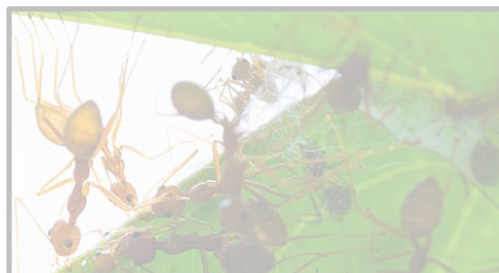




# Agenda

Unicode	Glyph	Symbol	Name	Diameter	Mass	Moons	Rings
U+2609	☉	Sun	Mercury	0.382	0.06	0	no
U+263D	☾	Moon	Venus	0.949	0.82	0	no
U+263E	☾	Moon	Earth	1.000	1.00	1	no
U+263F	☿	Mercury	Mars	0.532	0.11	2	no
U+2640	♀	Venus	Jupiter	11.209	317.8	67	yes
U+1F728	♁	Earth	Saturn	9.449	95.2	62	yes
U+2642	♂	Mars	Uranus	4.007	14.6	27	yes
U+2643	♃	Jupiter	Neptune	3.883	17.2	14	yes
U+2644	♄	Saturn					
U+2645	♅	Uranus					
U+26E2	♆	Uranus					
U+2646	♇	Neptune					
≈ U+2641	♁	Eris					
≈ U+29EC	♁	Eris					
U+2647	♇	Pluto					
not present	--	Pluto					



Sign	House	Domicile	Detriment	Exaltation
Aries	1st House	Mars	Venus	Sun
Taurus	2nd House	Venus	Pluto	Moon
Gemini	3rd House	Mercury	Jupiter	N/A
Cancer	4th House	Moon	Saturn	Jupiter
Leo	5th House	Sun	Uranus	Neptune
Virgo	6th House	Mercury	Neptune	Pluto, Mercury
Libra	7th House	Venus	Mars	Saturn
Scorpio	8th House	Pluto	Venus	Uranus
Capricorn	9th House	Jupiter	Mercury	N/A
	10th House	Saturn	Moon	Mars



Name	Mass	Orbital radius	Rotation period	Atmosphere
Mercury	0.06	0.47	58.64	minimal
Venus	0.82	0.72	-243.02	CO <sub>2</sub> , N <sub>2</sub>
Earth	1.00	1.00	1.00	N <sub>2</sub> , O <sub>2</sub> , Ar
Mars	0.11	1.52	1.03	CO <sub>2</sub> , N <sub>2</sub> , Ar
Jupiter	317.8	5.20	0.41	H <sub>2</sub> , He
Saturn	95.2	9.54	0.43	H <sub>2</sub> , He
Uranus	14.6	19.22	-0.72	H <sub>2</sub> , He
Neptune	17.2	30.06	0.67	H <sub>2</sub> , He

**BINDER**  
divide & conquer  
based IND detection

**SINDY**  
scaling out  
IND detection

**High arity**  
techniques to deal  
with high-arity INDs

**Advanced IND  
detection methods**

Sebastian Kruse,  
26th June, 2017

Chart 2

# Unary IND complexity (Repetition)

- Unary IND discovery has a complexity of  $O(n^2)$  (n: number of attributes)
  - Databases often comprise thousands of columns  
→ millions of IND candidates to be checked
- Checking an IND candidate requires “aligning” the values of the involved columns
  - Databases often comprise millions or billions of tuples  
→ huge amounts of data need to be re-organized
- Call for efficient, robust, and scalable IND discovery strategies.

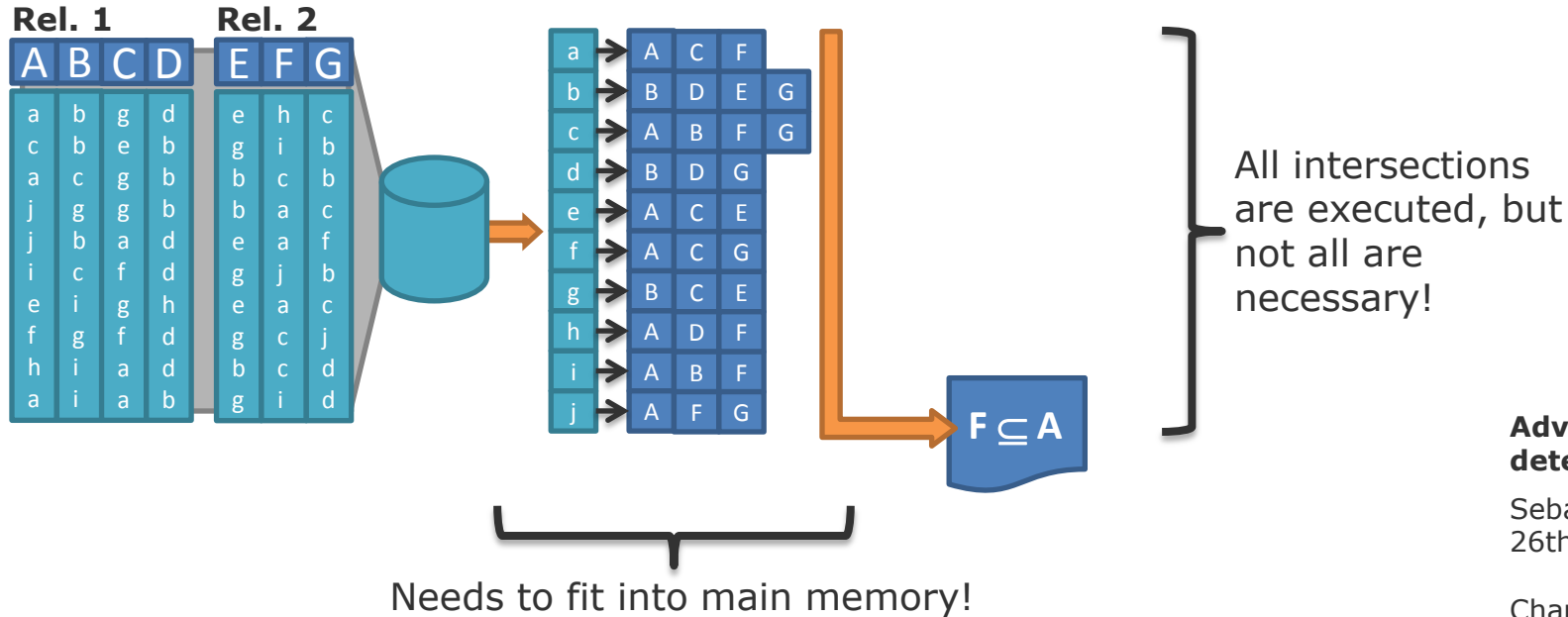
**Advanced IND  
detection methods**

Sebastian Kruse,  
26th June, 2017

Chart 3

# DeMarchi's algorithm (Repetition)

  attributes      values  
➔ dataflow    X ignored



**Advanced IND detection methods**

Sebastian Kruse,  
26th June, 2017

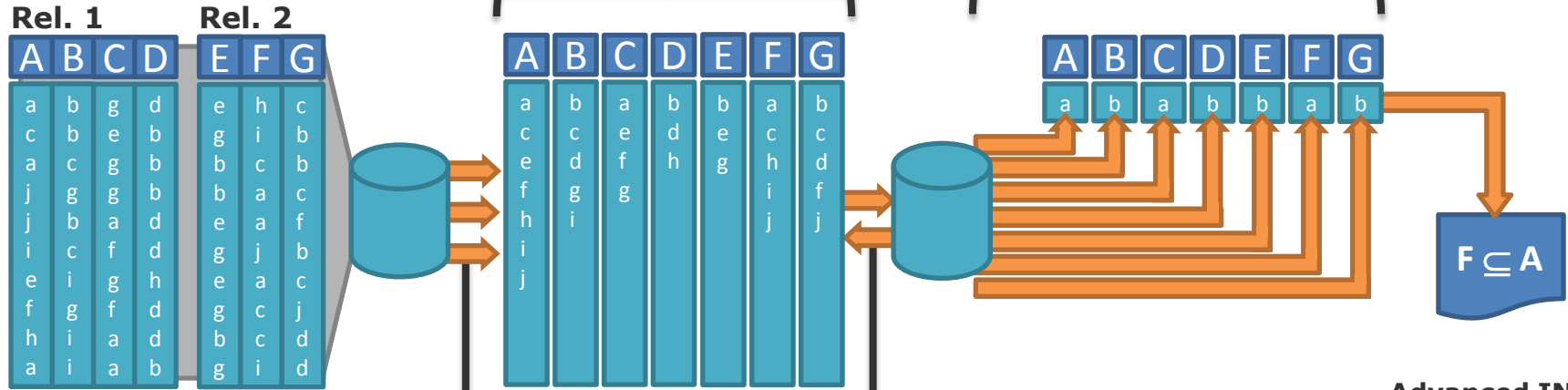
Chart 4

# SPIDER algorithm (Repetition)

■ attributes    ■ values  
➔ dataflow    ■ ignored

Needs to fully sort  
all attributes!

OS limit on open  
files / sockets!



Attributes are accessed  
individually!

Two Phase Multiway Merge Sort  
needed for larger datasets!

**Advanced IND  
detection methods**

Sebastian Kruse,  
26th June, 2017

Chart 5

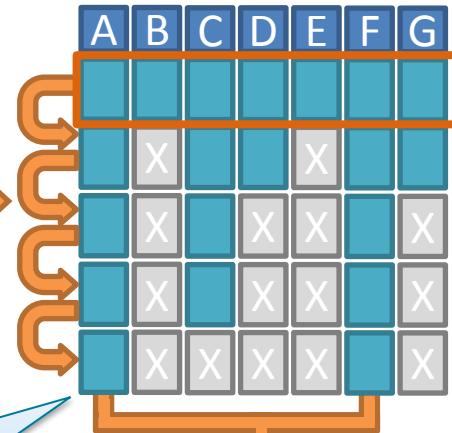
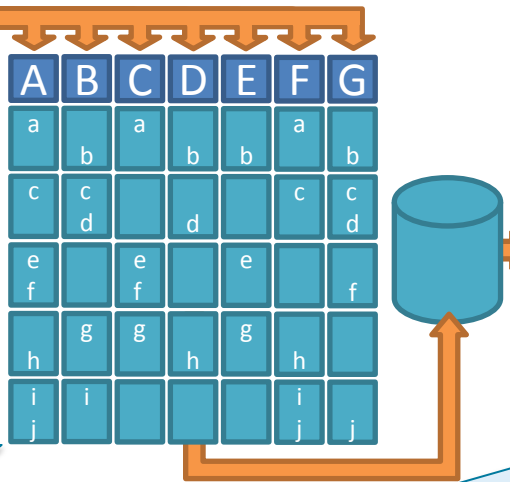
# BINDER algorithm – workflow (unary)

■ attributes    ■ values  
➔ dataflow    X ignored

**Divide**

**Conquer**

Rel. 1				Rel. 2		
A	B	C	D	E	F	G
a	b	g	d	e	h	c
c	b	e	b	g	i	b
a	c	g	b	b	c	b
j	g	g	b	b	a	c
j	b	a	d	e	a	f
i	c	f	d	g	j	b
e	g	i	h	e	a	c
f	g	f	d	g	c	j
h	i	a	d	g	b	c
a	i	a	b	g	i	d



**validation?**

**Dynamic Memory Handling:**  
Spill largest buckets to disk if memory is exhausted.

**Lazy Partition Refinement:**  
Split a partition if it does not fit into main memory.

**Advanced IND detection methods**  
Sebastian Kruse,  
26th June, 2017

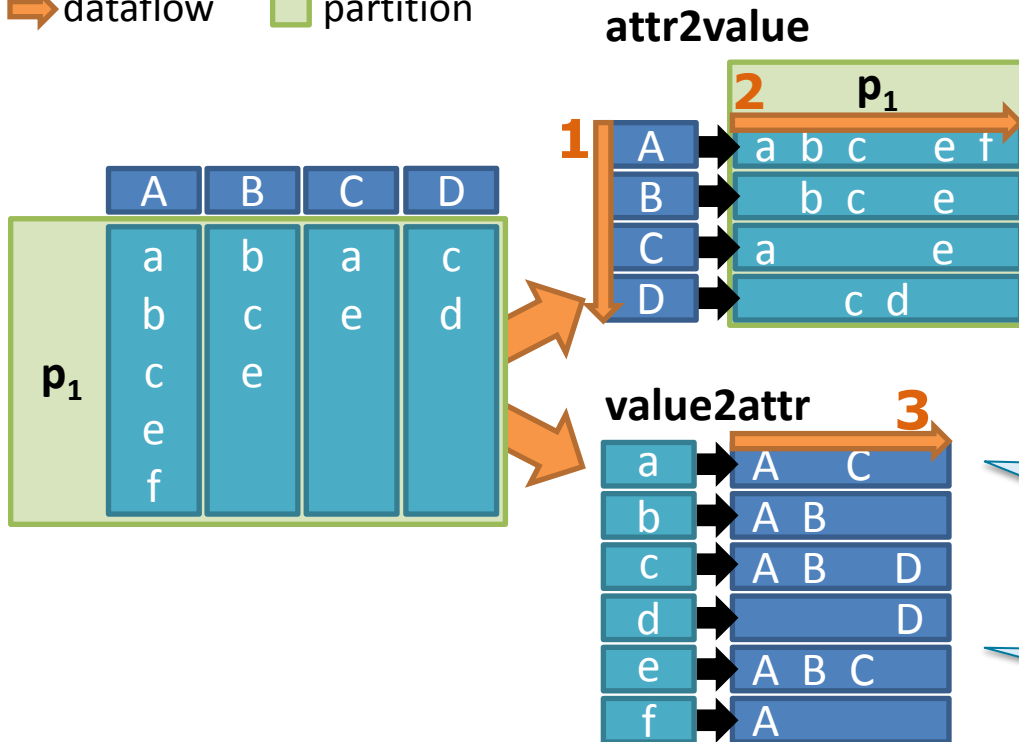
Chart 6

$$size(bucket) = \sum_{string \in bucket} 8 + 8 \cdot \left\lceil \frac{64 + 2 \cdot |string|}{8} \right\rceil$$

# BINDER – divide & conquer based IND detection

## BINDER algorithm – validation

■ attributes    ■ values  
➔ dataflow    ■ partition



1. Iterate attributes
2. Iterate values
3. If value2attr entry exists
  - Intersect candidates with this list
  - Remove value2attr entry
  - If attribute removed from all candidates
  - Remove entry from attr2value

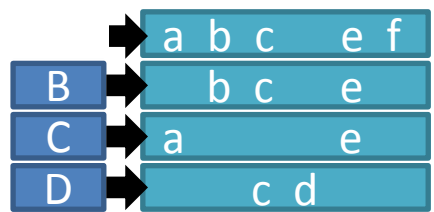
**Both indexes fit into main memory due to the partitioning!**

**see DeMarchi's algorithm**

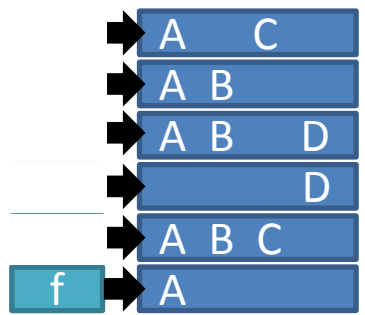
**Advanced IND detection methods**  
 Sebastian Kruse,  
 26th June, 2017

# BINDER algorithm – validation example

attr2value



value2attr

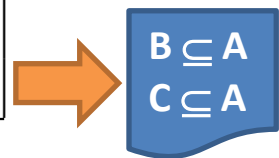


Never tested! →



1. Iterate attributes
2. Iterate values
3. If value2attr entry exists
  - Intersect candidates with this list
  - Remove value2attr entry
  - If attribute removed from all candidates
  - Remove entry from attr2value

