



**Hasso
Plattner
Institut**

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Towards Verifying Cyber-Physical Systems with Structural Dynamism

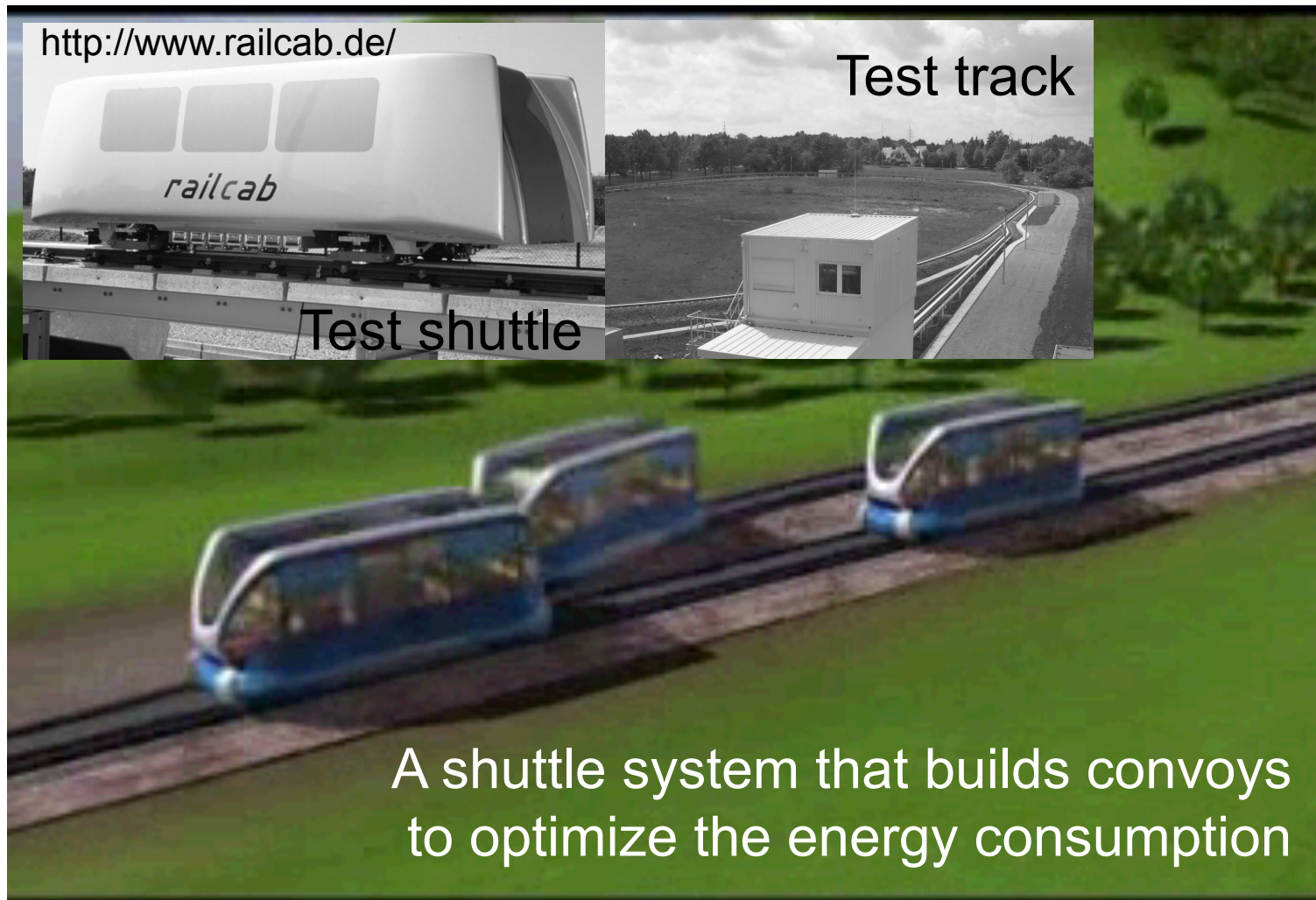
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Holger Giese and Basil Becker
System Analysis & Modeling Group, Hasso Plattner
Institute for Software Systems Engineering at the
University of Potsdam, Germany

holger.giese@hpi.uni-potsdam.de

Application Example: Combine shuttles as a CPS ...

