



## Functional Dependency Discovery: An Experimental Evaluation of Seven Algorithms

**Thorsten Papenbrock**, Jens Ehrlich, Jannik Marten, Tommy Neubert,  
Jan-Peer Rudolph, Martin Schönberg, Jakob Zwiener, Felix Naumann

# Motivation

## Functional Dependencies and Normalization

Name	Surname	Postcode	City	Mayor
Thomas	Miller	14482	Potsdam	Jakobs
Sarah	Miller	14482	Potsdam	Jakobs
Peter	Smith	60329	Frankfurt	Feldmann
Jasmine	Cone	01069	Dresden	Orosz
Thomas	Cone	14482	Jakobs	
Mike	Moore	60329	Frankfurt	Feldmann

Definition FD:  $X \rightarrow A$

- All values in X uniquely define the values in A.
- If  $t_1[X] = t_2[X]$ , then  $t_1[A] = t_2[A]$ .

Postcode  $\rightarrow$  City  
 Postcode  $\rightarrow$  Mayor

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## Functional Dependencies and Normalization

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<b>Postcode</b>	<b>City</b>	<b>Mayor</b>
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**Less Memory Consumption  
Less Anomaly Vulnerability**

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Postcode  $\rightarrow$  City  
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## Motivation

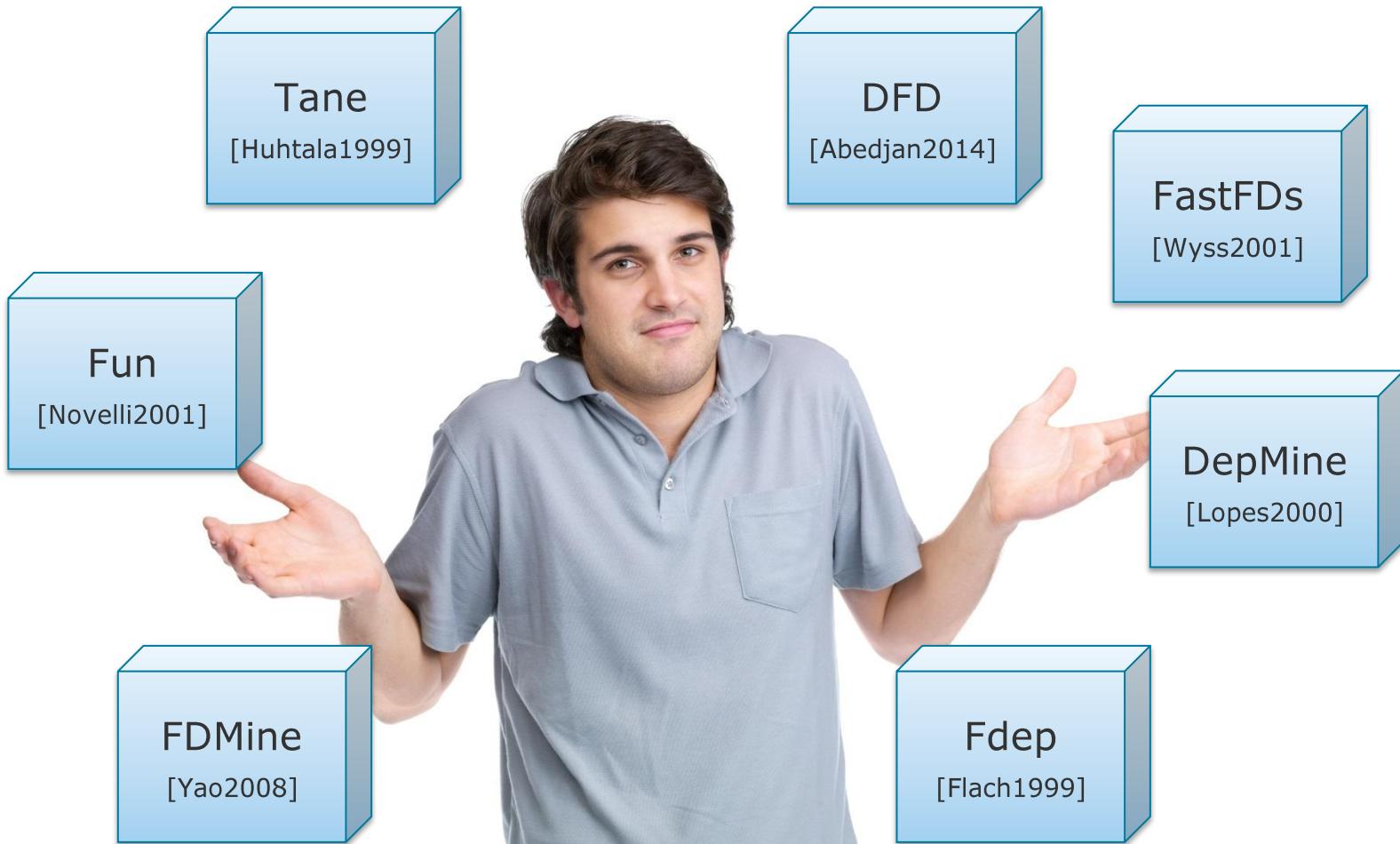
### Very large Tables e.g. uniprot

name	references	pubmed	keywords	gene	ontology	protein	existence	virus	host	ncbi	sequence	sequence	length	sequence	mass	sequence	checksum	sequence	modified	taconomic	taxonomic	lineage	protein	names	gene	orf	cross	reference	cross	ref				
017L_FRG3G	15165820		Complete proteome; Reference predicted			8295	8316	8404	3034	METMSDYSKEVSE,502	53469	A747EEF952CBA07	2004-07-19+01:00	654924	Viruses > dsDNA virus< Uncharacterized p	FV3-017L	AY548484; AAT09671Y_P_031595																	
040R_FRG3G	15165820		Complete proteome; Reference predicted			8295	8316	8404	3034	MIRALCTVILIAAGV,182	19577	FCF64F420039CF35	2004-07-19+01:00	654924	Viruses > dsDNA virus< Uncharacterized p	FV3-040R	AY548484; AAT09695Y_P_031618																	
057L_IIV3	15084204		Complete proteome; Reference predicted			7462	7483	7504	2404	MKHKWWTSCMCHQH,120	11915	C40E5A3297FAB855	2005-07-14+01:00	345391	Viruses > dsDNA virus< Uncharacterized p	IIV3-057L	AY542382; AAT09295Y_P_054629																	
078L_FRG																																		
1001R_AS			accession, name, references_pubmed, keywords, gene_ontology, protein_existence, virus_host_ncbi, sequence, sequence_length, sequence_mass, sequence_checksum, sequence_modified, taconomic_identifier, taxonomic_lineage, protein_names, gene_orf, cross_reference_embl, cross_reference_refseq, cross_reference_geneid, cross_reference_protclustdb, feature_chain, feature_compositionally_biased_region, feature_signal_peptide, gene_ordered_locus, comment_function, comment_similarity, cross_reference_interpro, cross_reference_pfam, feature_glycosylation_site, cross_reference_go, feature_transmembrane_region, feature_coiled-coil_region, comment_subcellular_location, gene_primary, gene_synonym, cross_reference_pir, cross_reference_proteinmodelportal, cross_reference_smr, cross_reference_dip, cross_reference_intact, cross_reference_mint, cross_reference_string, cross_reference_paxdb, cross_reference_pride, cross_reference_ensemblmetazoa, cross_reference_kegg, cross_reference_ucsc, cross_reference_ctd, cross_reference_wormbase, cross_reference_eggnog, cross_reference_genetree, cross_reference_hogenom, cross_reference_inparanoid, cross_reference_ko, cross_reference_oma, cross_reference_nextbio, cross_reference_arrayexpress, cross_reference_gene3d, cross_reference_panther, cross_reference_pirst, cross_reference_prints, cross_reference_smart, cross_reference_supfam, cross_reference_prosite, feature_sequence_conflict, comment_subunit, comment_interaction, cross_reference_ipi, cross_reference_unigene, cross_reference_ensemblplants, cross_reference_genomereviews, cross_reference_tair, cross_reference_genevestigator, cross_reference_germonline, feature_modified_residue, cross_reference_ensembl, cross_reference_hovergen, cross_reference_orthodb, feature_site, cross_reference_patric, cross_reference_biocyc, feature_lipid_moiety-binding_region, cross