	A	B	C	D
look up	B,C,D	A,C,D	A,B,D	A,B,C



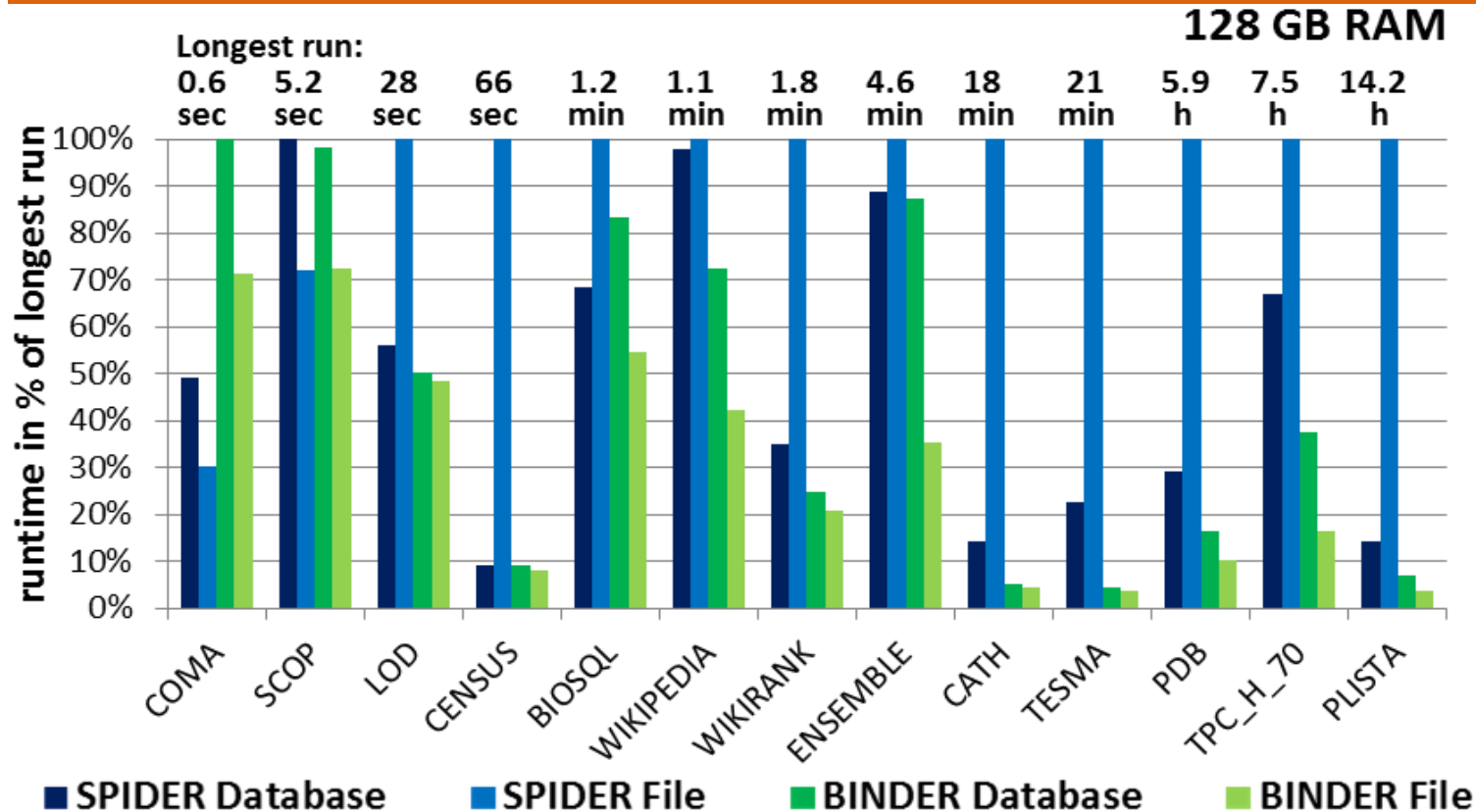
**Advanced IND detection methods**

Sebastian Kruse,  
26th June, 2017

Chart 8



# BINDER evaluation



**Advanced IND detection methods**

Sebastian Kruse,  
26th June, 2017

Chart 9

# N-ary IND detection complexity

No n-ary INDs here! Why?

$$X \subseteq Y: \\ X \cap Y = \emptyset$$

## IND Candidates in level k:

$$\binom{n}{k} * \binom{n-k}{k} * k!$$

nodes

all permutations

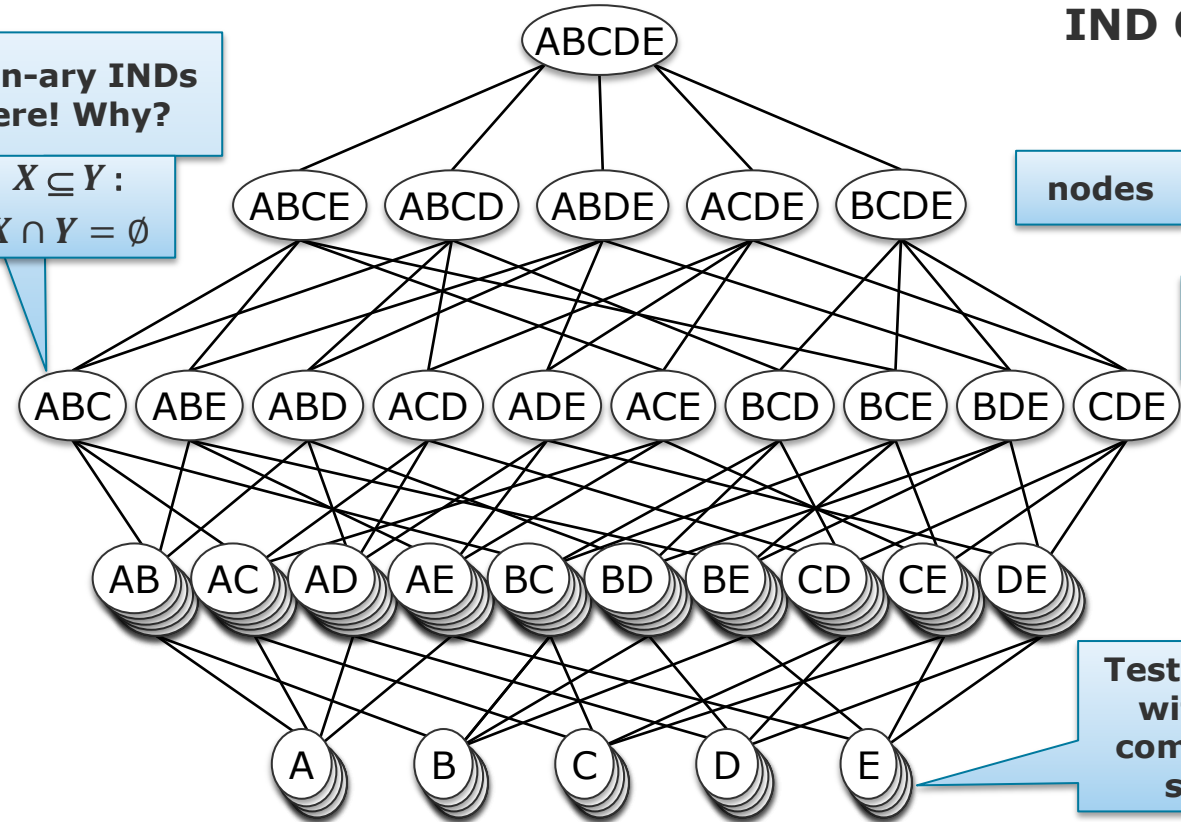
other, non-overlapping nodes

Test combination with all other combinations of same size!

### Advanced IND detection methods

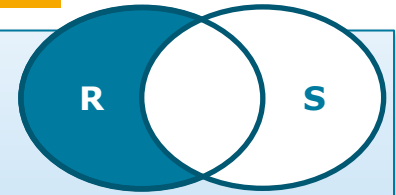
Sebastian Kruse, 26th June, 2017

Chart 10



# BINDER – divide & conquer based IND detection

## MIND (Recap)



**Validate**  $A, B \subseteq C, D$ :

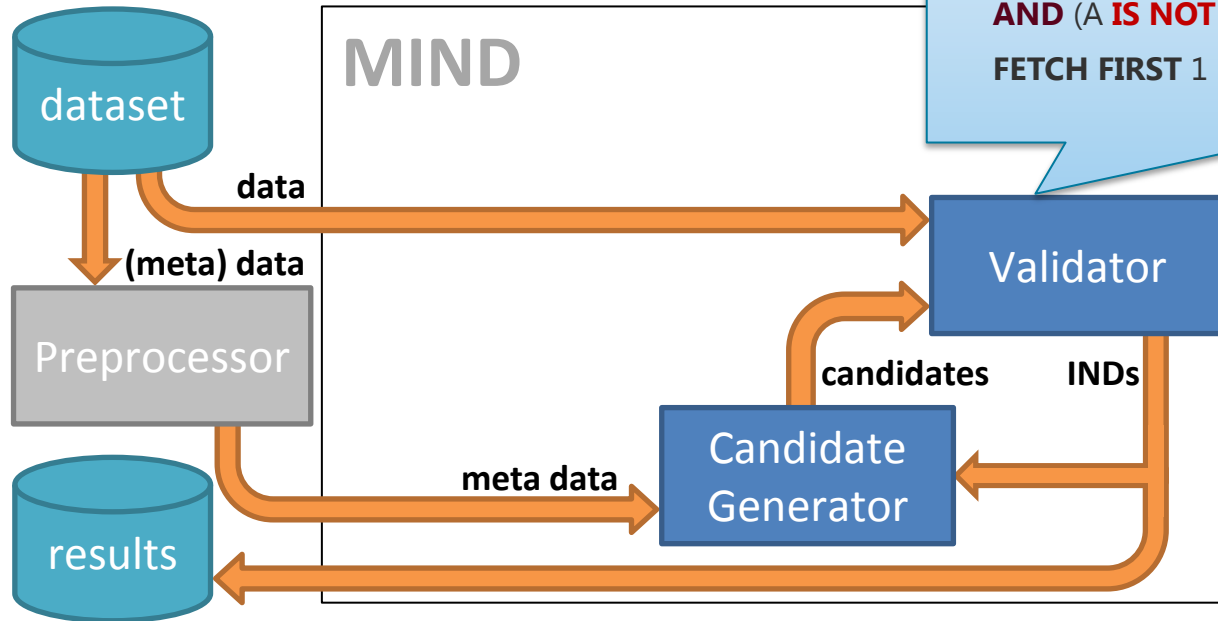
**SELECT** R.A, R.B, S.C, S.D

**FROM** R **LEFT OUTER JOIN** S **ON** A = C **AND** B = D

**WHERE** (C **IS NULL** **AND** D **IS NULL**)

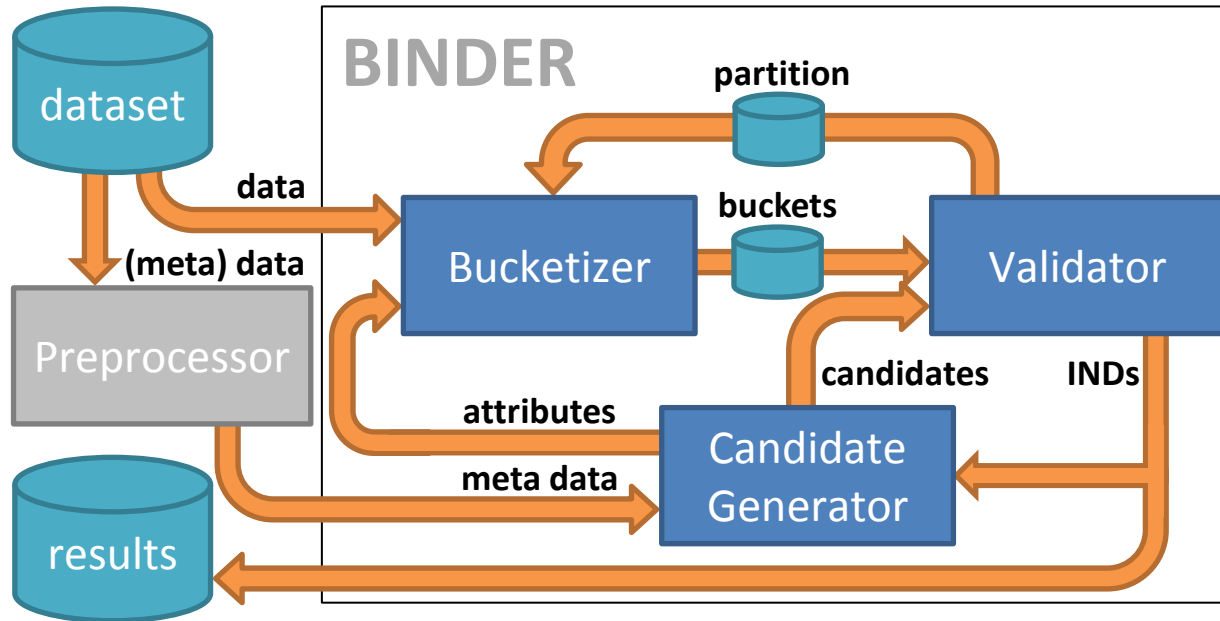
**AND** (A **IS NOT NULL** **OR** B **IS NOT NULL**)

**FETCH FIRST 1 ROWS ONLY;**



```
SELECT fromTable.AAGE, fromTable.ACLSWKR,
fromTable.ADTIND, fromTable.ADTOCC,
fromTable.AGI, fromTable.AHGA
FROM CENSUS6 fromTable LEFT OUTER JOIN
CENSUS exceptTable ON
fromTable.AAGE = exceptTable.AAGE AND
fromTable.ACLSWKR = exceptTable.ACLSWKR
AND
fromTable.ADTIND = exceptTable.ADTIND AND
fromTable.ADTOCC = exceptTable.ADTOCC AND
fromTable.AGI = exceptTable.AGI AND
fromTable.AHGA = exceptTable.AHGA
WHERE exceptTable.AAGE IS NULL AND
exceptTable.ACLSWKR IS NULL AND
exceptTable.ADTIND IS NULL AND
exceptTable.ADTOCC IS NULL AND
exceptTable.AGI IS NULL AND
exceptTable.AHGA IS NULL
AND (fromTable.AAGE IS NOT NULL OR
fromTable.ACLSWKR IS NOT NULL OR
fromTable.ADTIND IS NOT NULL OR
fromTable.ADTOCC IS NOT NULL OR
fromTable.AGI IS NOT NULL OR
fromTable.AHGA IS NOT NULL)
FETCH FIRST 1 ROWS ONLY;
```

# N-ary BINDER – workflow



**Advanced IND  
detection methods**

Sebastian Kruse,  
26th June, 2017

Chart **12**

# N-ary BINDER – candidate generation

## ■ Apriori algorithm:

- Bottom-up lattice traversal strategy
- Authors: R.Agrawal and R. Srikant
- Publication: Fast algorithms for mining association rules in large databases
- Input: all frequent item sets of size  $n$
- Output: all candidate frequent item sets of size  $n+1$

## ■ Adaption for n-ary IND detection:

- Let  $R_i$  be the  $i$ -th relation in the relational schemata  $R$ . For each valid IND  $R_j[X] \subseteq R_k[Y]$  with  $|X|=|Y|=n$  generate all IND candidates  $R_j[XA] \subseteq R_k[YB]$  so that:

1.  $R_j[X] \subseteq R_k[Y]$  and  $R_j[A] \subseteq R_k[B]$  (both are valid INDs)
2.  $\forall X_i \in X: X_i < A$  (INDs are permutable; do not generate them twice)
3.  $A \notin XY, B \notin XY$  and  $R_j[A] \neq \{\}$  (do not generate degenerate candidates)

**Advanced IND  
detection methods**

Sebastian Kruse,  
26th June, 2017

Chart 13

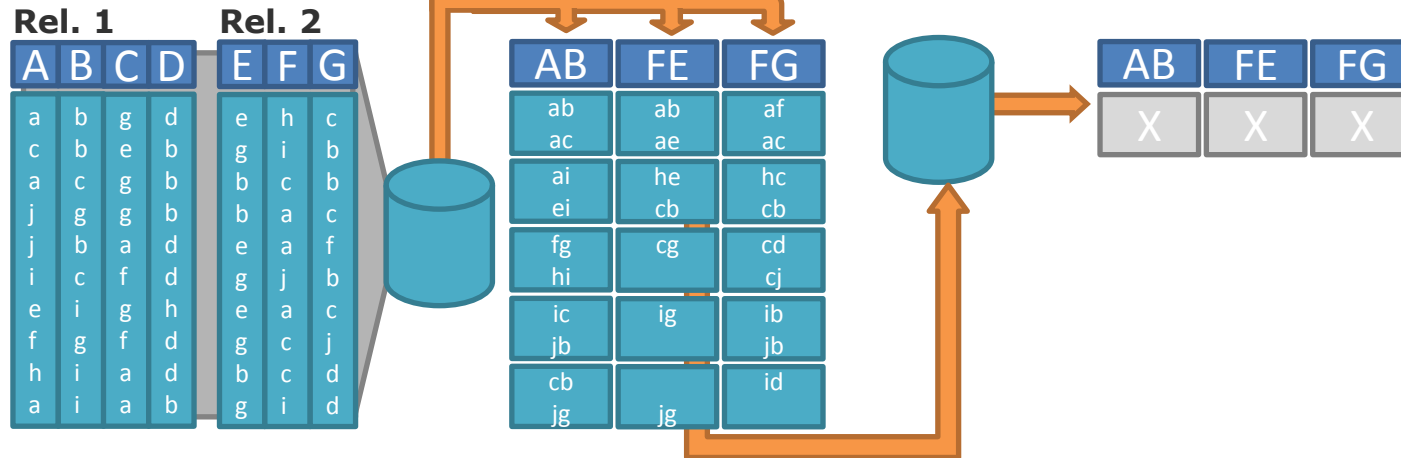
# BINDER algorithm – workflow (n-ary)

Assume that we need to check  $AB \subseteq FE$  and  $AB \subseteq FG$ .