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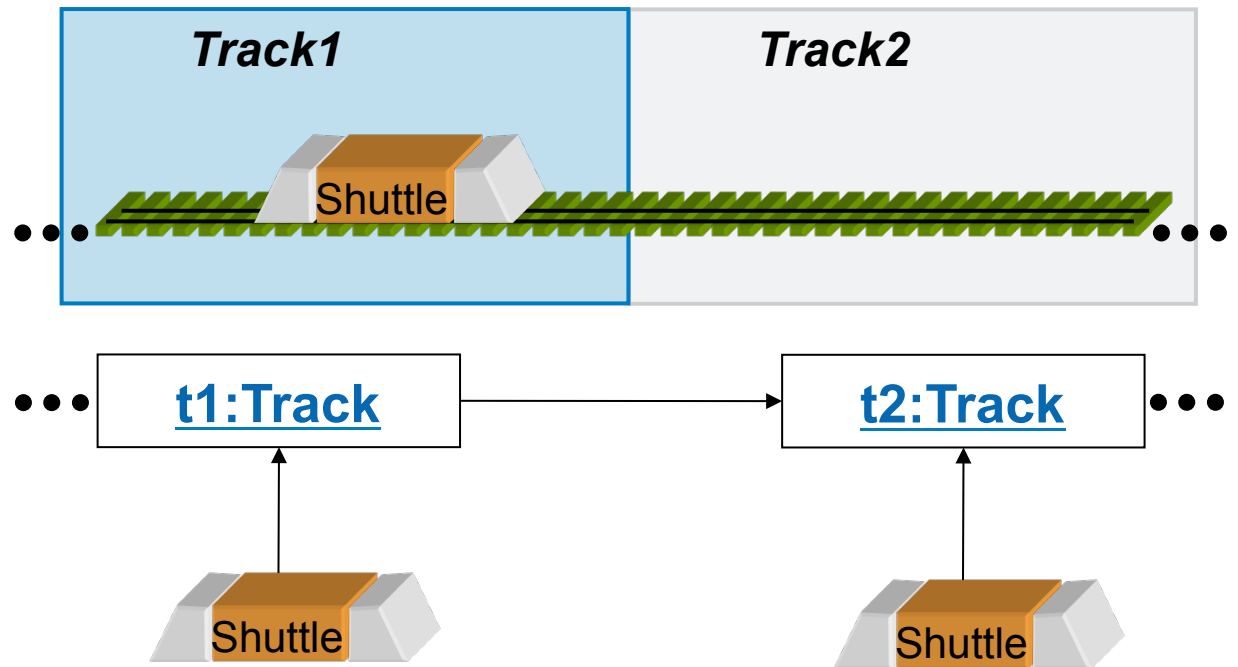


1) Modeling with Graph Transformation Systems

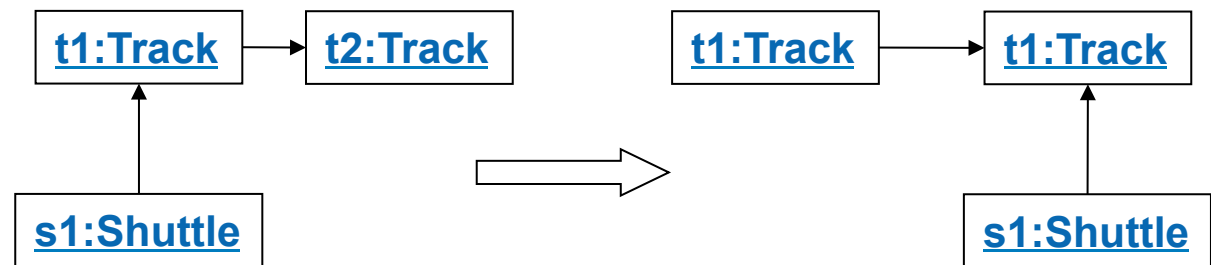
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Apply Graph Transformation Systems

- Map the tracks
- Map the shuttles
- Map the shuttle movement to rules (movement equals reconfiguration)