_reference_ec, cross_reference_gramene, cross_reference_unipathway, comment_catalytic_activity, comment_cofactor, comment_pathway, comment_induction, cross_reference_hamap, cross_reference_tigrfams, feature_active_site, cross_reference_pdb, cross_reference_pdbsum, cross_reference_evolutionarytrace, feature_helix, feature_strand, feature_turn, cross_reference_dmddm, cross_reference_genecards, cross_reference_hgnc, cross_reference_mim, cross_reference_nextprot, cross_reference_fam, cross_reference_fam, feature_domain, feature_region_of_interest, feature_disulfide_bond, feature_sequence_variant, comment_ptm, comment_reactive, cross_reference_reactome, cross_reference_genomernal, cross_reference_bggee, cross_reference_lipid, cross_reference_phosphosite, cross_reference_dnasu, cross_reference_phylomedb, cross_reference_pathway, feature_splice_variant, comment_alternative_products, comment_tissue_specificity, feature_non-terminal, consecutive_residues, cross_reference_prodrom, feature_initiator_methionine, feature_binding_site, cross_reference_amino_acid, feature_sequence_caution, cross_reference_ensemblbacteria, cross_reference_genolist, cross_reference_enzyme, cross_reference_ecoli, cross_reference_chembio, cross_reference_mgi, cross_reference_flybase, feature_propeptide, feature_transit_peptide, cross_reference_tuberculist, cross_reference_candida, merops, comment_developmental_stage, cross_reference_arachnoserver, comment_toxic_dose, cross_reference_cazy, cross_reference_blast, cross_reference_cygd, cross_reference_sgd, cross_reference_peptideatlas, cross_reference_drugbank, cross_reference_tcdb, comment_physicochemical_properties, cross_reference_promex, cross_reference_pombase, cross_reference_swiss-2dpage, cross_reference_echobase, cross_reference_ecogene, cross_reference_rgd, cross_reference_pmap_ctdb, comment_caution, feature_zinc_finger_region, feature_cross-link, cross_reference_vectorbase, feature_unsure_residue, feature_dna_binding_region, cross_reference_pseudocap, cross_reference_orphanet, comment_disease, cross_reference_ensemblprotists, cross_reference_dictybase, cross_reference_world-2dpage, cross_reference_xenbase, feature_calcium-binding_region, comment_mass_spectrometry, feature_peptide, cross_reference_genefarm, cross_reference_peroxibase, cross_reference_maize gdb, cross_reference_allergome, comment_allergen, cross_reference_glycositedb, cross_reference_cornea-2dpage, cross_reference_dosac-cobs-2dpage, cross_reference_ogp, cross_reference_reproduction-2dpage, cross_reference_sienna-2dpage, cross_reference_ucd-2dpage, cross_reference_agd, cross_reference_bindingdb, cross_reference_phossite, cross_reference_legiolist, feature_intramembrane_region, cross_reference_cgd, cross_reference_disprot, comment_rna_editing, comment_biotecnology, cross_reference_conoserver, cross_reference_pmma-2dpage, cross_reference_mycoclad, comment_pharmaceutical, cross_reference_phci-2dpage, cross_reference_eupathdb, cross_reference_leprroma, cross_reference_rebase, cross_reference_compluyeast-2dpage, feature_non-standard_amino_acid, cross_reference_aarhus/ghent-2dpage, cross_reference_euhcvdb, cross_reference_rat-heart-2dpage, cross_reference_pptasedb, cross_reference_anu-2dpage, cross_reference_2dbase-ecoli	15489334; 16141072; 1946 Acetylation; Alternative splicing; evidence at transcript level	MTAKATVLMRQPGRV,292	33578	3AE26BCE06833085	2008-04-08+01:00	10090	Eukaryota > Metazoa > Cytosolic 5'-nucleotidase III	I	I	I	I	I	B015307; AAH1530	NP_1808837																	
60A_DROVI	8688461		Cytokine; Disulfide bond; Glyco inferred from homology								MTASLVLVPLSLWL,436	49999	C744BAE58796692	1997-11-01Z	7244	Eukaryota > Metazoa > Protein 60A																		
9727_PAPU											MMLMILVYVYVTLV,129	14074	C744BAE58796692	1997-11-01Z	2129	Eukaryota > Metazoa > Protein 9727																		
5NT3_MOUSE	15489334																																	
5056R_AS																																		
5565_RAT																																		
5HT1B_RA																																		
5HT2A_PI																																		
5HT5A_HU																																		

223 attributes!