- attribute (combinations)
- value (combinations)
- X ignored
- dataflow

## Divide

## Conquer

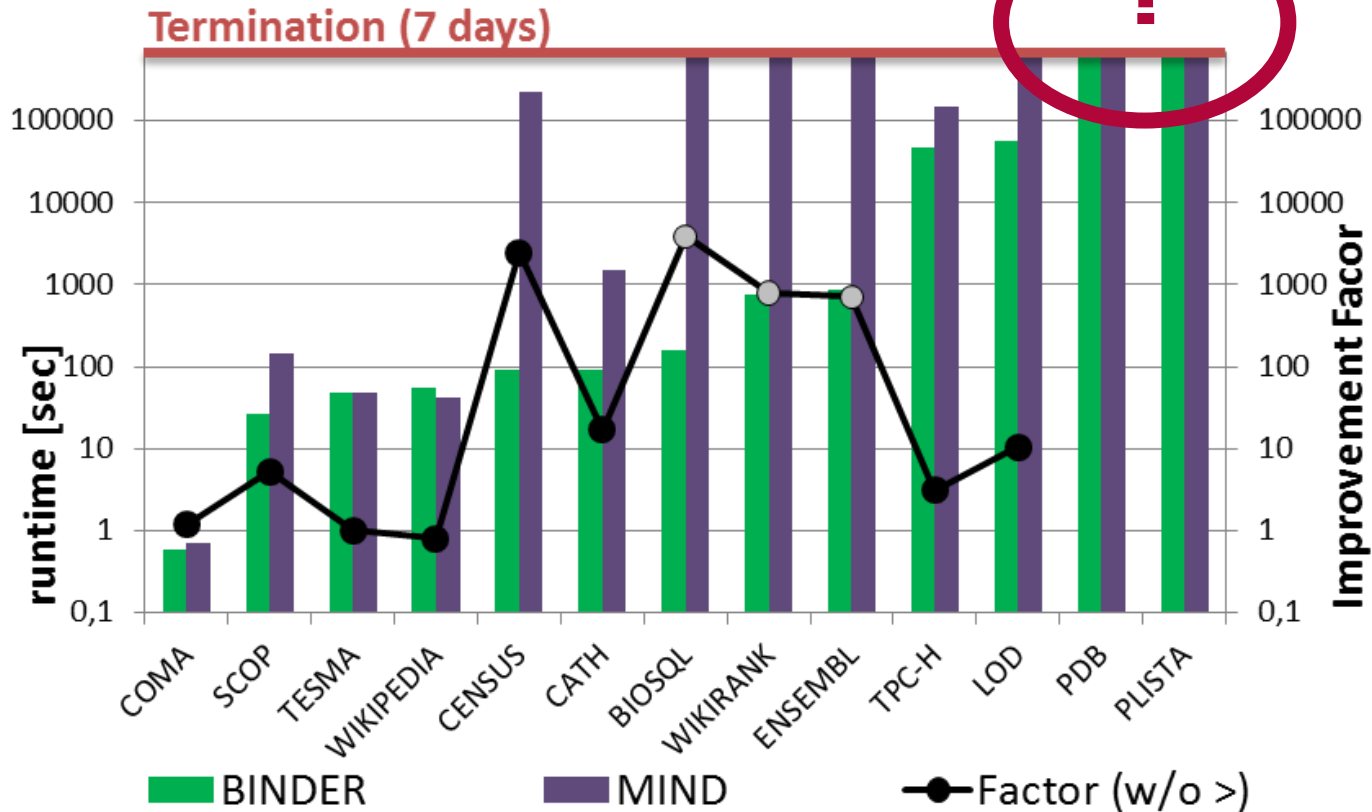


**Advanced IND detection methods**

Sebastian Kruse,  
26th June, 2017

# BINDER – divide & conquer based IND detection

## N-ary BINDER evaluation

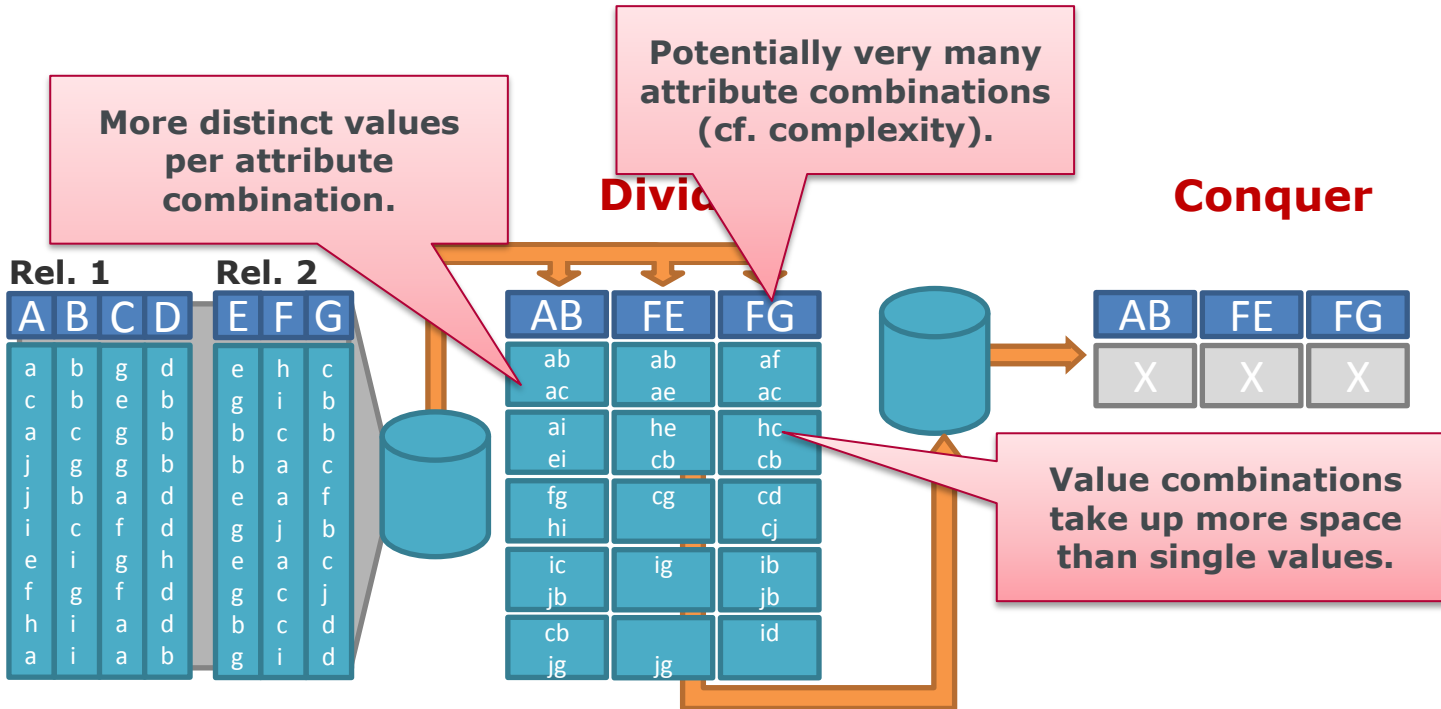


Advanced IND detection methods

Sebastian Kruse,  
26th June, 2017

Chart 15

# N-ary BINDER evaluation



**Advanced IND detection methods**

Sebastian Kruse,  
26th June, 2017



# Agenda

Unicode	Glyph	Symbol	Name	Diameter	Mass	Moons	Rings										
U+2609	☉	Sun	Mercury	0.382	0.06	0	no										
U+263D	☾	Moon	Venus	0.949	0.82	0	no										
U+263E	☿	Mercury	Earth	1.000	1.00	1	no										
U+263F	♁	Mercury	Mars	0.532	0.11	2	no										
U+2640	♀	Venus	Jupiter	11.209	317.8	67	yes										
U+1F728	♁	Earth	Saturn	9.449	95.2	62	yes										
U+2642	♂	Mars	Uranus	4.007	14.6	27	yes										
U+2643	♃	Jupiter	Neptune	U+2641	♅	Eris	U+29EC	♁	Eris	U+2647	♇	Pluto	not present	--	Pluto	...	...



Sign	House	Domicile	Detriment	Exaltation
Aries	1st House	Mars	Venus	Sun
Taurus	2nd House	Venus	Pluto	Moon
Gemini	3rd House	Mercury	Jupiter	N/A
Cancer	4th House	Moon	Saturn	Jupiter
Leo	5th House	Sun	Uranus	Neptune
Virgo	6th House	Mercury	Neptune	Pluto, Mercury
Libra	7th House	Venus	Mars	Saturn
Scorpio	8th House	Pluto	Venus	Uranus
Capricorn	10th House	Saturn	Moon	Mars



Name	Mass	Orbital radius	Rotation period	Atmosphere
Mercury	0.06	0.47	58.64	minimal
Venus	0.82	0.72	-243.02	CO <sub>2</sub> , N <sub>2</sub>
Earth	1.00	1.00	1.00	N <sub>2</sub> , O <sub>2</sub> , Ar
Mars	0.11	1.52	1.03	CO <sub>2</sub> , N <sub>2</sub> , Ar
Jupiter	317.8	5.20	0.41	H <sub>2</sub> , He
Saturn	95.2	9.54	0.43	H <sub>2</sub> , He
Uranus	14.6	19.22	-0.72	H <sub>2</sub> , He
Neptune	17.2	30.06	0.67	H <sub>2</sub> , He

**BINDER**  
divide & conquer  
based IND detection

**SINDY**  
scaling out  
IND detection

**High arity**  
techniques to deal  
with high-arity INDs

**Advanced IND  
detection methods**

Sebastian Kruse,  
26th June, 2017

Chart **17**

# The hardware side

- Some problems are intrinsically hard
  - “defeat it with iron”: use more/better hardware for the computation
  
- **Scalability != efficiency**
  - Efficient = fast / spare resources
  - Scalable = improvement by leveraging more resources

“Do the **same** work in **less** time.” ≠ “Do **more** work in the **same** time.”

**Advanced IND  
detection methods**

Sebastian Kruse,  
26th June, 2017

Chart **18**

# Scaling dimensions

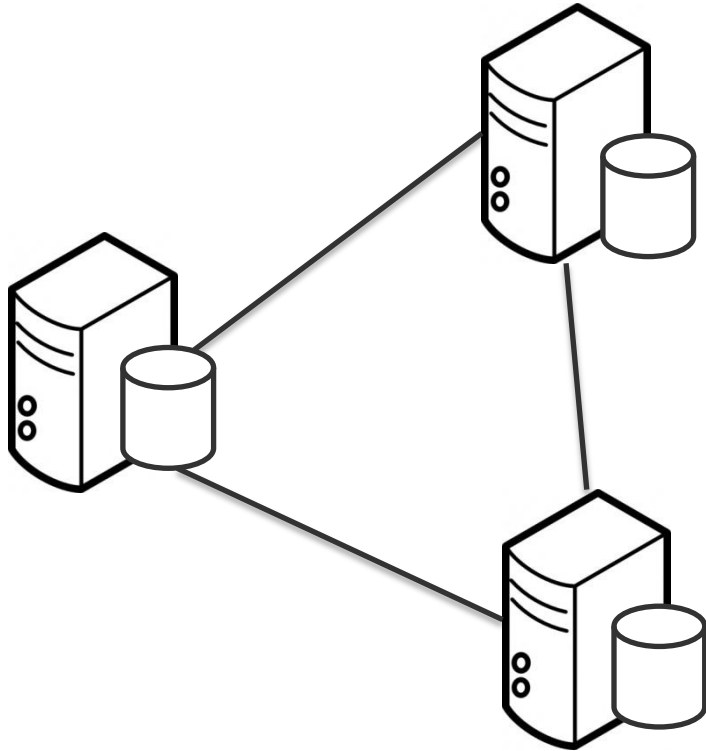
- **Scale up:** faster CPUs/disk, more main memory, ...
  - lowest impact on code
  - expensive, limited, shift of bottlenecks
- **Scale in:** more cores, (RAID)
  - thread-level parallelization, cache coherency
  - limited, shift of bottlenecks
- **Scale out:** computer clusters
  - Actors, message passing, data partition
  - Less limited, most complicated
  
- Is **problem suited** to certain scaling direction?

**Advanced IND  
detection methods**

Sebastian Kruse,  
26th June, 2017

Chart **19**

# Scale out: Setting



- Multiple **independent** nodes
- can **communicate** and exchange data
- oftentimes **data distributed** among nodes
- **no** shared state
- **network** new potential bottleneck
  - network topology relevant
- **fault tolerance** important
- **load balancing** important

## Advanced IND detection methods

Sebastian Kruse,  
26th June, 2017

# Distributed Application Frameworks



*NB: overview not complete!*

**Advanced IND detection methods**

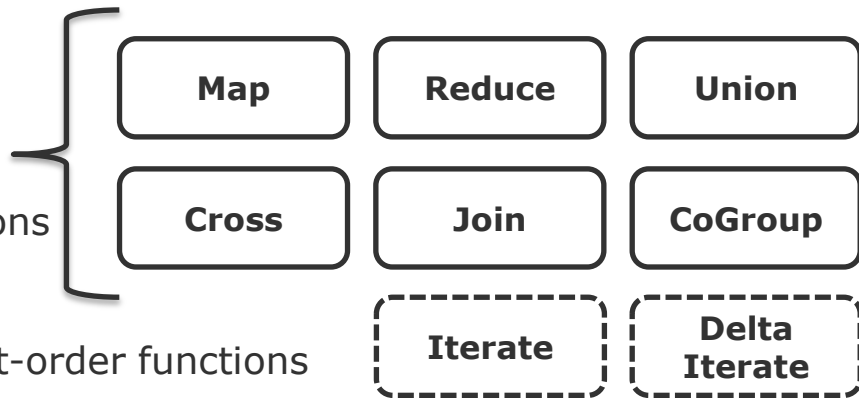
Sebastian Kruse,  
26th June, 2017

Chart 21

# Writing an Apache Flink program

## ■ Four ingredients

- Datasets
- First-order functions
  - high-level data operations
- Second-order functions
  - one passed to each first-order functions
  - refine semantics of first-order functions
  - transform data
- Directed acyclic graph
  - starts with data sources, ends in data sinks
  - describes workflow



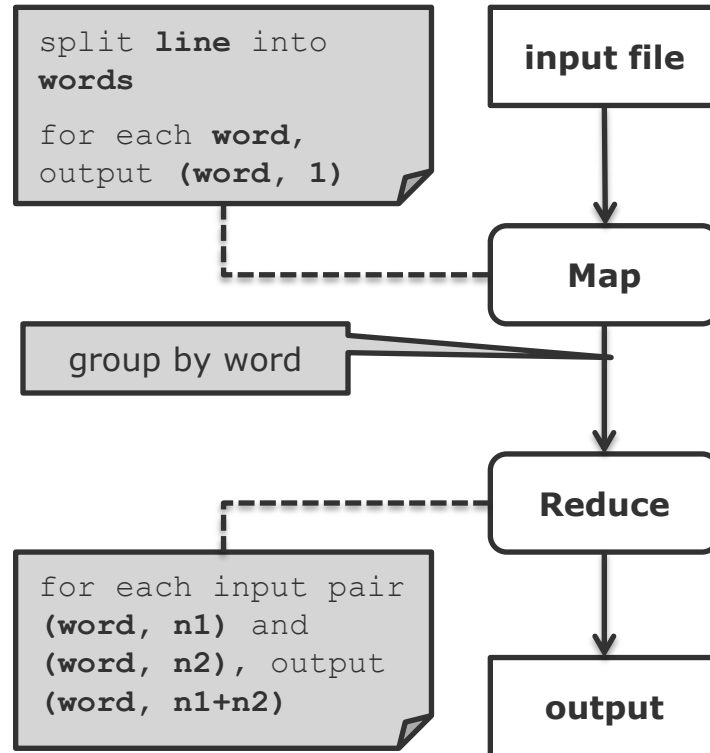
**Advanced IND detection methods**

Sebastian Kruse,  
26th June, 2017

Chart 22

# Classic example: word count

- implemented as **DAG** with two first-order functions (and two second-order functions)
- specifies
  - operations on a **logical** level
- does not specify
  - how to **parallelize**
  - data **serialization** and shipping
  - handling when available **main memory** is exceeded
  - **fault tolerance**
  - ...