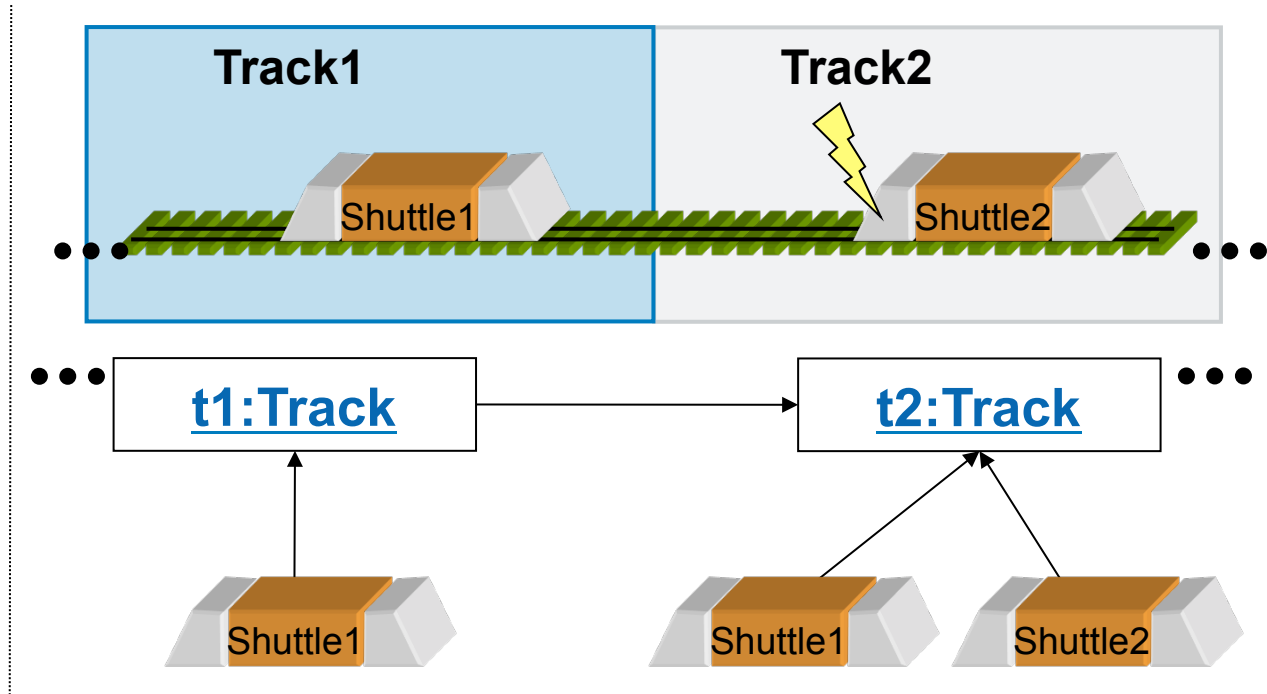
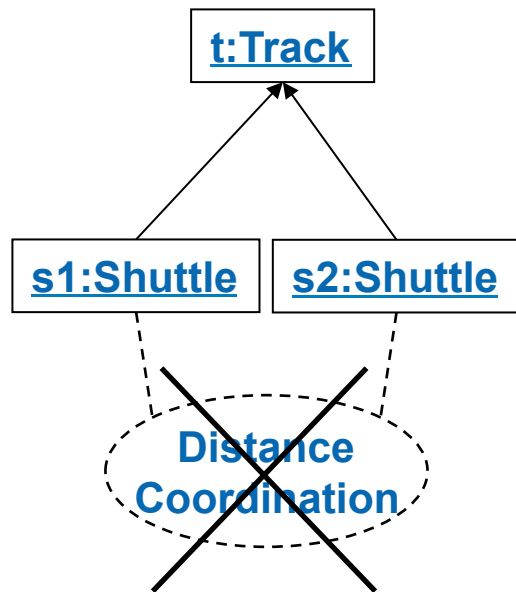
Rule:



2) Modeling with Graph Transformation Systems

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Forbidden Graph



- **Correctness:** all reachable system graphs do not match the forbidden graph pattern

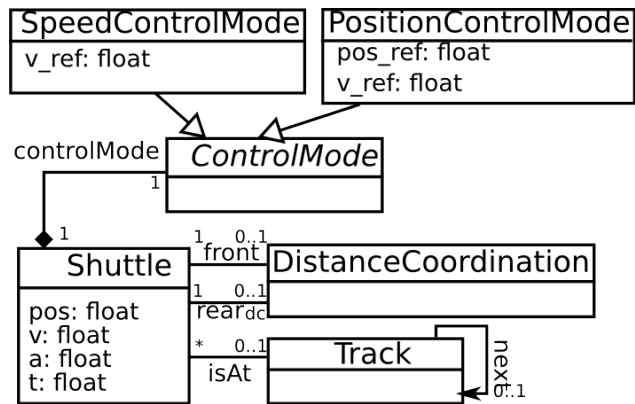
Idea for hybrid behavior: continuous attributes and modes with continuous laws