## Motivation Functional Dependencies Discovery



## FD Algorithm Classes



## Experimental Evaluation



## Extrapolation of Results

Boeing 747-451



Boeing 767-432(ER)



Boeing 757-351



Boeing 737-832

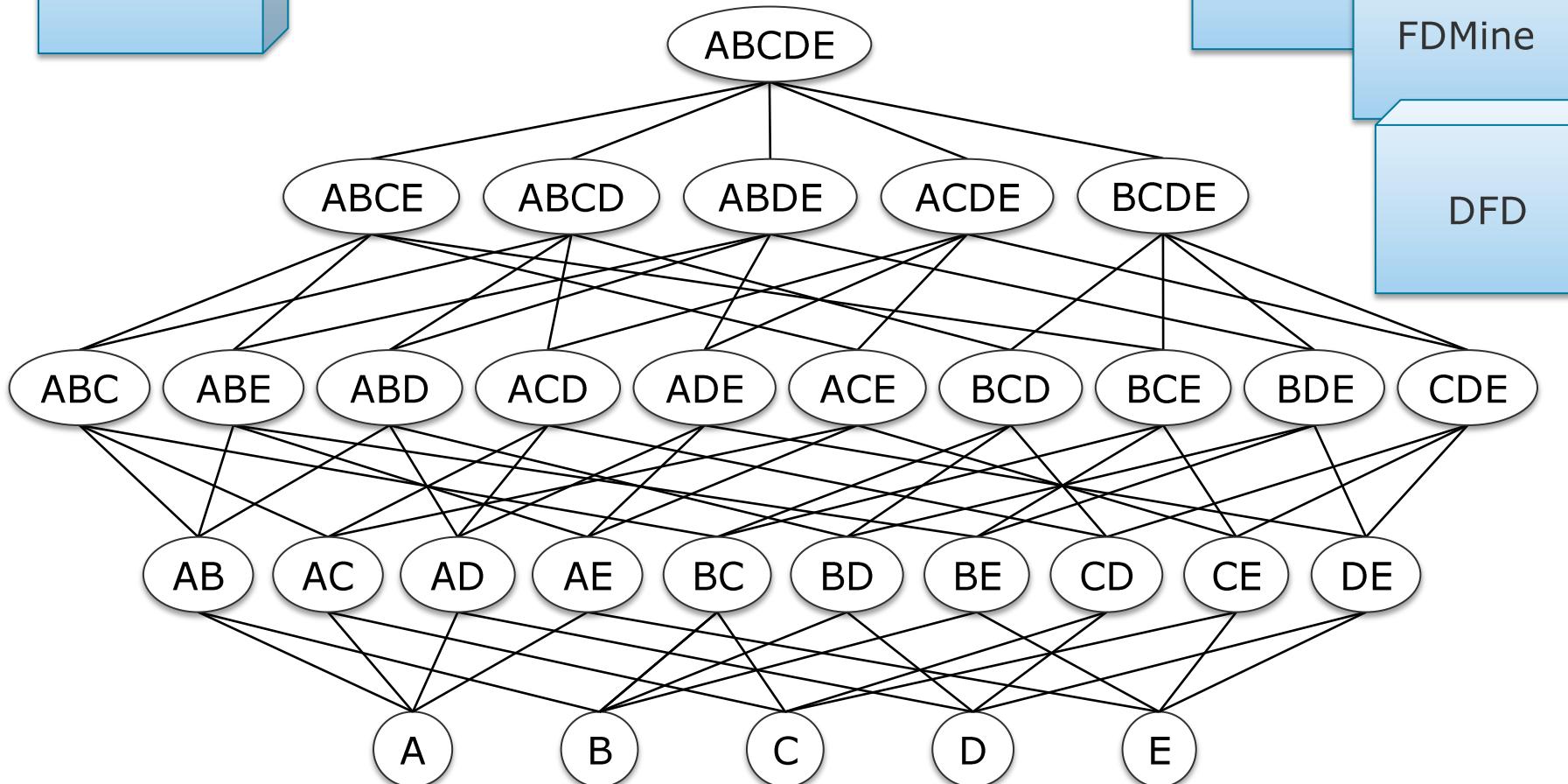
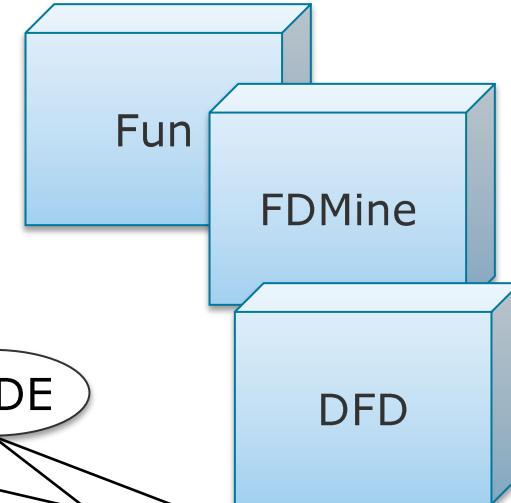