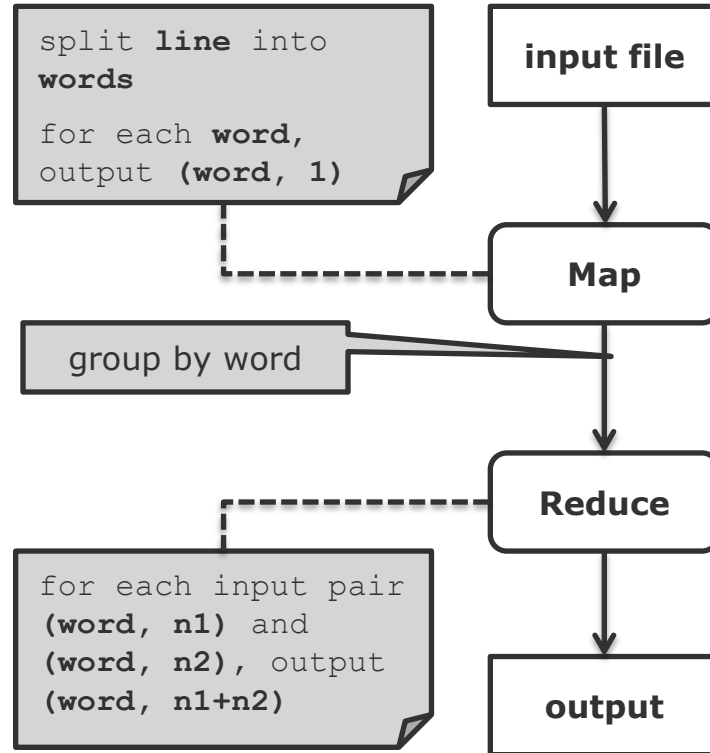
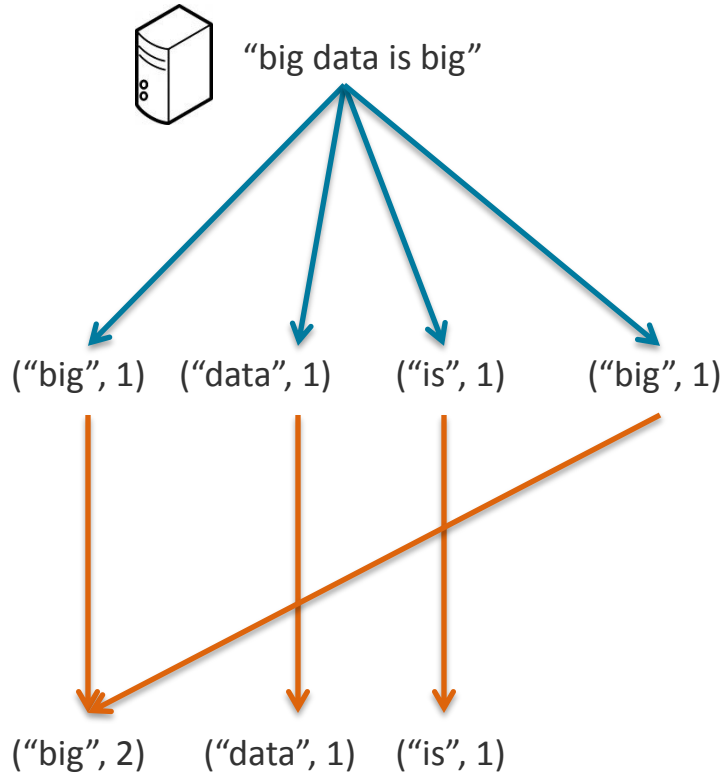


**Advanced IND detection methods**

Sebastian Kruse,  
26th June, 2017

Chart 23

# Classic example: word count



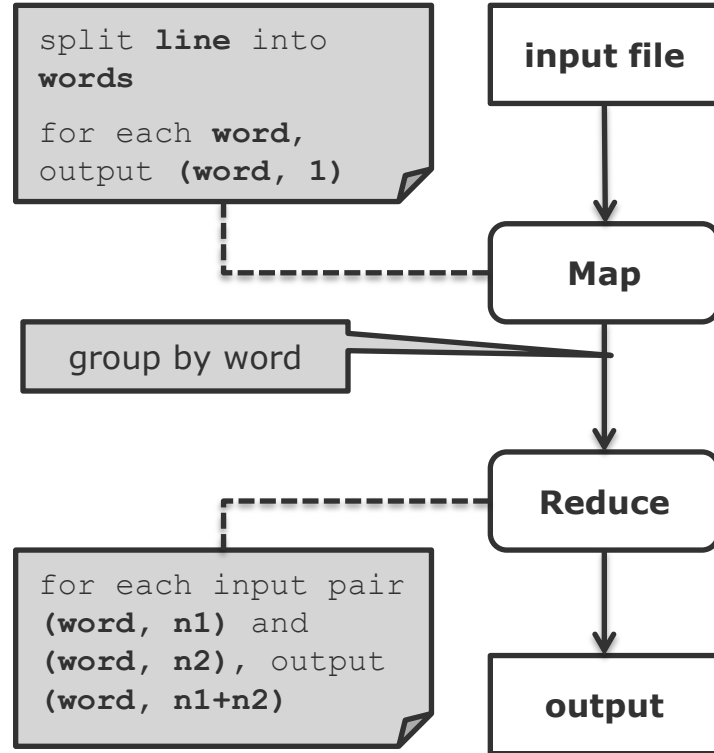
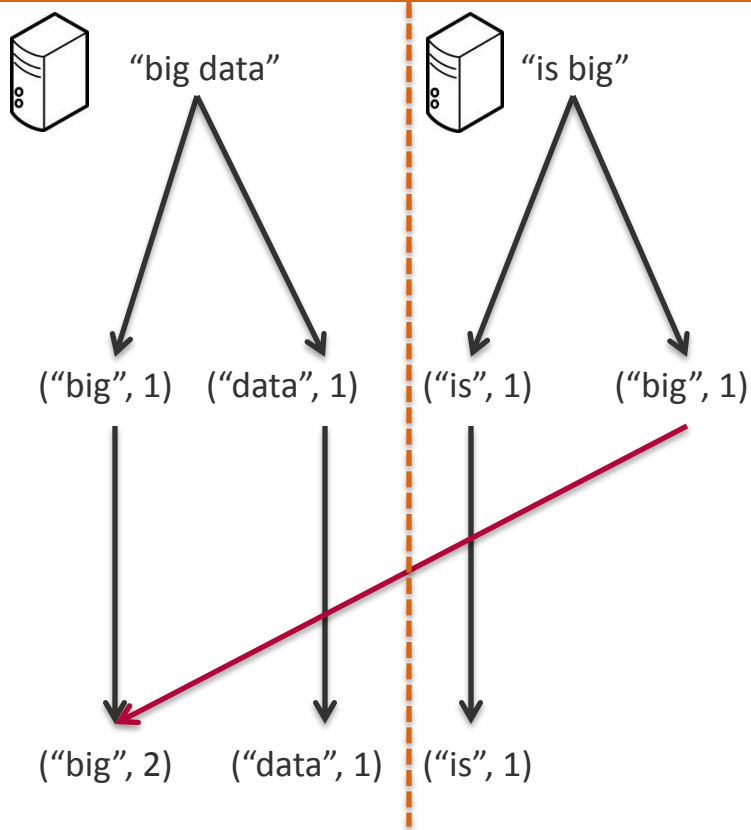
**Advanced IND  
detection methods**

Sebastian Kruse,  
26th June, 2017

Chart 24



# Classic example: word count



**Advanced IND detection methods**

Sebastian Kruse,  
26th June, 2017

Chart 25

# Classic example: word count

```
public class CountWords() {  
    public static void main(String[] args) {  
        ExecutionEnvironment env =  
            ExecutionEnvironment.getExecutionEnvironment();  
        env.readTextFile(args[0])  
            .flatMap(  
                (String line, Collector<WordCount> out) -> {  
                    Arrays.stream(line.split("\\W+"))  
                        .forEach(t -> out.collect(new WordCount(t, 1)))  
                })  
            .groupBy("word")  
            .sum("count")  
            .print();  
        env.execute();  
    }  
}
```



**Advanced IND  
detection methods**

Sebastian Kruse,  
26th June, 2017

Chart 26

# Intrinsic limitations of IND algorithms

- Observations: all IND algorithms follow a common pattern

Algorithm	Phase 1 Data Reorganization	Phase 2 Comparison
De Marchi	Create Inverted Index	Intersect Attribute Groups
SPIDER	Sort Columns	Simultaneous Iteration
BINDER	Partition Columns	In-Memory Partition Comparison

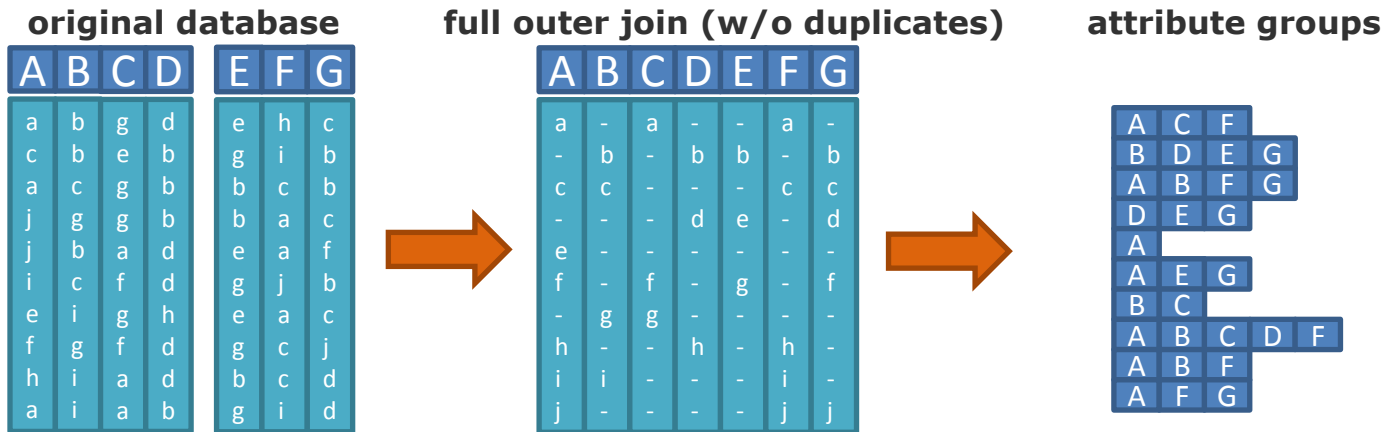
- e.g., IND  $A \subseteq B$ 
  - to prove, need to read A completely
  - to disprove, need to read B completely
- Data reorganization is the most expensive phase
  - I/O-heavy workload, but other phase brings considerable I/O as well

## Advanced IND detection methods

Sebastian Kruse,  
26th June, 2017

Chart 27

# General IND approach



$$X \subseteq Y \Leftrightarrow \forall x \in X : x \in Y$$

$$X \subseteq Y \Leftrightarrow \forall t \in X \bowtie Y : t[X] \neq \perp \rightarrow t[Y] \neq \perp$$

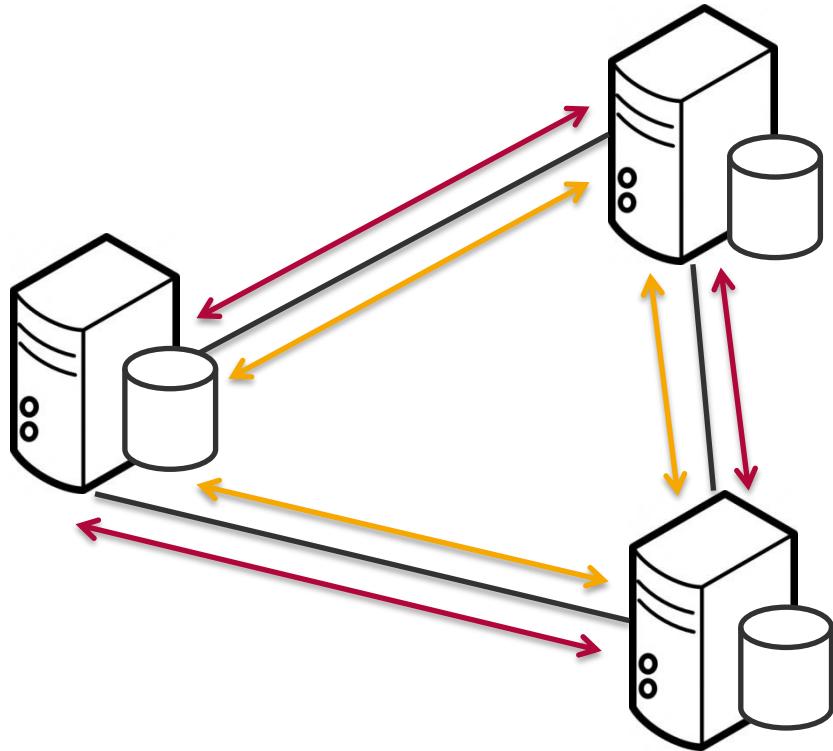
$$X \subseteq Y \Leftrightarrow \forall G \in \mathcal{G} : X \in G \rightarrow Y \in G$$

$$\Leftrightarrow Y \in \bigcap_{G \in \mathcal{G} | Y \in G} G$$

**Advanced IND detection methods**

Sebastian Kruse,  
26th June, 2017

# Distributed IND detection: general idea



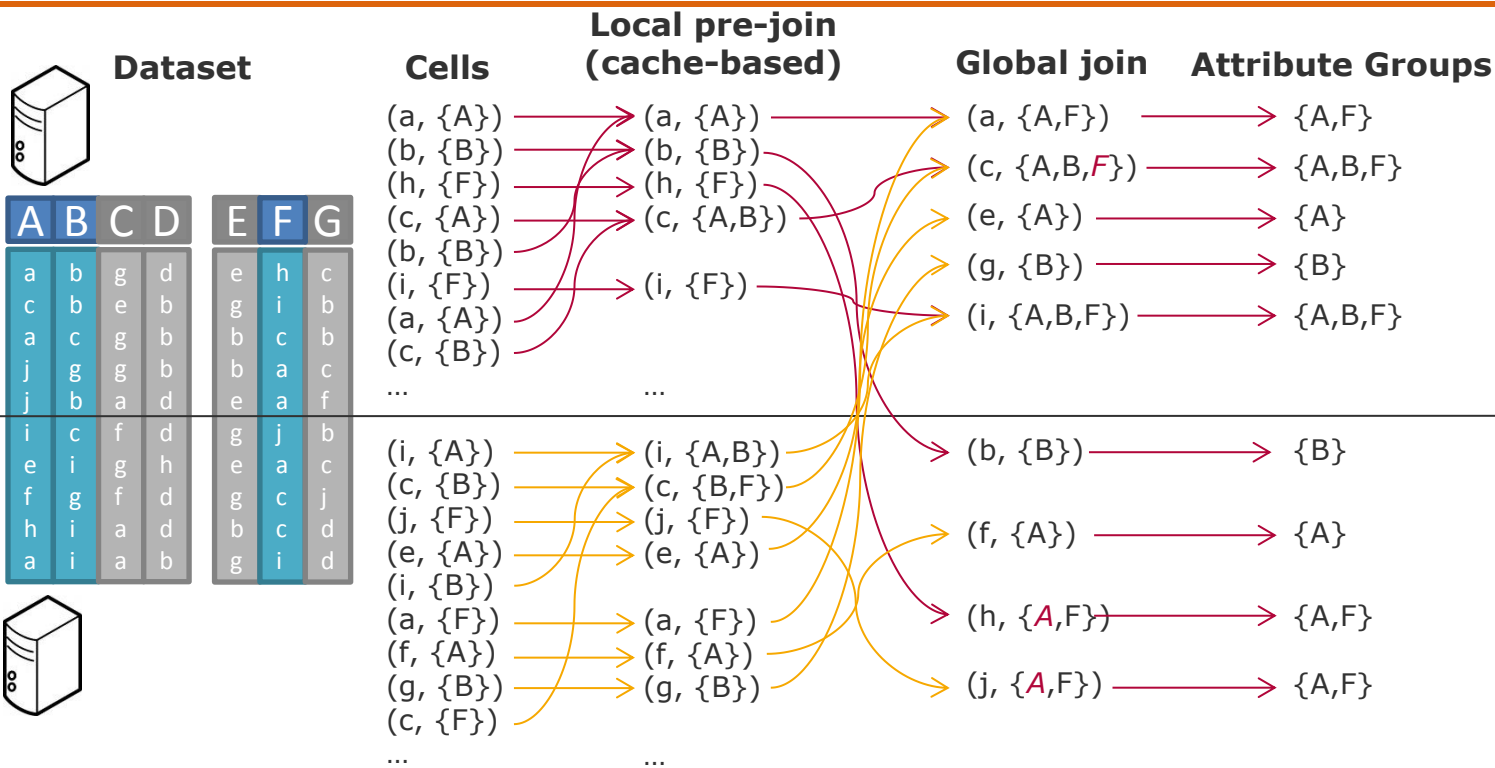
1. Calculate full outer join
2. Intersect attribute groups