- **Correctness:** all reachable hybrid system graphs do not match the forbidden hybrid graph pattern

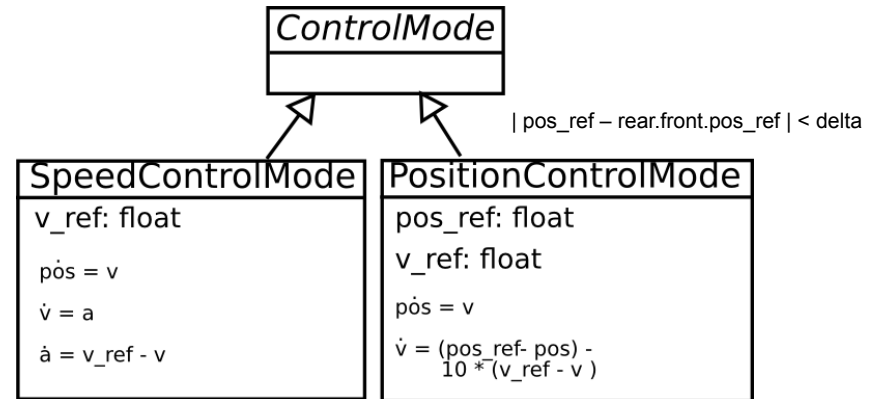
Modeling the Railcab System

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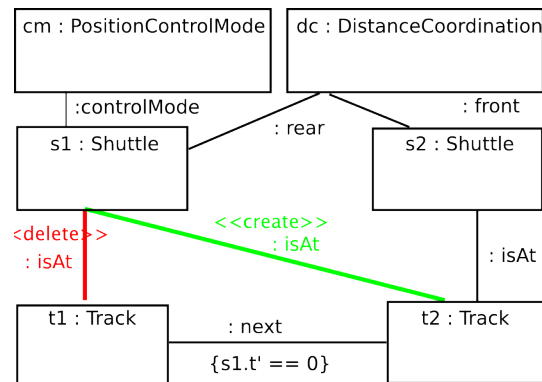
Meta Model:



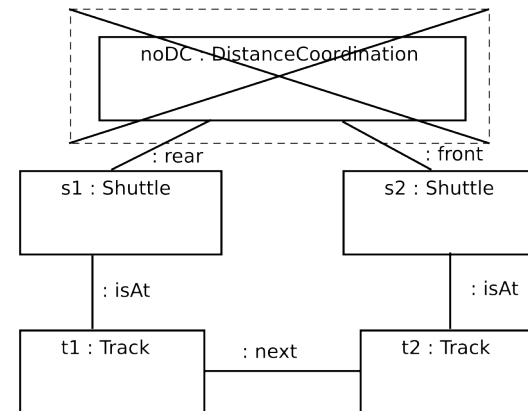
Continuous Behavior:



Discrete Behavior (Rule):