Boeing 737-732

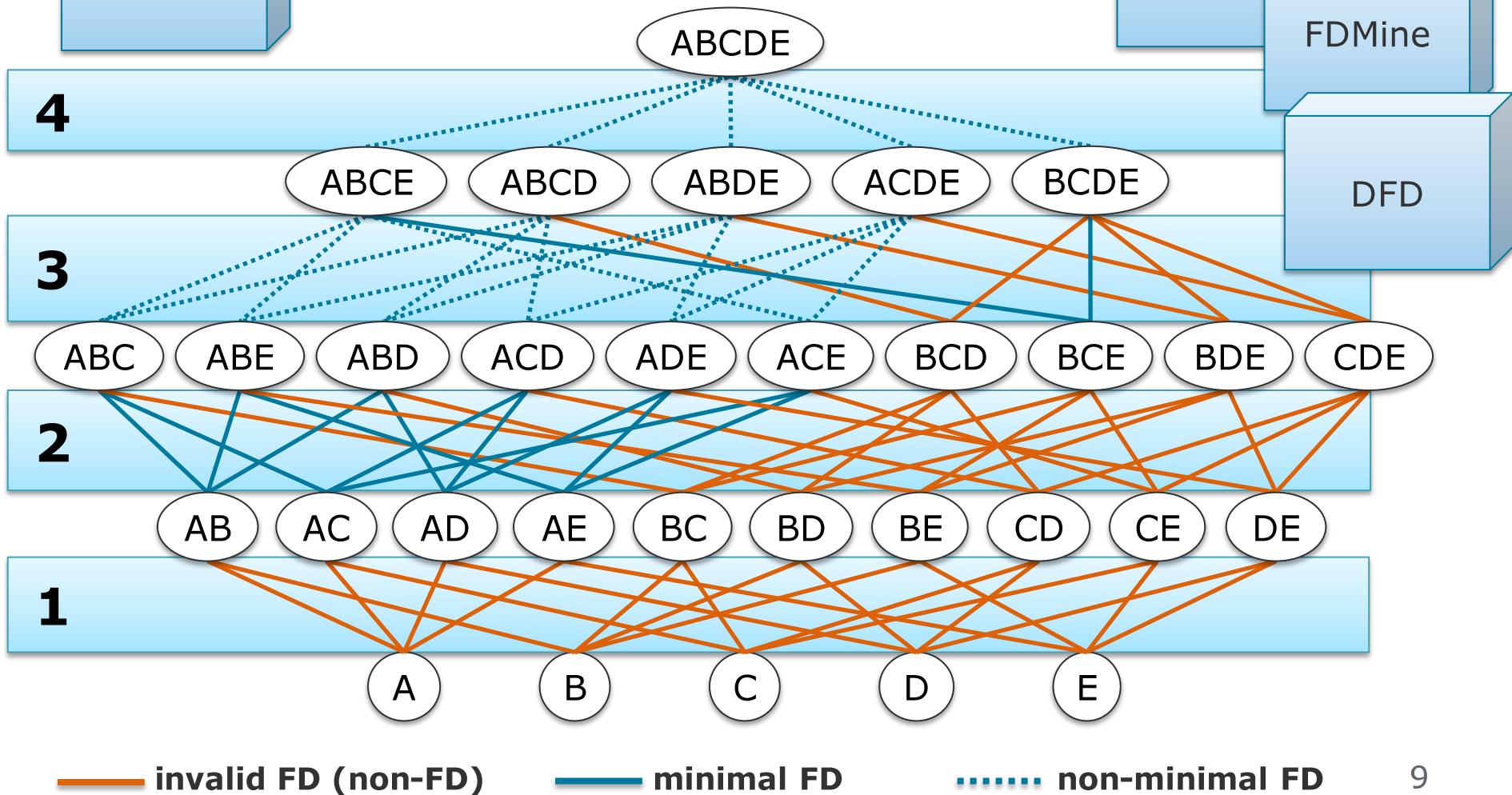




## FD Algorithm Classes Lattice Traversal Algorithms



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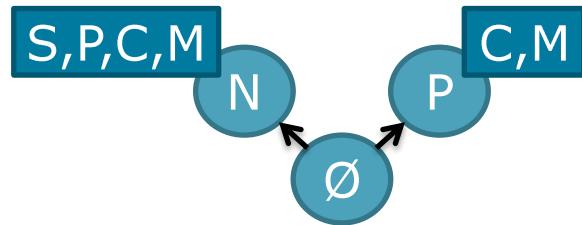


# FD Algorithm Classes

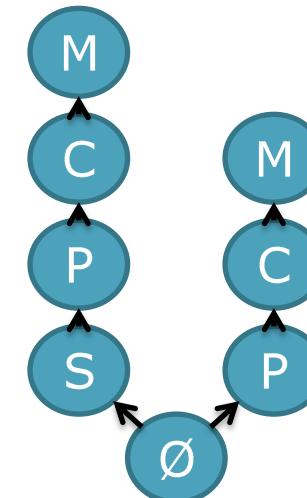
## Dependency Induction Algorithms

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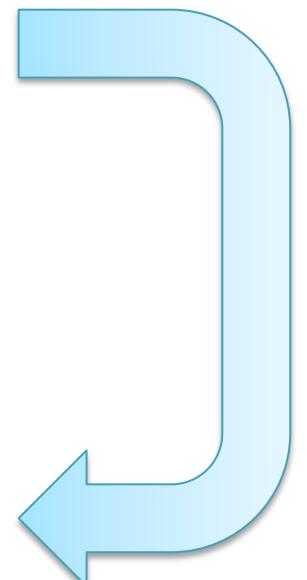
N,P,C,M  $\nrightarrow$  S