**Advanced IND detection methods**

Sebastian Kruse,  
26th June, 2017

Chart 29

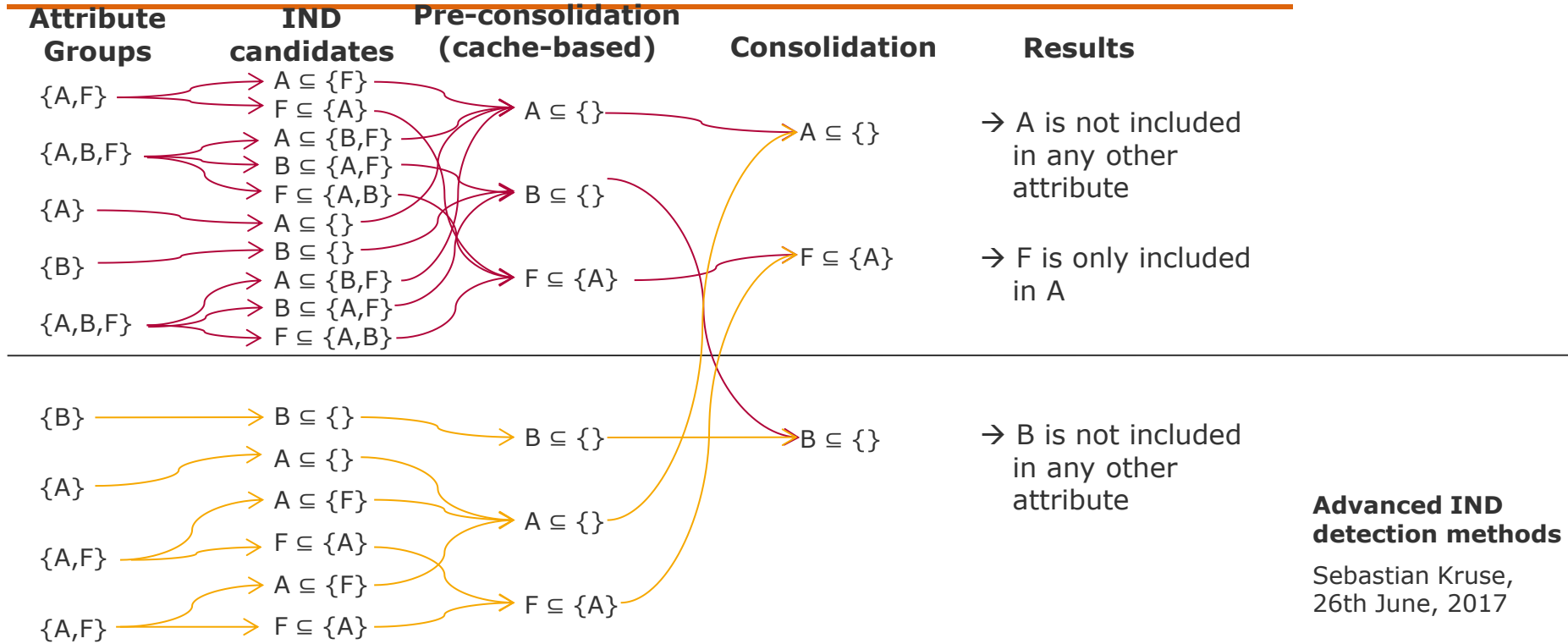
# SINDY: Calculate outer join



**Advanced IND detection methods**

Sebastian Kruse,  
26th June, 2017

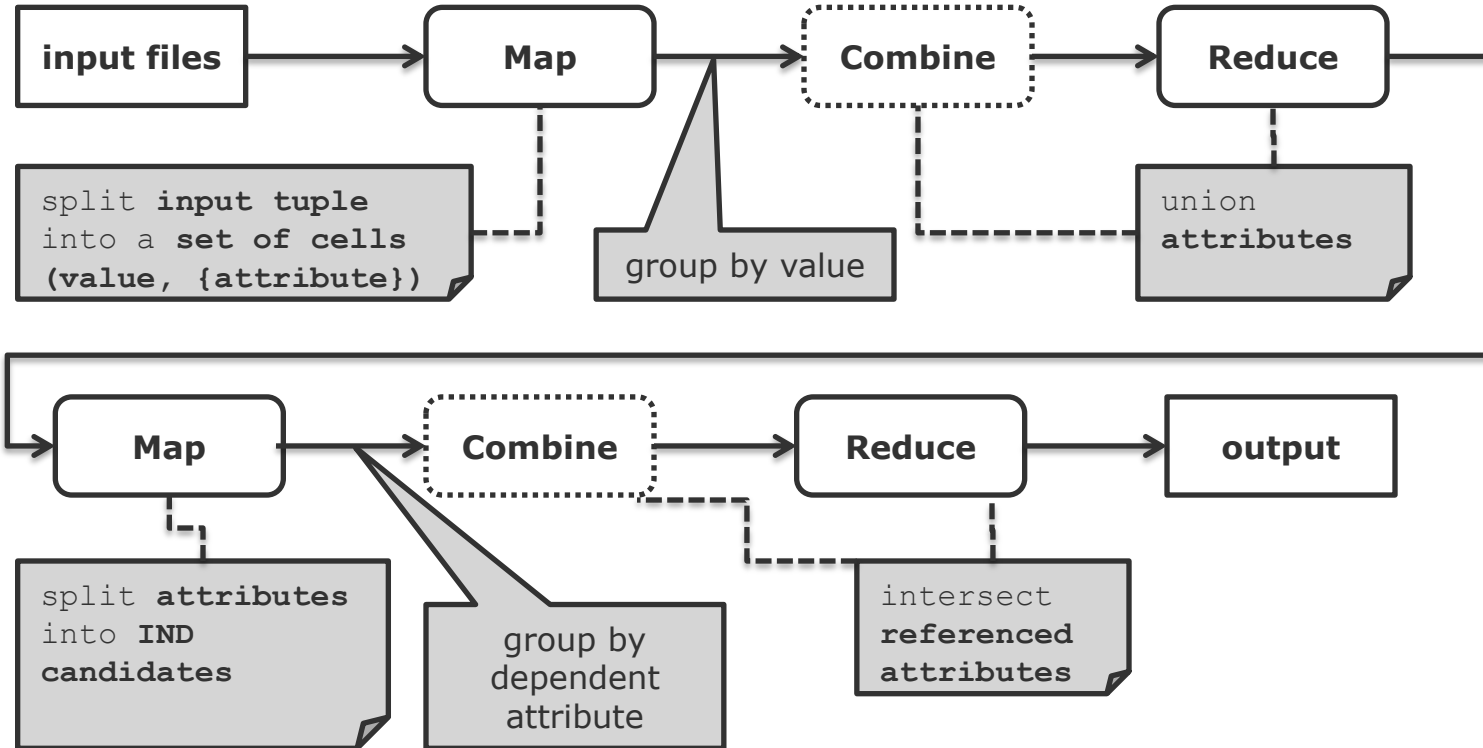
# Determine INDs from join result



**Advanced IND detection methods**

Sebastian Kruse,  
26th June, 2017

# Implementation on Flink (unary INDs)



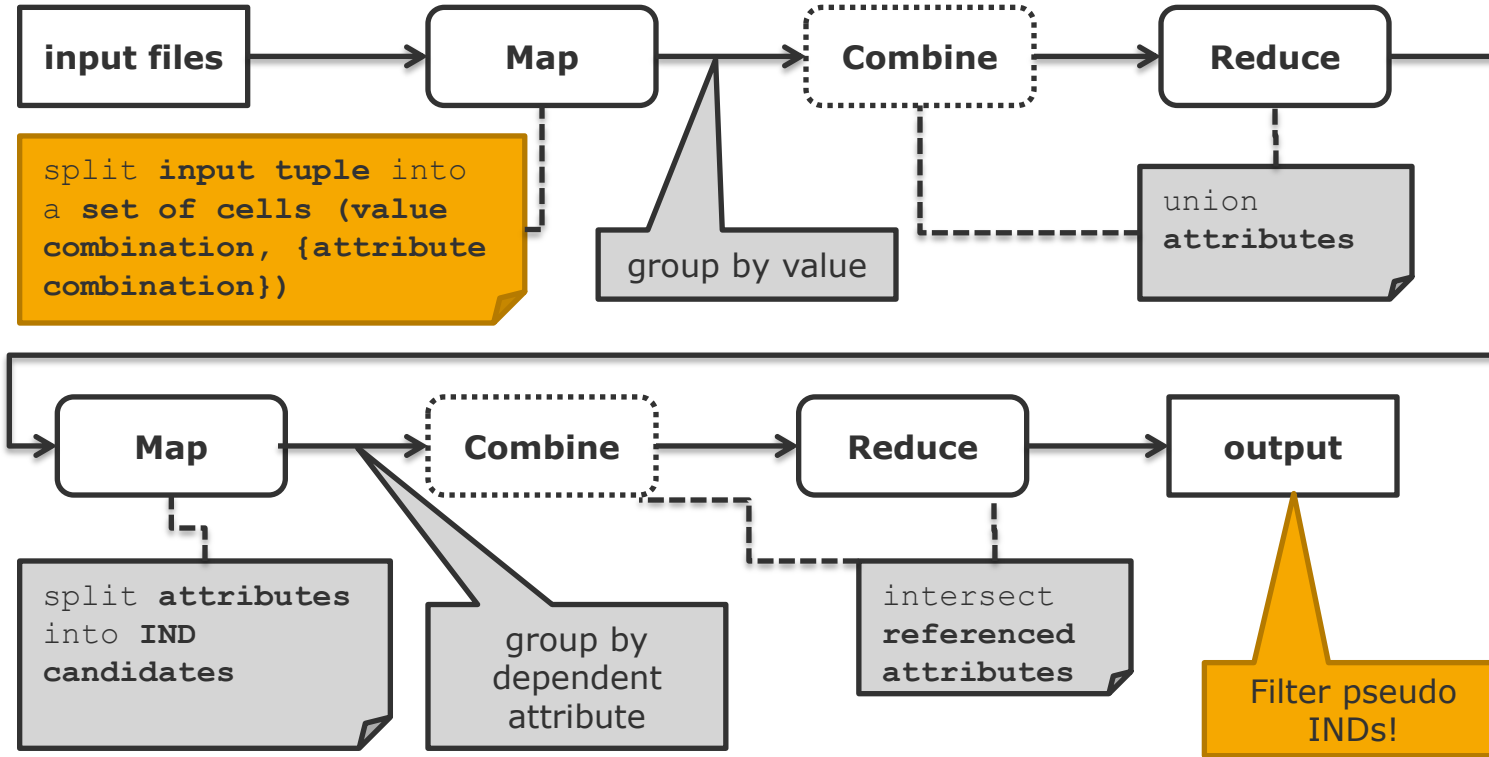
**Advanced IND detection methods**

Sebastian Kruse,  
26th June, 2017

Chart 32



# Implementation on Flink (n-ary INDs)



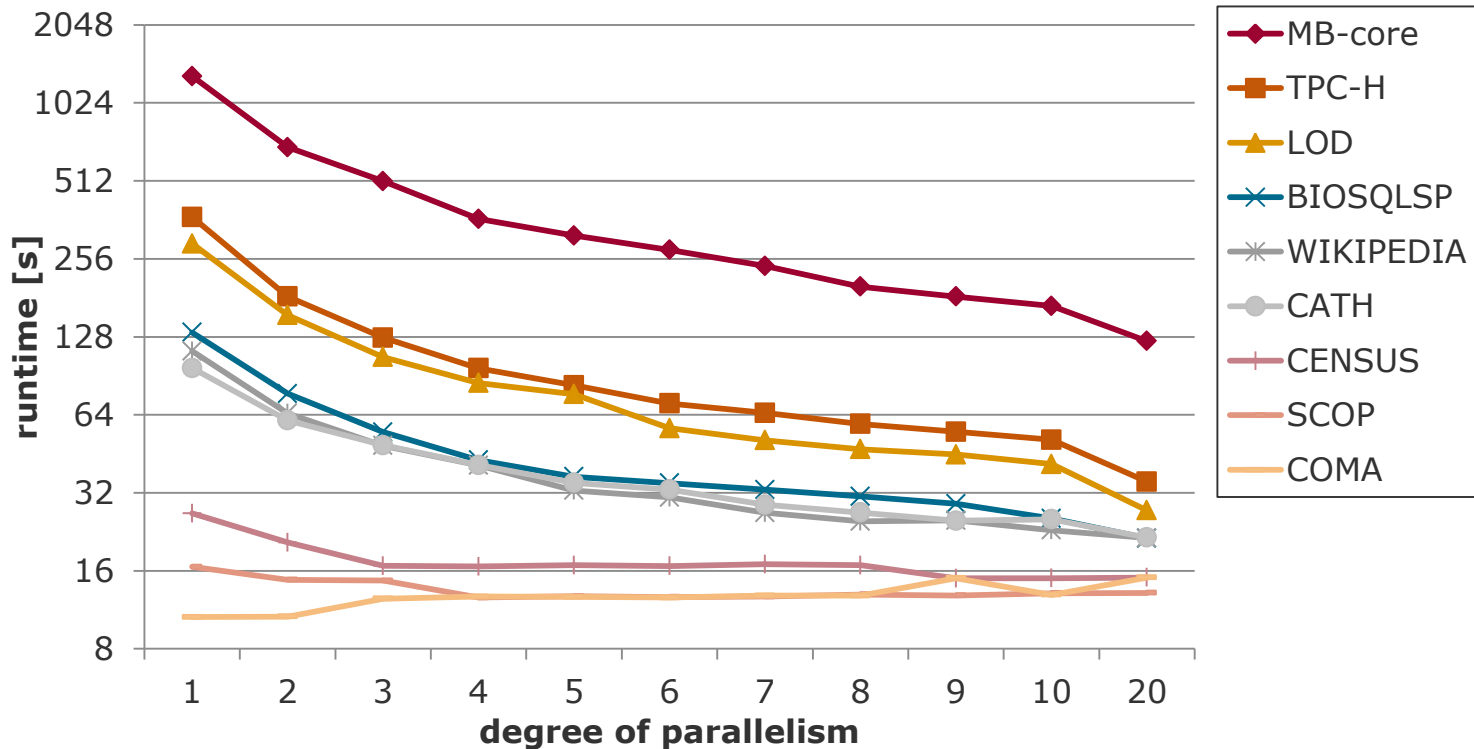
**Advanced IND detection methods**

Sebastian Kruse,  
26th June, 2017

Chart 33

# SINDY – scaling out IND detection

## Scale-out behavior

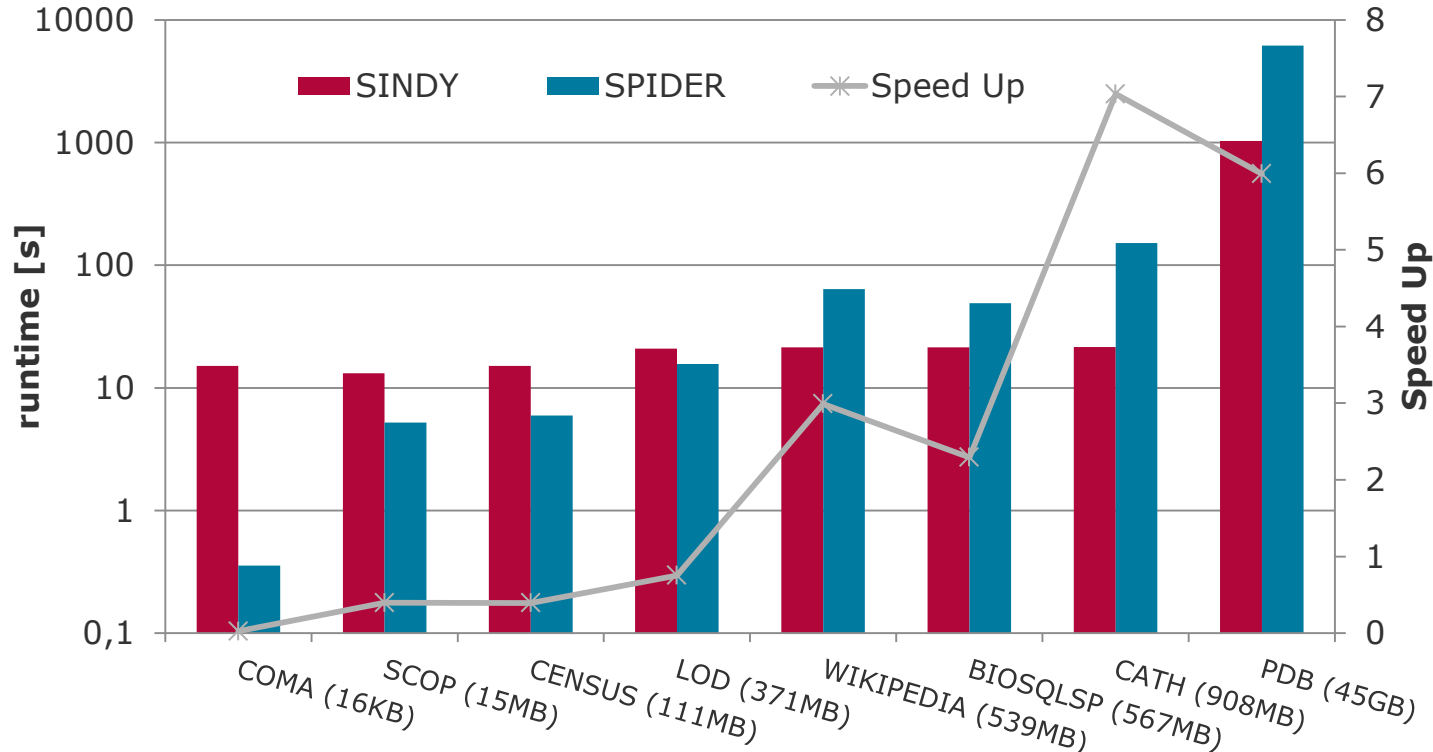


**Advanced IND detection methods**

Sebastian Kruse,  
26th June, 2017

Chart 34

# Performance comparison with SPIDER



**Advanced IND detection methods**

Sebastian Kruse,  
26th June, 2017

Chart 35

# Conclusions


- Problem of **IND detection can be scaled out** with the Map/Reduce paradigm
  - Comes with a certain loss of control
- SINDY does **not employ pruning** (except for apriori proceeding)
  - A general problem for distributed algorithms
  - Not a big issue for IND detection
- Only suitable **for large** datasets
- Arising questions
  - To what extent is attribute scaling possible? → MANY
  - What if some INDs are n-ary for some larger n?