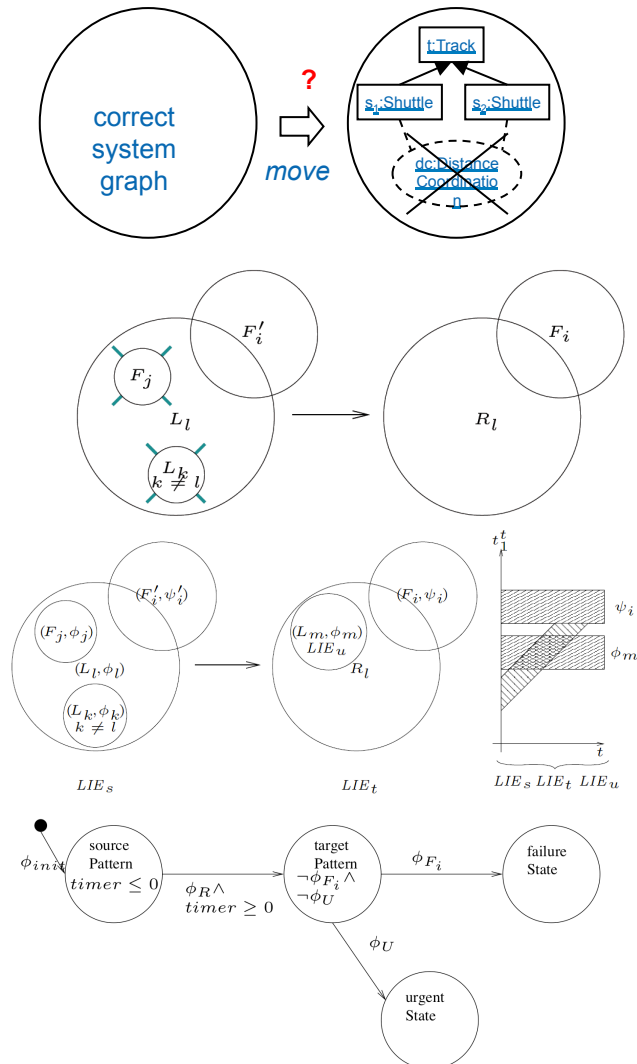


Forbidden Situation (Graph Pattern):



Basic Verification Idea

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Idea (invariant checking):

- Look only for a transition from a safe to an unsafe state
- Found a case leading from a safe to a forbidden graph pattern

Timed:

- Found a case leading from a safe to a forbidden graph pattern also fulfilling the time constraints that is not prevented by other rules (system of linear inequality; CPLEX solver)

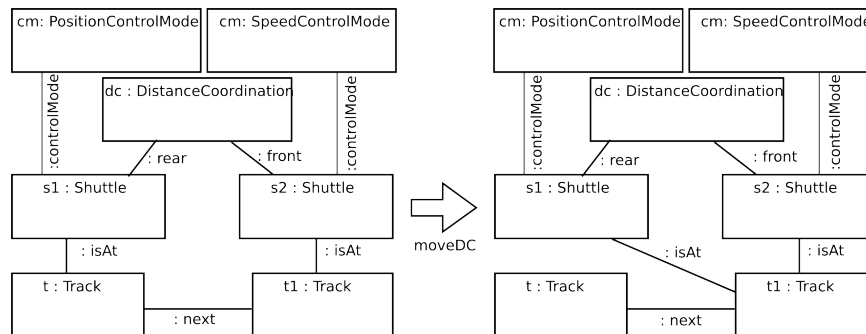
Hybrid:

- Construct hybrid automata for the check (PHAVer)

Verification of the Application Example

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- Structural Check returns possible counterexamples (not taking the continuous behavior and constraints into account)
- Modelchecking a related hybrid automata disproof or conforms each counterexample



```

automaton GenericHybridGTS
  contr_var: s1_pos, s2_pos, s1_v, s2_v, s1_a, s2_a,
            v_ref, pos_ref, timer;
  parameter: distance, failure;
  synclabs: void;
  loc sourcePattern: while t<=0 wait {timer' == 1};
  when timer >= 0 sync void do {pos_ref' ==
    s1_pos - distance - 2 & s1_pos' ==
    s1_pos & s2_pos' == s2_pos & s2_v' ==
    s2_v & s1_v' == s1_v & s1_a' == s1_a &
    s2_a' == s2_a & v_ref' == v_ref &
    failure' == 0} goto targetPattern;
  loc targetPattern: while s1_pos - distance -
    s2_pos >= 0 wait {s1_pos' == s1_v & s1_v'
    == s1_a & s1_a' == P + (v_ref - s1_v) &
    s2_v' == P-2 * (s1_pos - distance - 10 -
    s2_pos) - Q-2 * (s2_v - 3 - s1_v) &
    pos_ref' == s1_pos' & v_ref' == 0};
  when s1_pos - distance - s2_pos <= 0 sync
  void do {failure' == 1} goto
  failureState;
  loc failureState: while true wait {true};
  loc urgentTransition: while true wait {true};
  initially: sourcePattern & s1_pos > s2_pos +
    distance + 10 & s2_pos > 0 & 60 < v_ref &
    v_ref < 200 & 60 < s1_v & s1_v < 200 & 3
    <= s1_v - s2_v & s1_v - s2_v <= 3 &
    failure == 0 & 5 < distance & distance <
    10;
end
    
```

Summary

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- Very *expressive* model in form of hybrid graph transformation model containing
 - **Discrete behavior** with structural dynamism (which potentially leads to a discrete infinite states spaces in form of graphs)
 - **Continuous behavior** in form of mode nodes and their continuous laws that can in principle reference all continuous variables of reachable other nodes
- Invariant checker for restricted variant where for all counter-examples a closed continuous system of inequalities can be derived.
- Tool support is still under development ...