Positive Cover

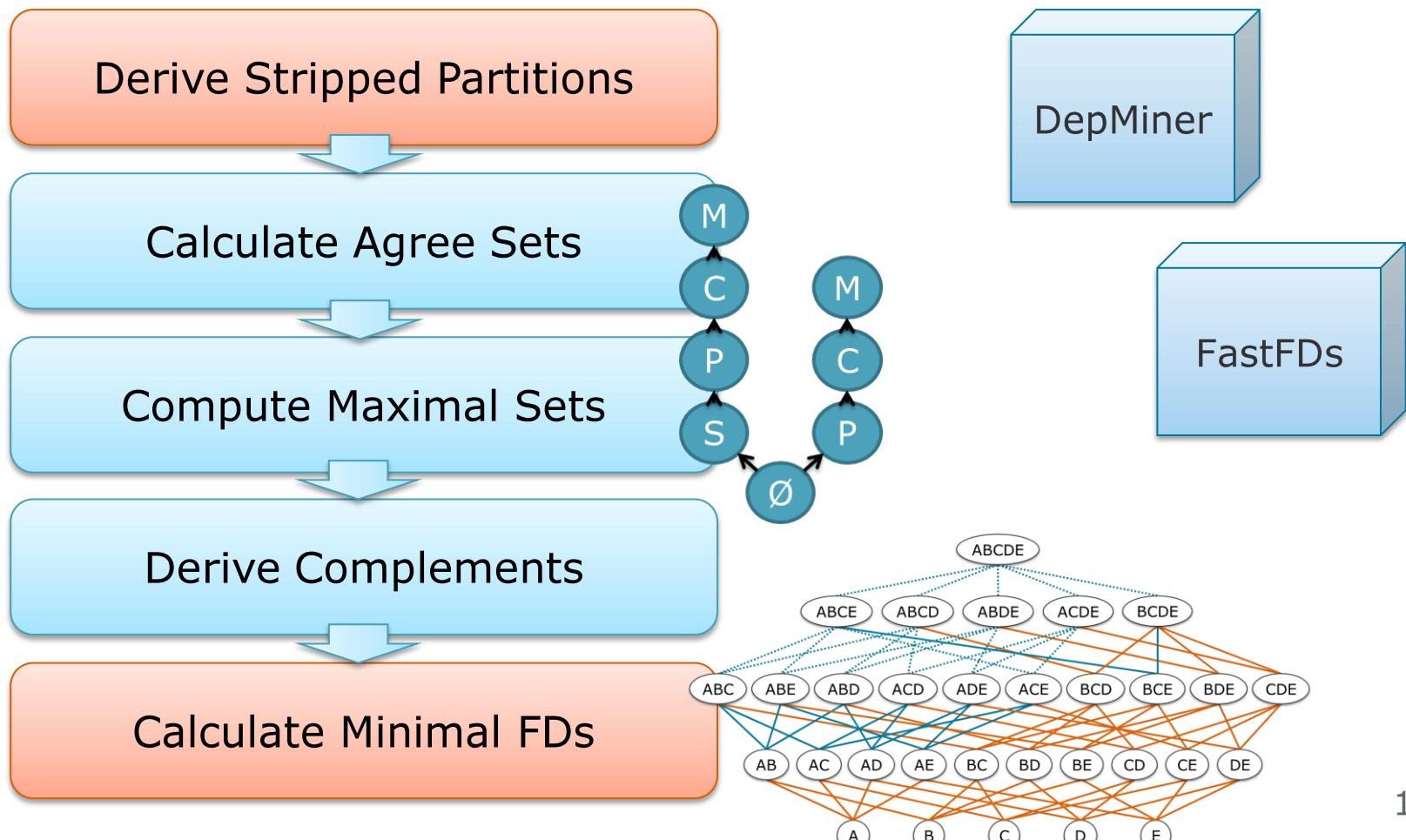


Negative Cover



# FD Algorithm Classes

## Difference- and Agree-Set Algorithms





## FD Algorithm Classes

## Experimental Evaluation



## Extrapolation of Results

Boeing 747-451



Boeing 767-432(ER)



Boeing 757-351



Boeing 737-832

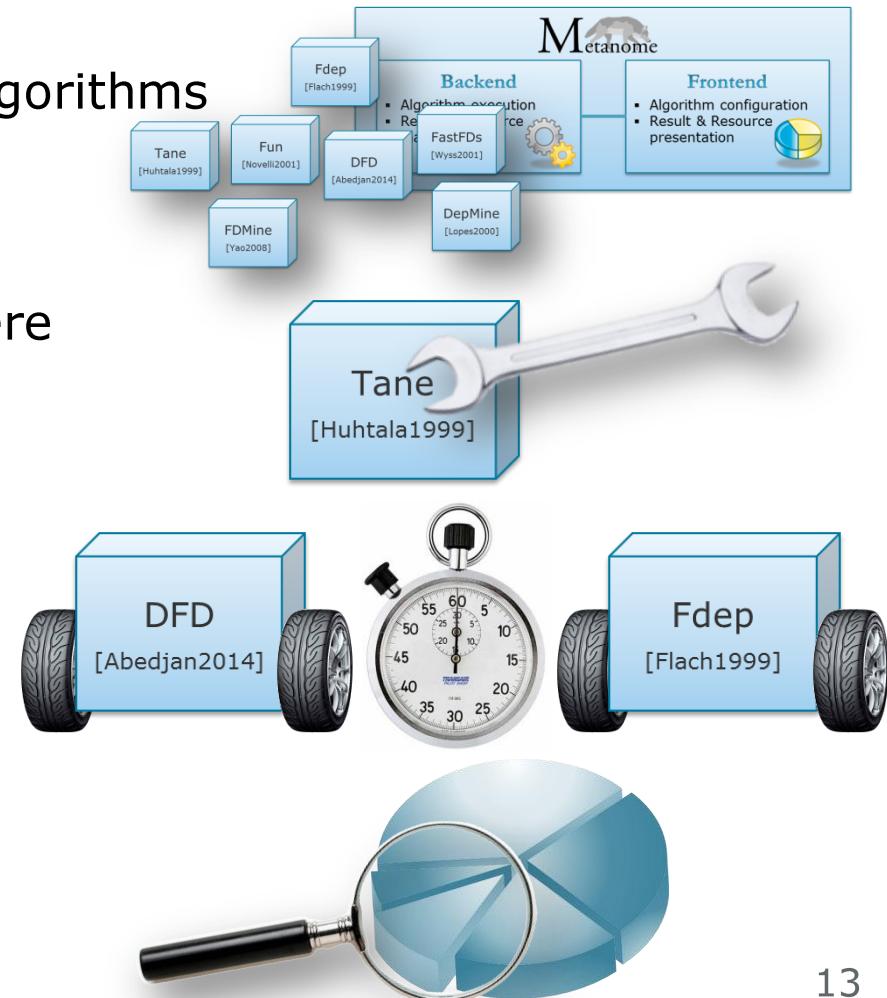


Boeing 737-732



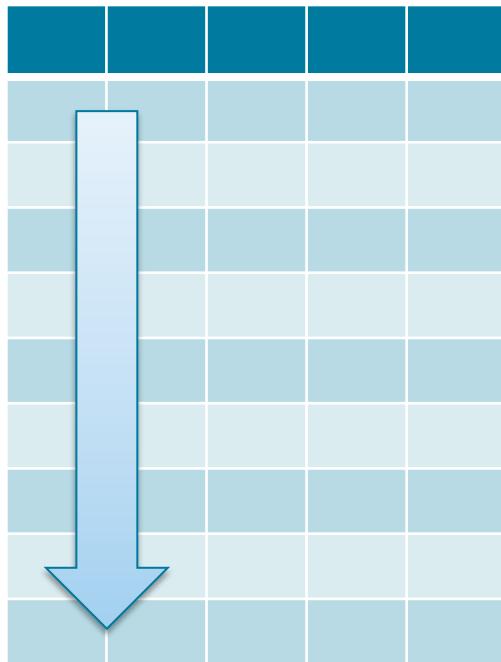
## Experimental Evaluation Contributions

- We **re-implemented** all seven algorithms for the Metanome profiling tool.
- We **amended** the algorithms where original descriptions were sparse.
- We **evaluated** the algorithms under comparable conditions.
- We **analyzed** and extrapolated the experimental results.