**Advanced IND detection methods**


Sebastian Kruse,  
26th June, 2017

# Agenda

Unicode	Glyph	Symbol	Name	Diameter	Mass	Moons	Rings
U+2609	☉	Sun	Mercury	0.382	0.06	0	no
U+263D	☾	Moon	Venus	0.949	0.82	0	no
U+263E	☾	Moon	Earth	1.000	1.00	1	no
U+263F	☿	Mercury	Mars	0.532	0.11	2	no
U+2640	♀	Venus	Jupiter	11.209	317.8	67	yes
U+1F728	♁	Earth	Saturn	9.449	95.2	62	yes
U+2642	♂	Mars	Uranus	4.007	14.6	27	yes
U+2643	♃	Jupiter	Neptune	4.007	14.6	27	yes
U+2644	♄	Saturn	Uranus	4.007	14.6	27	yes
U+2645	♅	Uranus	Neptune	4.007	14.6	27	yes
U+2646	♆	Neptune	Pluto	4.007	14.6	27	yes
≈ U+2641	♁	Eris	Pluto	4.007	14.6	27	yes
≈ U+29EC	♁	Eris	Pluto	4.007	14.6	27	yes
U+2647	♇	Pluto	Pluto	4.007	14.6	27	yes
not present	--	Pluto	Pluto	4.007	14.6	27	yes
...	...	...	...	...	...	...	...



Sign	House	Domicile	Detriment	Exaltation
Aries	1st House	Mars	Venus	Sun
Taurus	2nd House	Venus	Pluto	Moon
Gemini	3rd House	Mercury	Jupiter	N/A
Cancer	4th House	Moon	Saturn	Jupiter
Leo	5th House	Sun	Uranus	Neptune
Virgo	6th House	Mercury	Neptune	Pluto, Mercury
Libra	7th House	Venus	Mars	Saturn
Scorpio	8th House	Pluto	Venus	Uranus
Capricorn	9th House	Jupiter	Mercury	N/A
...	...	...	...	...



Name	Mass	Orbital radius	Rotation period	Atmosphere
Mercury	0.06	0.47	58.64	minimal
Venus	0.82	0.72	-243.02	CO <sub>2</sub> , N <sub>2</sub>
Earth	1.00	1.00	1.00	N <sub>2</sub> , O <sub>2</sub> , Ar
Mars	0.11	1.52	1.03	CO <sub>2</sub> , N <sub>2</sub> , Ar
Jupiter	317.8	5.20	0.41	H <sub>2</sub> , He
Saturn	95.2	9.54	0.43	H <sub>2</sub> , He
Uranus	14.6	19.22	-0.72	H <sub>2</sub> , He
Neptune	17.2	30.06	0.67	H <sub>2</sub> , He

**BINDER**  
divide & conquer  
based IND detection

**SINDY**  
scaling out  
IND detection

**High arity**  
techniques to deal  
with high-arity INDs

**Advanced IND  
detection methods**

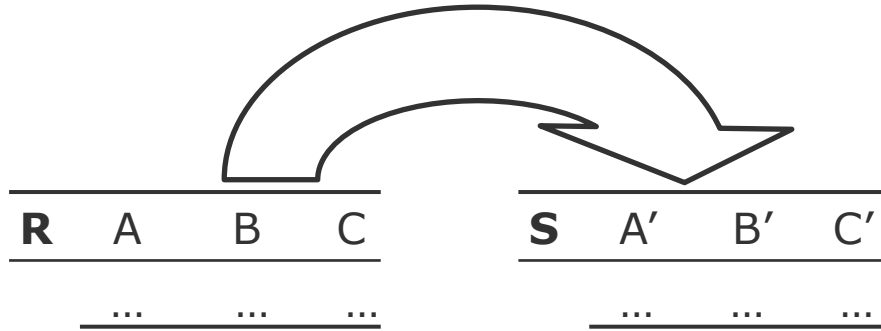
Sebastian Kruse,  
26th June, 2017

Chart **37**

- High-arity INDs do not go well together with apriori-based algorithms
  - Consider an IND of arity  $n$
  - Then there are  $2^n - 2$  sub-INDs to be verified
  - No pruning possible
  - Recall the hardness of  $n$ -ary IND discovery
- Different approaches necessary
  - Cf. TANE and HyFD

- Most (maximal) INDs are of low arity, but we do find high-arity INDs when...

