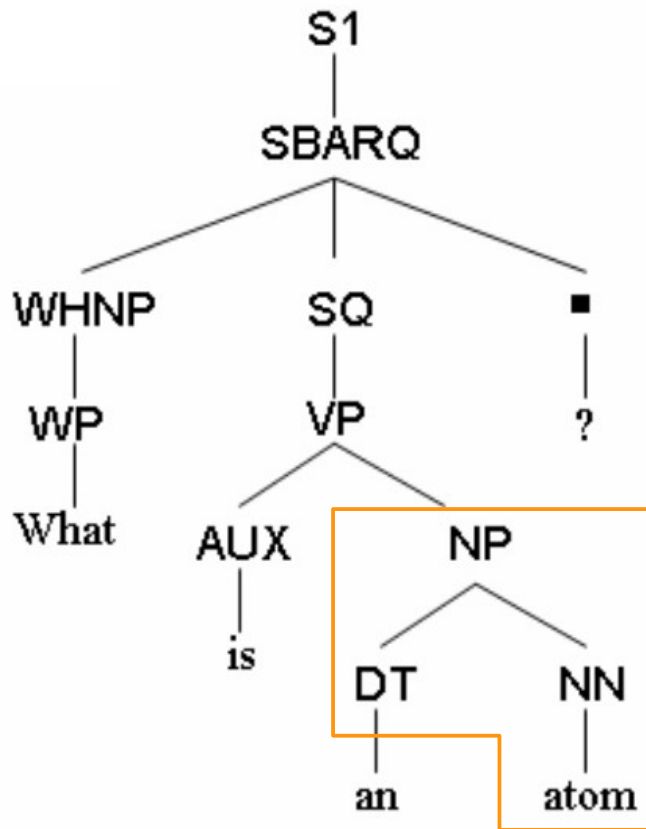
terminal symbol

Tree Fragments



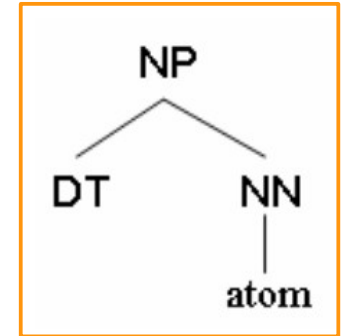
an atom

Tree Fragments: Weight



syntax tree **T**

tree fragment **i**



$s(i)$ = size of **i** (here: 2)

$$v_i(T) = \begin{cases} \sqrt{\lambda}^{s(i)} \cdot \sqrt{\mu}^{d(i)} & \text{if } i \text{ is in } T \\ 0 & \text{otherwise} \end{cases}$$

$0 \leq \lambda \leq 1, 0 \leq \mu \leq 1$

$d(i)$ = depth of **i** in **T**
(here: 4)

Tree Kernel

$$\mathbf{v}(T) = \begin{bmatrix} v_1(T) \\ v_2(T) \\ \vdots \\ v_m(T) \end{bmatrix} \text{ for all tree fragments } v_i$$

$$K(T_1, T_2) = \mathbf{v}(T_1) \cdot \mathbf{v}(T_2)$$



dynamic programming algorithm in $O(|N_1| \cdot |N_2|)$

Summary and evaluation

- Approach 1: **Hierarchical Classifiers**
 - **Coarse-grained categories:** 91.00 % accuracy
 - **Fine-grained categories:** 84.20 % accuracy

- Approach 2: **Support Vector Machines with tree kernels**
 - **Coarse-grained categories:** 90.00 % accuracy
 - **Fine-grained categories:** Slight improvements compared to word/n-gram kernel
(*“The experiment results are omitted to save space”*)

training set: 5500 questions, **test set:** 500 questions

References

- Xin Li, Dan Roth: *Learning Question Classifiers*, COLING Conference, 2002
- Dell Zhang, Wee Sun Lee: *Question Classification using Support Vector Machines*, SIGIR Conference, 2003
- Xin Li, Dan Roth: *Learning Question Classifiers: The Role of Semantic Information*, Journal of Natural Language Engineering, 2004
- Christopher J.C. Burges: *A Tutorial on Support Vector Machines for Pattern Recognition*, Data Mining and Knowledge Discovery 2, 121-167, 1998
- Andrew Ng: *CS229 Lecture Notes Part V: Support Vector Machines*, Stanford University