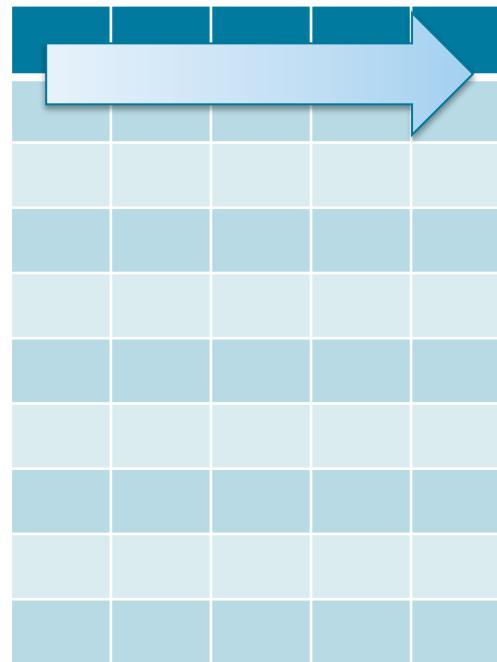


## Experimental Evaluation Evaluation Strategy

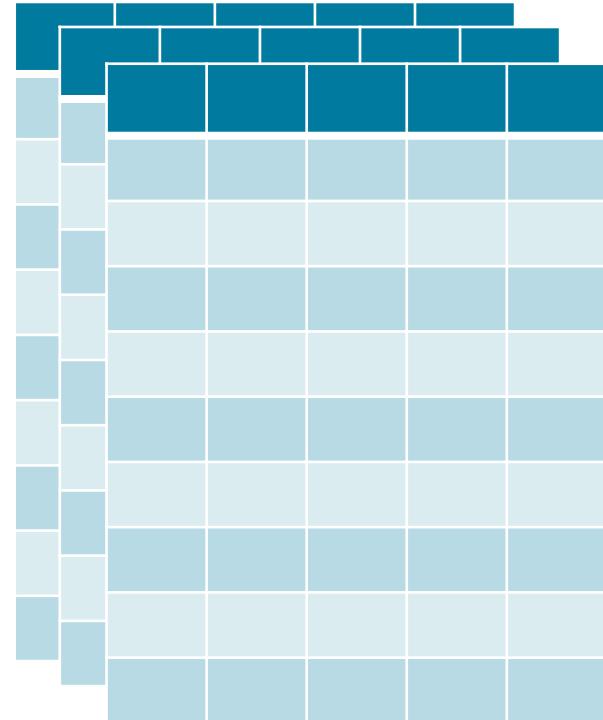
### Row Scalability



### Column Scalability

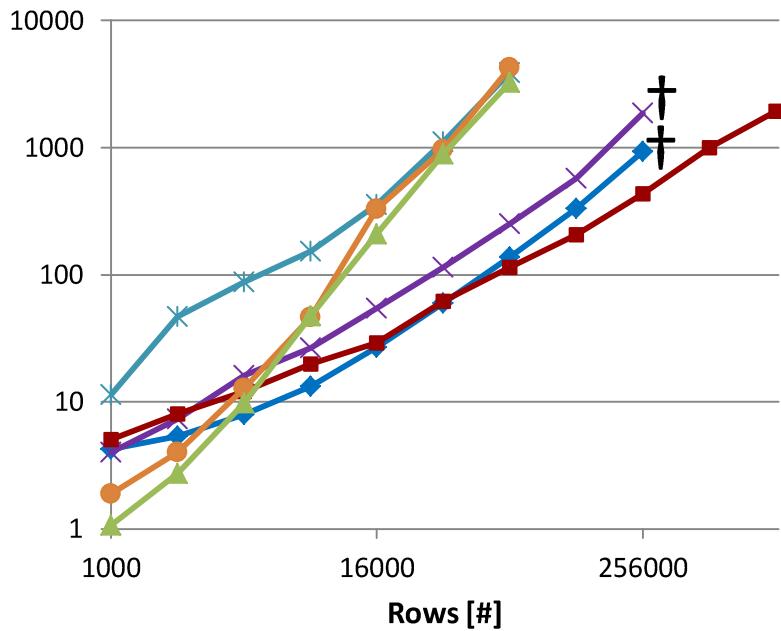


### Different Datasets

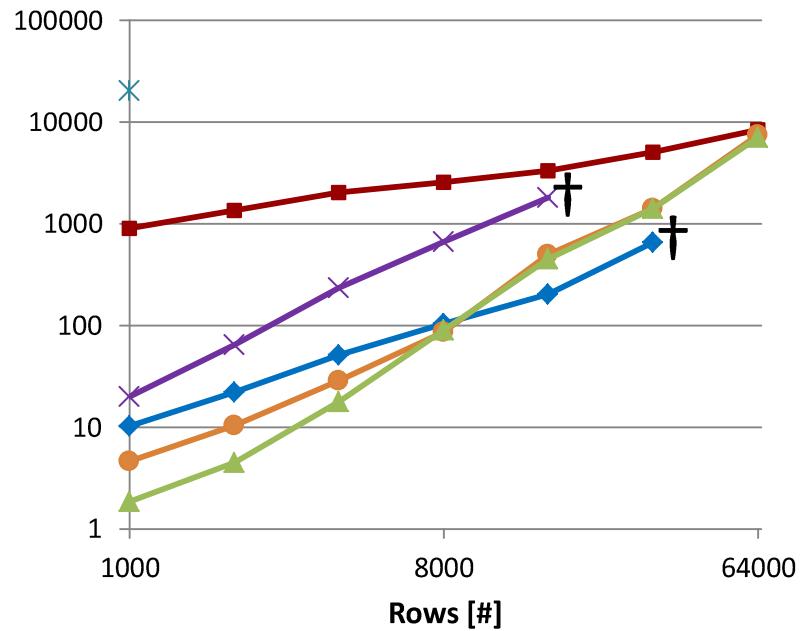


# Experimental Evaluation Row-Scalability

**ncvoter dataset (19 columns)**



**uniprot dataset (30 columns)**

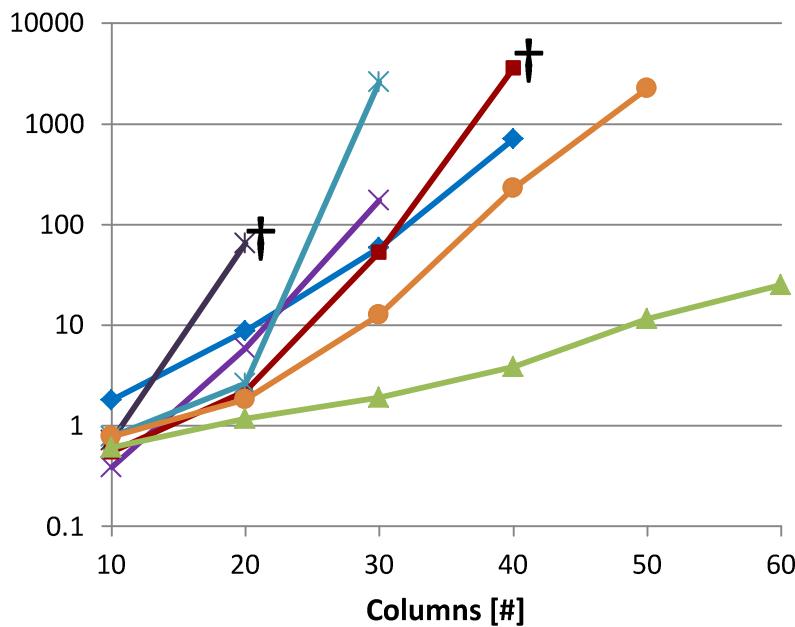


 Tane       FUN       FD\_Mine       DFD  
 Dep-Miner       FastFDs       Fdep      ..... FDs

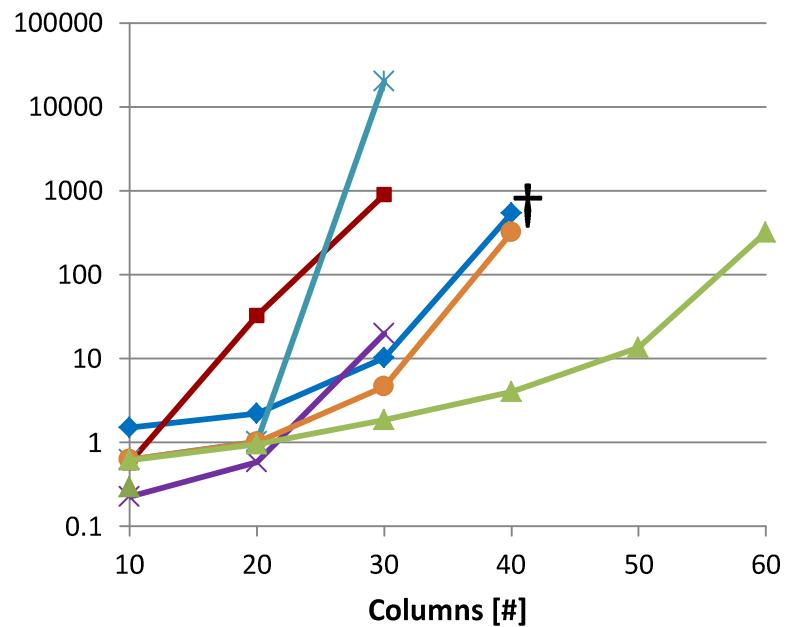
† 100 GB memory exhausted

## Experimental Evaluation Column-Scalability

**plista dataset (1000 rows)**



**uniprot dataset (1000 rows)**



 Tane       Dep-Miner       FUN       FD\_Mine       FastFDs  
 Fdep      ..... FDs

† 100 GB memory exhausted

# Experimental Evaluation

## Different Datasets

Dataset	Columns [#]	Rows [#]	Size [KB]	FDs [#]	Runtime [sec]						
					TANE [7]	FUN [15]	FD_MINE [21]	DFD [1]	DEP-MINER [12]	FASTFDs [20]	FDEP [6]
iris	5	150	5	4	1.1	0.1	0.2	0.2	0.2	0.2	0.1
balance-scale	5	625	7	1	1.2	0.1	0.2	0.3	0.3	0.3	0.2
chess	7	28,056	519	1	2.9	1.1	3.8	1.0	174.6	164.2	125.5