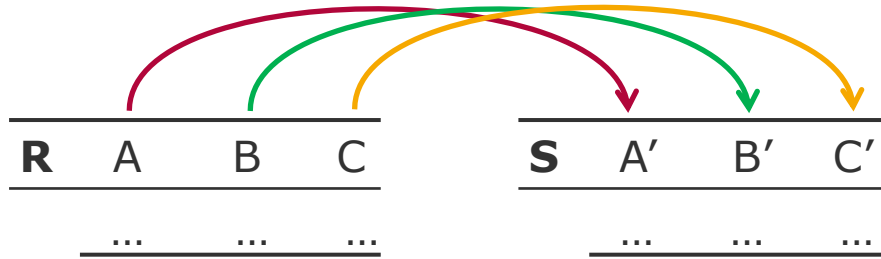
# A different notation for n-ary INDs



$$R[A, B, C] \subseteq S[A', B', C']$$



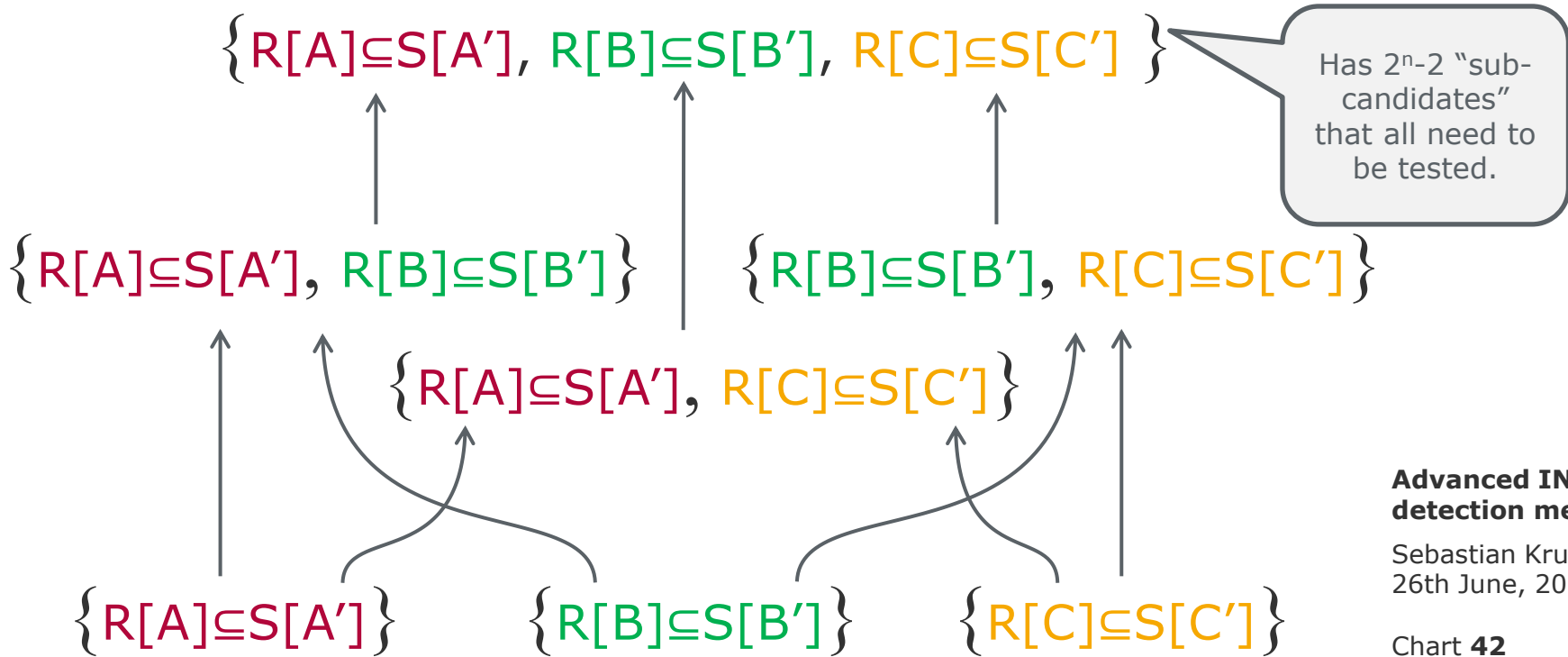
# A different notation for n-ary INDs



$$\text{ens}( R[A, B, C] \subseteq S[A', B', C'] ) =$$

$$\{ R[A] \subseteq S[A'], R[B] \subseteq S[B'], R[C] \subseteq S[C'] \}$$

# A different notation for n-ary INDs

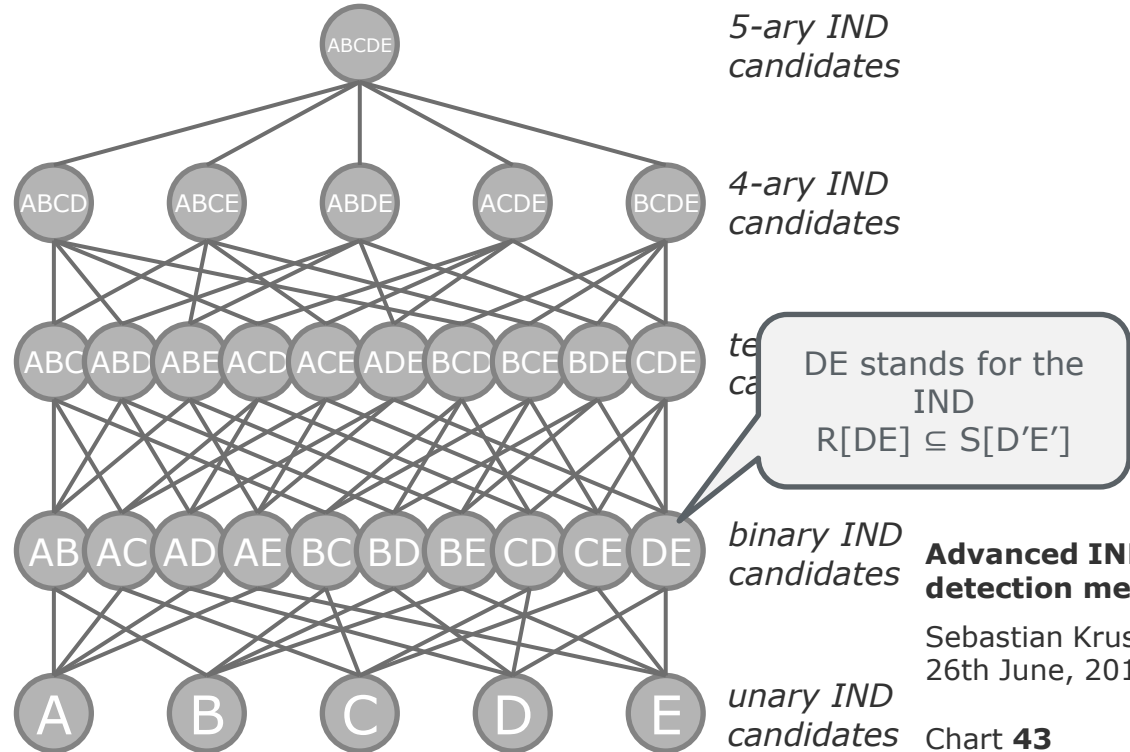


**Advanced IND  
detection methods**

Sebastian Kruse,  
26th June, 2017

Chart 42

# Optimistic and pessimistic strategies



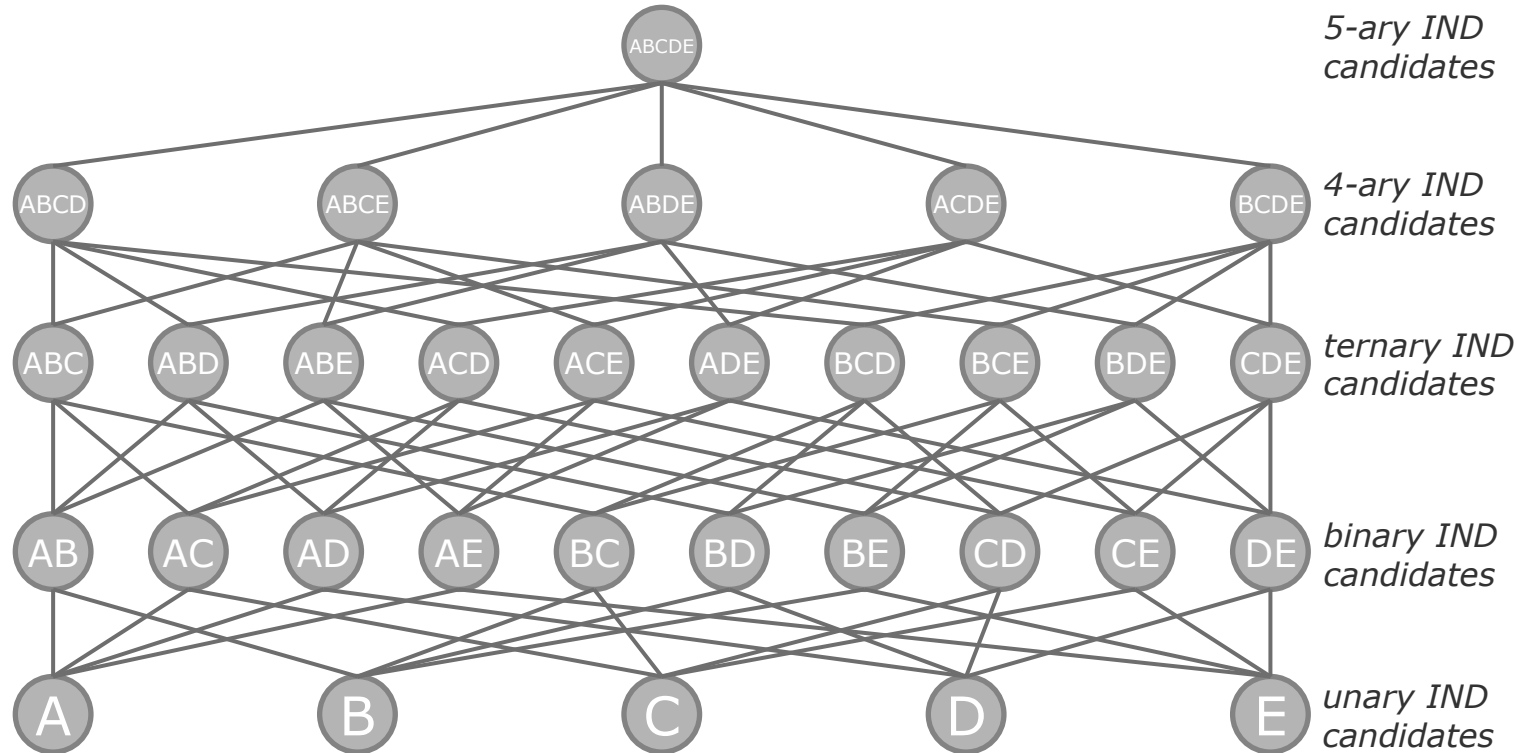
**Advanced IND detection methods**

Sebastian Kruse,  
26th June, 2017

Chart 43

# High-arity INDs - ZigZag

## IND borders



### Advanced IND detection methods

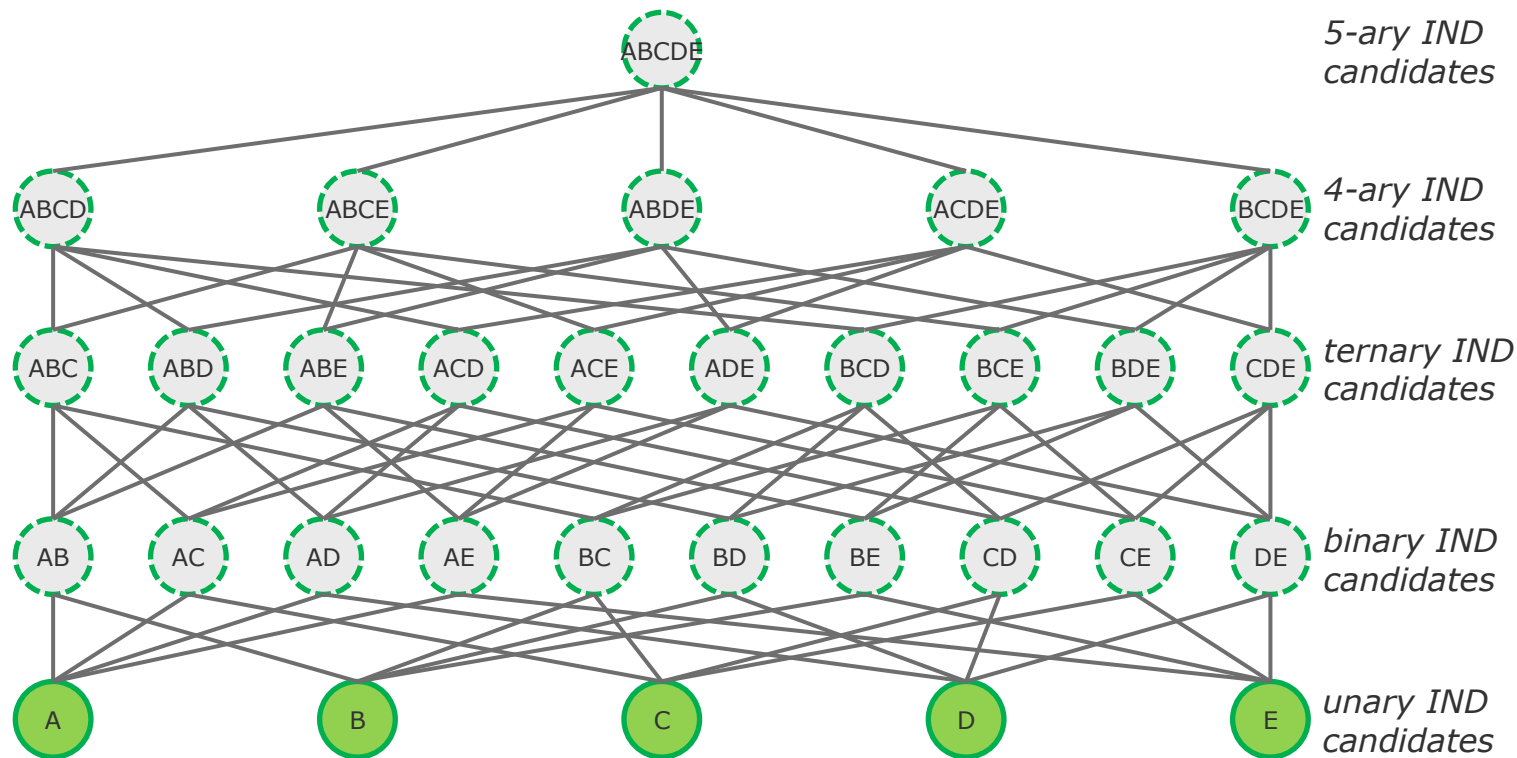
Sebastian Kruse,  
26th June, 2017

Chart 44

- IND
- Maximal IND
- IND candidate
- Non-IND
- Minimal non-IND

# High-arity INDs - ZigZag

## IND borders



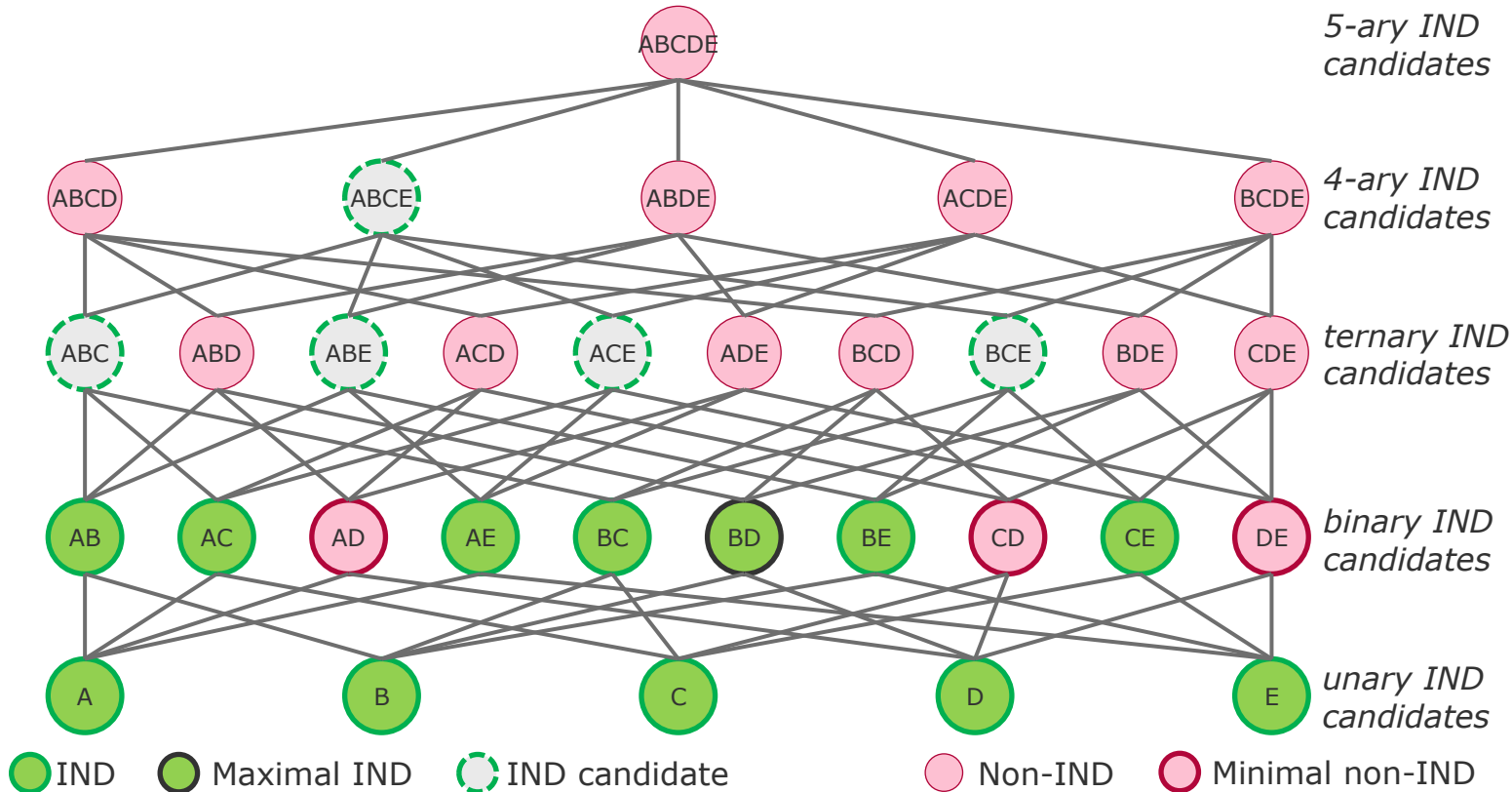
### Advanced IND detection methods

Sebastian Kruse,  
26th June, 2017

Chart 45

# High-arity INDs - ZigZag

## IND borders



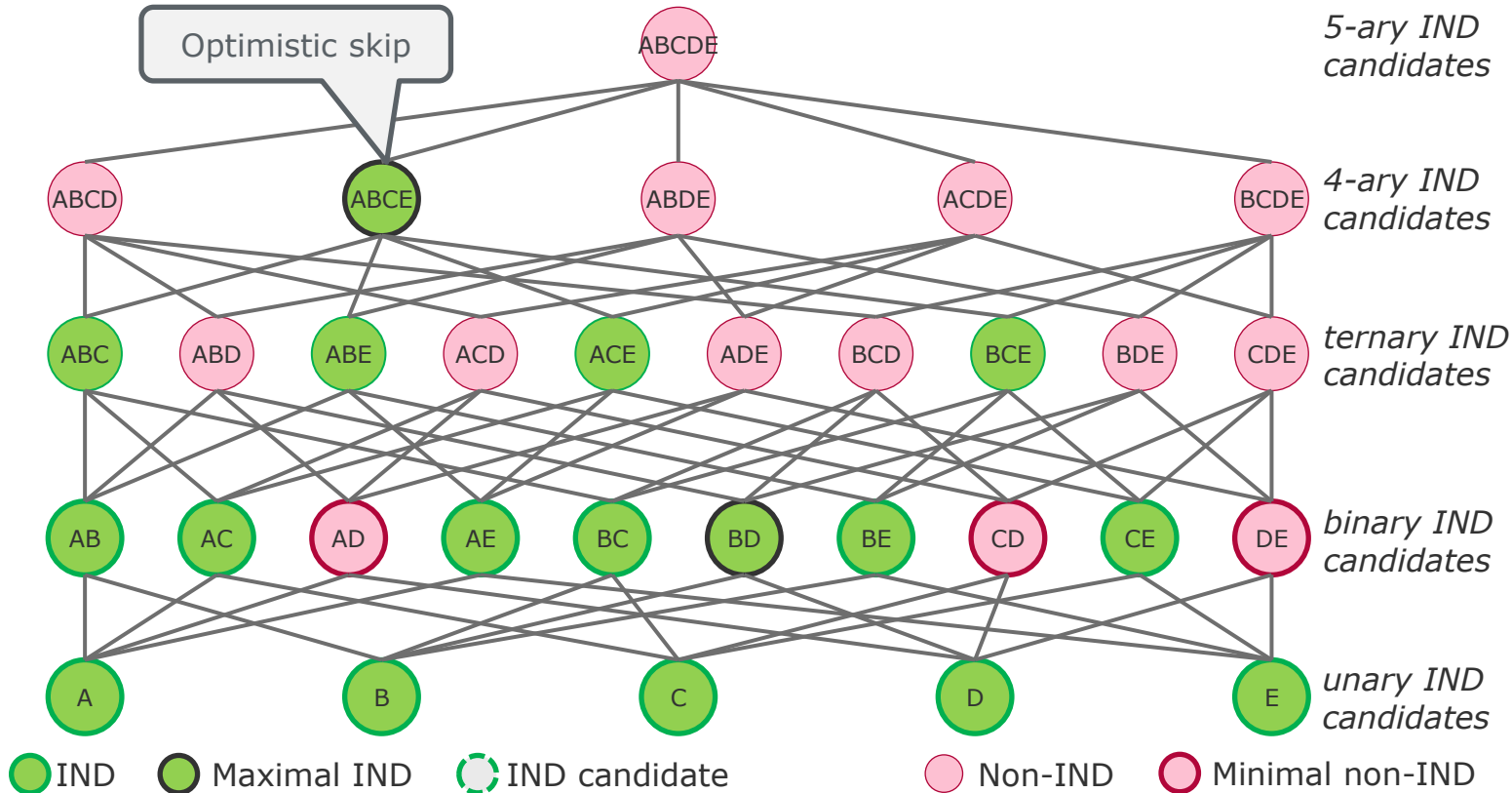
**Advanced IND detection methods**

Sebastian Kruse,  
26th June, 2017

Chart 46

# High-arity INDs - ZigZag

## IND borders



**Advanced IND detection methods**

Sebastian Kruse, 26th June, 2017

Chart 47

# Calculate the optimistic IND border

- Given two tables, and a set of known INDs and/or non-INDs, how can we determine *the optimistic IND border*?
  - All IND candidates that are (i) **not known non-INDs** and (ii) are **maximal** w.r.t. property (i).
- FIND<sub>2</sub>
  - Determine **hypergraph cliques** based on INDs
- ZigZag
  - Determine **hitting sets** based on non-INDs



# Calculate the optimistic IND border

## ■ Example:

- Unary INDs = {A, B, C, D, E}
- INDs = {AB, AC, AE, BC, BD, BE, CE}
- non-INDs = {AD, CD, DE}

## ■ Goal:

- find **all maximal** sets  $\subseteq$  ABCDE that are **no supersets** of AD, CD, or DE

## ■ General strategy

- Determine **minimal sets** that **intersect** with **all** non-INDs (ACE, D)
- Remove these minimal sets from ABCDE (BD, ABCE)

**Advanced IND  
detection methods**

Sebastian Kruse,  
26th June, 2017

Chart **49**

# Calculate the optimistic IND border (simple)

■ **Input:** non-INDs N

$N=[AD, CD, DE]$

**Advanced IND  
detection methods**

Sebastian Kruse,  
26th June, 2017

Chart **50**

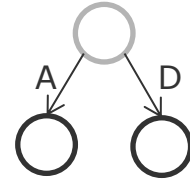
# Calculate the optimistic IND border (adv.)

- **Input:** non-INDs  $N$ , unary INDs  $U$      $N=[AD, CD, DE]$ ,  $U=\{A, B, C, D, E\}$

# Calculate the optimistic IND border (adv.)

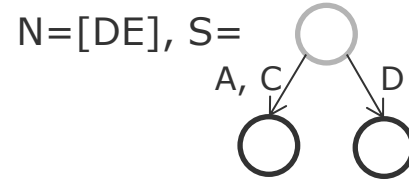
- Current state

$N=[CD, DE], S=$



# Calculate the optimistic IND border (adv.)

- Current state



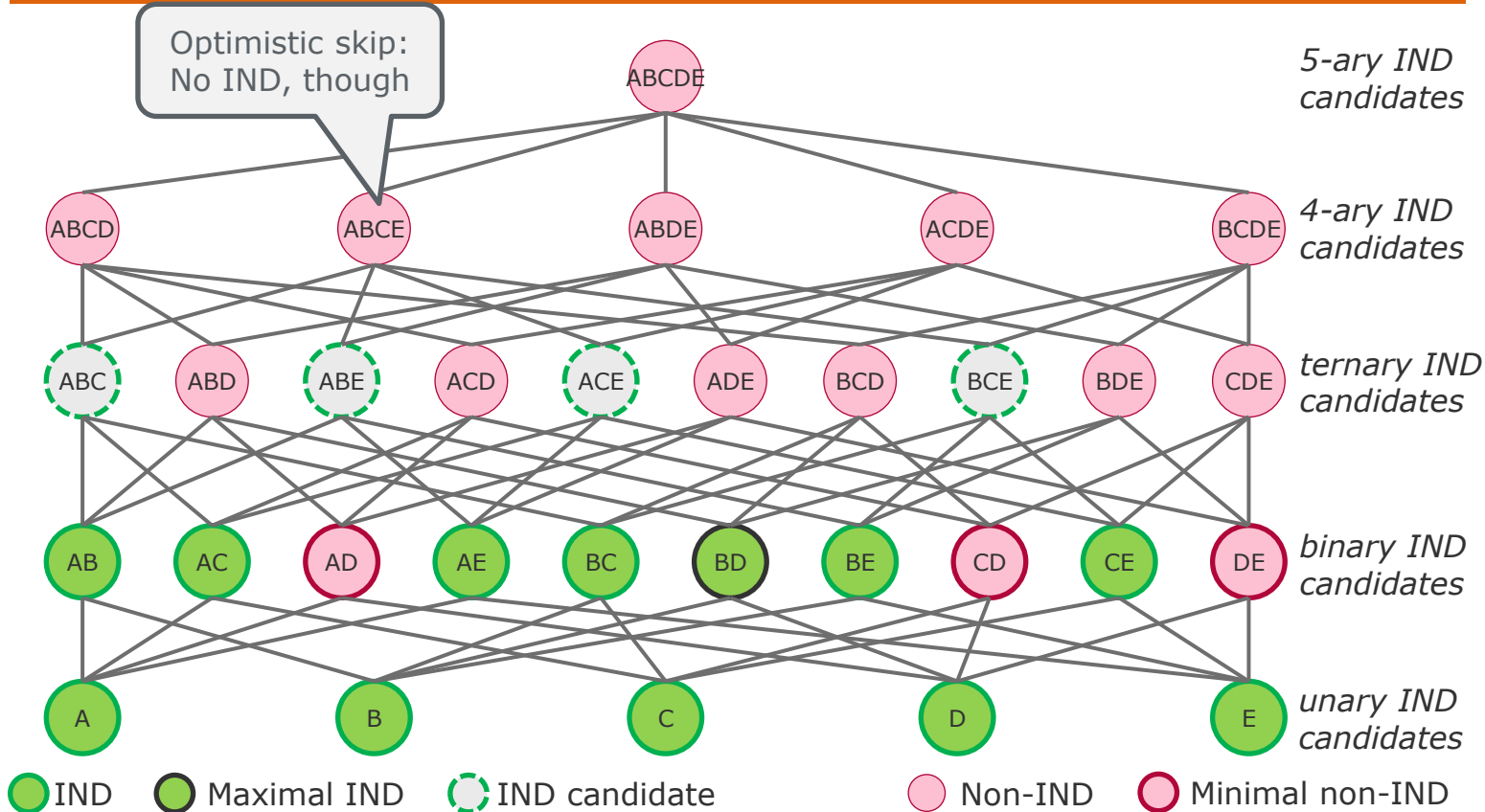
# Calculate the optimistic IND border (adv.)