abalone	9	4,177	187	137	2.1	0.6	1.8	1.1	3.0	2.9	3.8
nursery	9	12,960	1,024	1	4.1	1.8	7.1	0.9	121.2	118.9	46.8
breast-cancer	11	699	20	46	2.3	0.6	2.2	0.8	1.1	1.1	0.5
bridges	13	108	6	142	2.2	0.6	4.2	0.9	0.5	0.6	0.2
echocardiogram	13	132	6	538	1.6	0.4	69.9	1.2	0.5	0.5	0.2
adult	14	48,842	3,528	78	67.4	111.6	531.5	5.9	6039.2	6033.8	860.2
letter	17	20,000	695	61	260.0	529.0	7204.8	6.0	1090.0	1015.5	291.3
ncvoter	19	1,000	151	758	4.3	4.0	ML	5.1	11.4	1.9	1.1
hepatitis	20	155	8	8,250	12.2	175.9	ML	326.7	5576.5	9.5	0.8
horse	27	368	25	128,726	457.0	TL	ML	TL	TL	385.8	7.2
fd-reduced-30	30	250,000	69,581	89,571	41.1	77.7	ML	TL	377.2	382.4	TL
plista	63	1,000	568	178,152	ML	ML	ML	TL	TL	TL	26.9
flight	109	1,000	575	982,631	ML	ML	ML	TL	TL	TL	216.5
uniprot	223	1,000	2,439	unknown	ML	ML	ML	TL	TL	TL	ML

TL: time limit of 4 hours exceeded

ML: memory limit of 100GB exceeded

1. There are **many FDs** to discover!

2. Algorithms are either **row or column efficient!**

3. No algorithm can handle datasets of **real-world size!**

## FD Algorithm Classes



## Experimental Evaluation



## Extrapolation of Results

Boeing 747-451



Boeing 767-432(ER)



Boeing 757-351



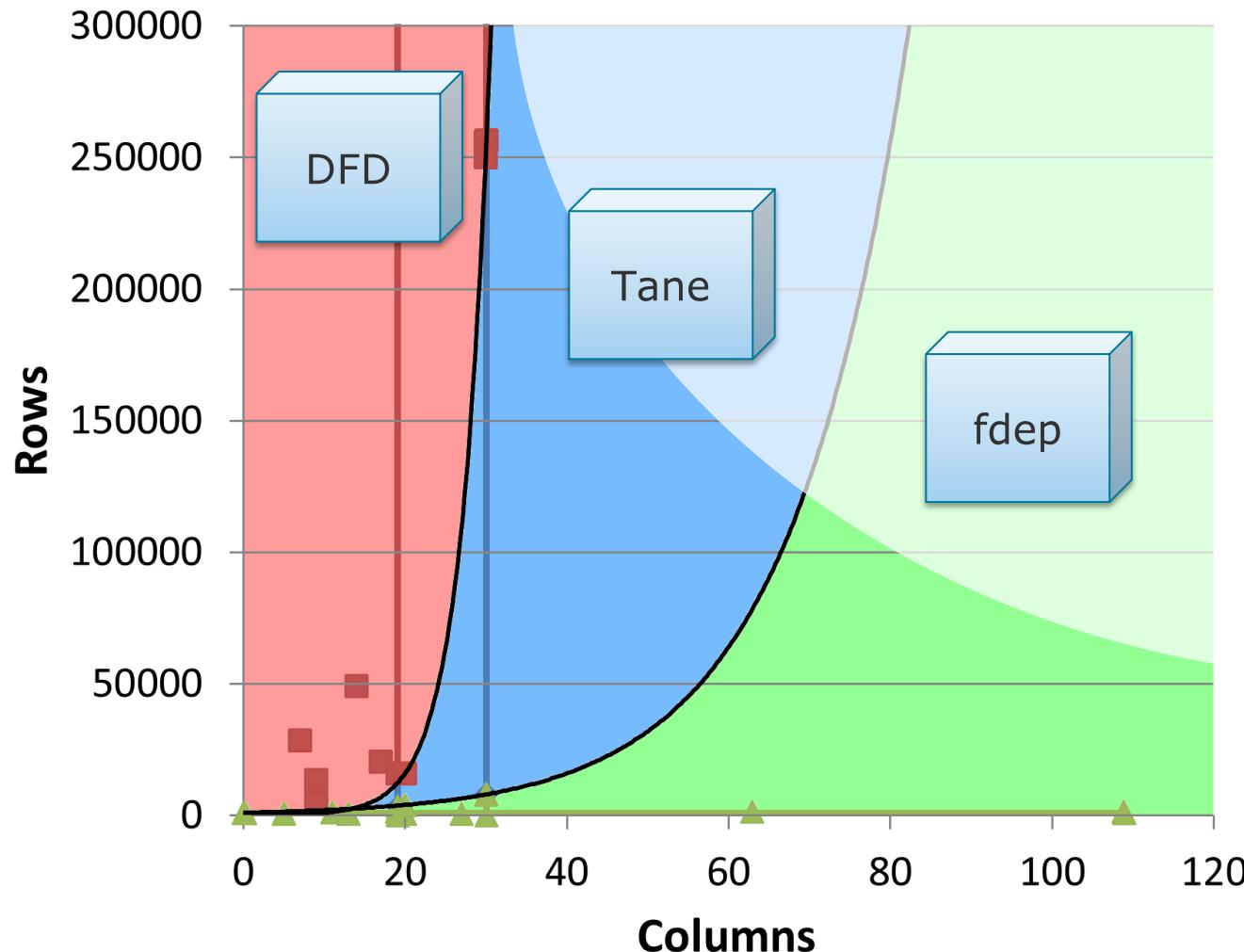
Boeing 737-832



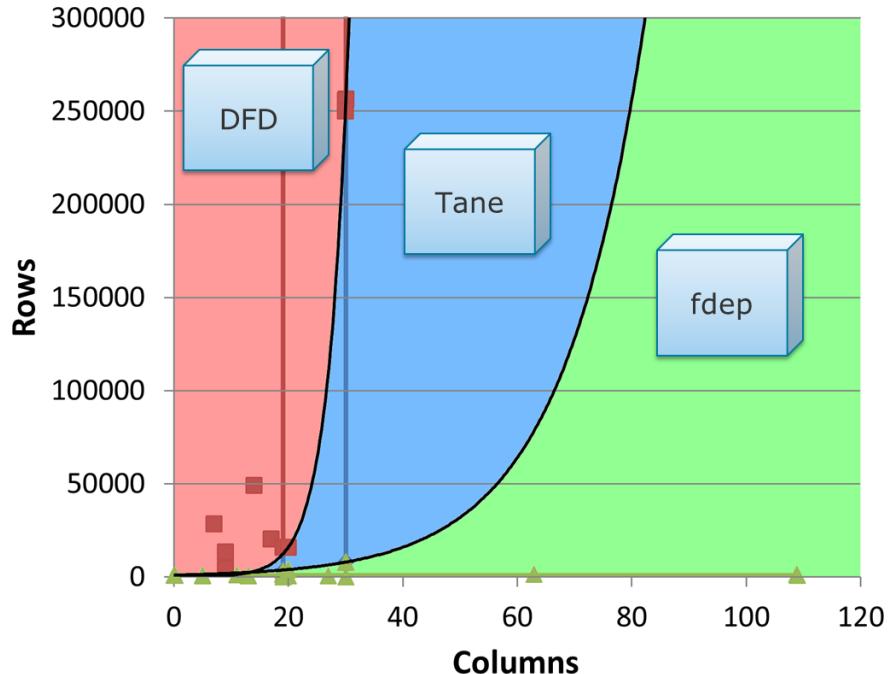
Boeing 737-732



## Extrapolation of Results Decision Chart



TANE [7]	FUN [15]	FD_MINE [21]	DFD [1]	DEP-MINER [12]	FASTFDs [20]	FDEP [6]
1.1	<b>0.1</b>	0.2	0.2	0.2	0.2	<b>0.1</b>
1.2	<b>0.1</b>	0.2	0.3	0.3	0.3	0.2
2.9	1.1	3.8	<b>1.0</b>	174.6	164.2	125.5
2.1	<b>0.6</b>	1.8	1.1	3.0	2.9	3.8
4.1	1.8	7.1	<b>0.9</b>	121.2	118.9	46.8
2.3	0.6	2.2	0.8	1.1	1.1	<b>0.5</b>
2.2	0.6	4.2	0.9	0.5	0.6	<b>0.2</b>
1.6	0.4	69.9	1.2	0.5	0.5	<b>0.2</b>
67.4	111.6	531.5	<b>5.9</b>	6039.2	6033.8	860.2
260.0	529.0	7204.8	<b>6.0</b>	1090.0	1015.5	291.3
4.3	4.0	ML	5.1	11.4	1.9	<b>1.1</b>
12.2	175.9	ML	326.7	5576.5	9.5	<b>0.8</b>
457.0	TL	ML	TL	TL	385.8	<b>7.2</b>
<b>41.1</b>	77.7	ML	TL	377.2	382.4	TL
ML	ML	ML	TL	TL	TL	<b>26.9</b>
ML	ML	ML	TL	TL	TL	<b>216.5</b>
ML	ML	ML	TL	TL	TL	ML



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