- For the attentive student:
  - (6) update  $S$  with all elements in  $L$  except a subset is already in  $S$ 
    - What if an existing solution is a superset of a new solution?
- This is not possible (inductive proof):
  - Assume, we introduced a new element  $N$  that is a subset of some existing element  $E$  in  $S$
  - Then we would have obtained  $N$  from some  $N' = N \setminus I$  for some unary IND in  $U$ .
  - Hence,  $S$  must have been already in an inconsistent state.
  - Initially,  $S = \{\emptyset\}$ , which is a consistent state.
  - What about two elements being added in a single iteration, though?  
→ Figure out yourselves.

## Advanced IND detection methods

Sebastian Kruse,  
26th June, 2017

# Non-INDs in the optimistic IND border

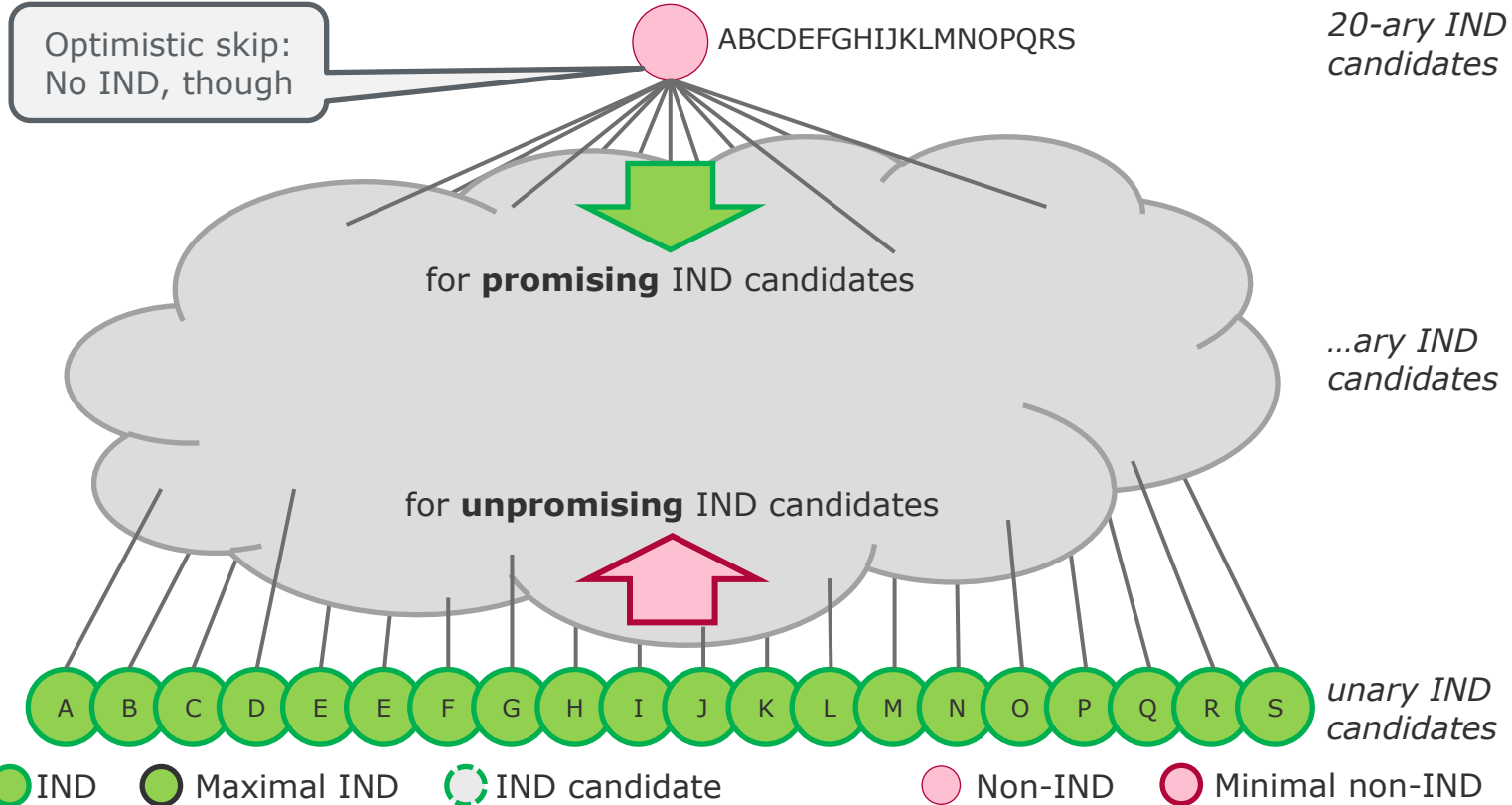


**Advanced IND detection methods**

Sebastian Kruse,  
26th June, 2017

Chart **55**

# Non-INDs in the optimistic IND border



**Advanced IND detection methods**

Sebastian Kruse,  
26th June, 2017

Chart **56**



# Non-INDs in the optimistic IND border

- Promising IND candidate  $R[X] \subseteq S[Y]$  if  $g'_3(R[X] \subseteq S[Y]) \leq \varepsilon$
- $g'_3(R[X] \subseteq S[Y])$ : **proportion of distinct values** in  $R[X]$  to be removed, such that  $R[X] \subseteq S[Y]$  is a valid IND
  - Alternative: proportion of **tuples** to be removed from  $R$
- Example:  $g'_3(R[Planet] \subseteq S[Planet]) = 1 / 10 = 0.1$ 
  - The value "Ceres" has to be removed out of 10 distinct values

R

Planet	Mean distance	Relative mean distance
Mercury	57.91	1
Venus	108.21	1.86859
Earth	149.6	1.3825
Mars	227.92	1.52353
Ceres	413.79	1.81552
Jupiter	778.57	1.88154
Saturn	1,433.53	1.84123
Uranus	2,872.46	2.00377
Neptune	4,495.06	1.56488
Pluto	5,869.66	1.3058

S

Planet	Calculated (in AU)	Observed (in AU)	Perfect octaves	Actual distance
Mercury	0.4	0.387	0	0
Venus	0.7	0.723	1	1.1
Earth	1	1	2	2
Mars	1.6	1.524	4	3.7
Asteroid belt	2.8	2.767	8	7.8
Jupiter	5.2	5.203	16	15.7
Saturn	10	9.539	32	29.9
Uranus	19.6	19.191	64	61.4
Neptune	38.8	30.061	96	-96.8
Pluto	77.2	39.529	128	127.7

## Advanced IND detection methods

Sebastian Kruse,  
26th June, 2017

# Non-INDs in the optimistic IND border

- 1. Input:** tables  $R$  and  $S$ , pessimistic levels  $k$ , promising error  $\varepsilon$
- Calculate lower  $k$  levels with a pessimistic approach (e.g., BINDER)
- Calculate optimistic IND border from non-INDs
- 4. For each** IND candidate  $I$  in the optimistic IND border
  - Calculate error  $g'_3(I)$  of  $I$
  - If**  $g'_3(I) = 0$  **then output** IND  $I$
  - Else if**  $g'_3(I) \leq \varepsilon$  **then** traverse lattice top-down breadth-first from  $I$
  - Else** add all  $k+1$ -ary parent IND candidates of  $I$  to the pessimistic IND candidates
- Check all pessimistic IND candidates
- 6. If** there are open IND candidates, set  $k=k+1$  and start over with **step 3**

# Practical considerations

- A strategy for handling more than **two tables** is missing
- Several **optimizations** are possible, e.g., not all kinds of unary INDs can be combined to valid  $n$ -ary IND candidates (attribute repetition)
- **Empirical evidence** on the actual advantages of optimistic IND discovery is **missing**
  - Thorough evaluation all IND algorithms is called for!
- The original article on ZigZag proposes to do use **SQL-based error checks** for  $n$ -ary INDs (cf. MIND)
  - the traversal strategy, however, is **orthogonal** to IND error checks
  - more efficient techniques, such as those of BINDER and SINDY, could be used instead

**Advanced IND detection methods**

Sebastian Kruse,  
26th June, 2017

Chart **59**

# FDs cause high-arity INDs

- Consider following dependencies:  $[ZIP', City'] \subseteq [ZIP, City]$  and  $ZIP \rightarrow City$
- **Rule 1)** Then  $ZIP' \rightarrow City'$  is also a valid FD.
  - Because FDs cannot be violated by **removing** tuples.
- Additionally, consider  $[Name', ZIP'] \subseteq [Name, ZIP]$
- **Rule 2)** Then  $[Name', ZIP', City'] \subseteq [Name, ZIP, City]$  is an IND.
  - Because if  $t[ZIP] = t[ZIP']$ , then  $t[City] = t[City']$ .

Name	Zip	City
Tim	10627	Berlin
Tom	10627	Berlin
Tom	14482	Potsdam
Sandy	10324	Berlin
Inge	14469	Potsdam

**Students**

Name'	Zip'	City'
Tim	10627	Berlin
Tom	10627	Berlin
Inge	14469	Potsdam

**HPI Students**

## Advanced IND detection methods

Sebastian Kruse,  
26th June, 2017

Chart **60**

# Augmentation rules

- Idea: split INDs into “core” INDs and “augmentation rules”
  - IND:  $[Name', ZIP'] \subseteq [Name, ZIP]$
  - AR:  $[ZIP'] \subseteq [ZIP] \rightarrow [City'] \subseteq [City]$
- Separates INDs into core and supplemental INDs
  - Useful for foreign key discovery and understanding
- Potentially reduces the size of the result set
  - Speed up discovery and make results more manageable

Name	Zip	City
Tim	10627	Berlin
Tom	10627	Berlin
Tom	14482	Potsdam
Sandy	10324	Berlin
Inge	14469	Potsdam

Students

Name'	Zip'	City'
Tim	10627	Berlin
Tom	10627	Berlin
Inge	14469	Potsdam

HPI Students

## Advanced IND detection methods

Sebastian Kruse,  
26th June, 2017

Chart 61

# Augmentation rule discovery

- Assume, we know  $[ZIP'] \subseteq [ZIP]$  and  $[ZIP', City'] \subseteq [ZIP, City]$ 
  - Problem: we **need to know** if  $ZIP \rightarrow City$  is an FD to tell if  $[ZIP'] \subseteq [ZIP] \rightarrow [City'] \subseteq [City]$  is an AR.
- Solution 1: Discover FDs beforehand (e.g., with HyFD).
- Solution 2: Check relevant FD candidates **on-the-fly**.
  - $ZIP \rightarrow City \leftrightarrow |\pi(ZIP)| = |\pi(ZIP, City)|$  (cf. TANE)
  - We have to group our data anyways, so we can “**piggyback**” the counting of distinct values at little extra cost.

Name	Zip	City
Tim	10627	Berlin
Tom	10627	Berlin
Tom	14482	Potsdam
Sandy	10324	Berlin
Inge	14469	Potsdam

**Students**

Name'	Zip'	City'
Tim	10627	Berlin
Tom	10627	Berlin
Inge	14469	Potsdam

**HPI Students**

## Advanced IND detection methods

Sebastian Kruse,  
26th June, 2017

Chart **62**

# Augmentation rule discovery

- Special case: columns/INDs with only a **single value**
  - $[Status'] \subseteq [Status]$  is valid
  - $X \rightarrow Status$  is a valid AR for any column  $X$  in *Students*
- $\{\}$   $\rightarrow [Status'] \subseteq [Status]$  is a valid AR
- This is a very frequent case
  - **Empty or constant columns** can be found in many databases
  - They are **highly susceptible** to form  $n$ -ary INDs

Name	Zip	City	Status
Tim	10627	Berlin	Student
Tom	10627	Berlin	Student
Tom	14482	Potsdam	Student
Sandy	10324	Berlin	Student
Inge	14469	Potsdam	Student

**Students**

Name'	Zip'	City'	Status'
Tim	10627	Berlin	Student
Tom	10627	Berlin	Student
Inge	14469	Potsdam	Student

**HPI Students**

## Advanced IND detection methods

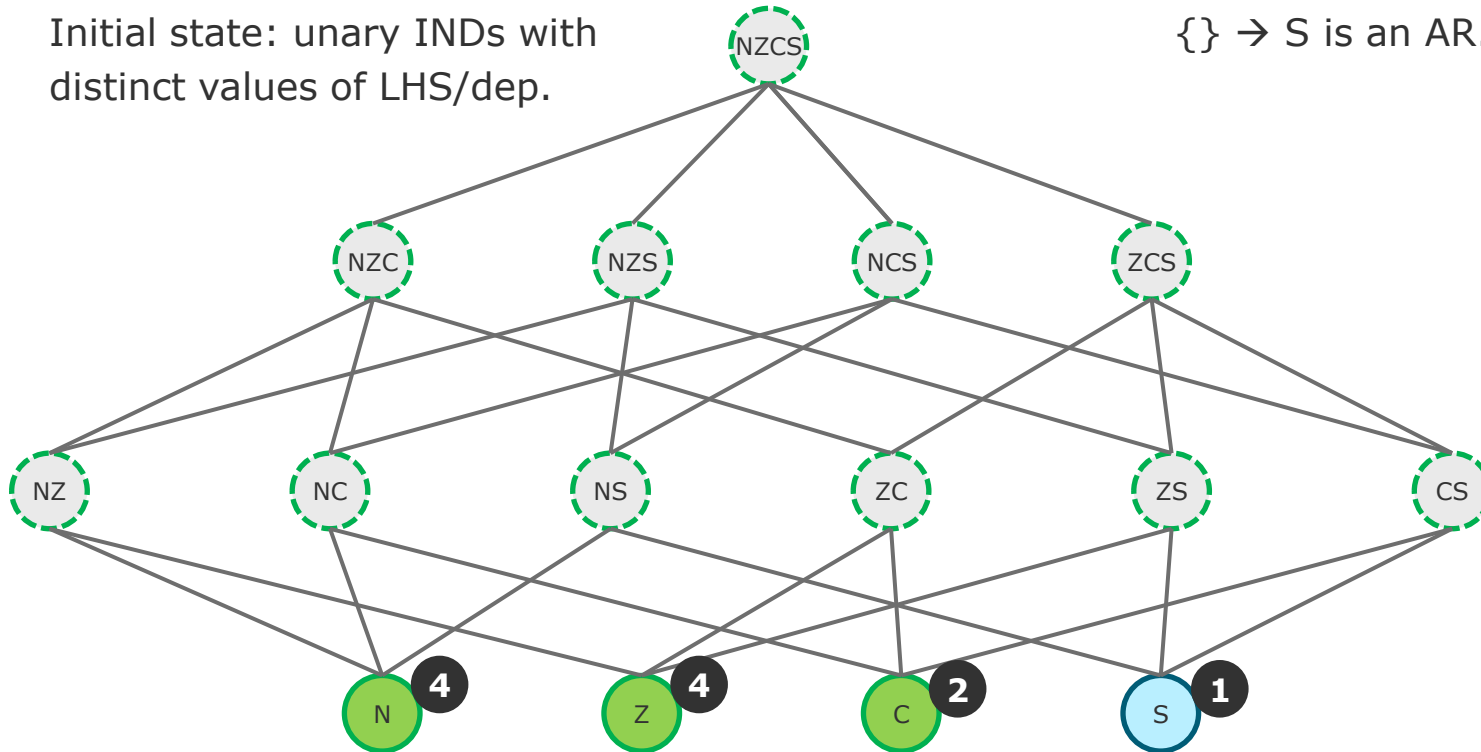
Sebastian Kruse,  
26th June, 2017

Chart **63**

# Mixed IND and AR discovery

Initial state: unary INDs with distinct values of LHS/dep.

$\{\}$   $\rightarrow$  S is an AR.



**Advanced IND detection methods**

Sebastian Kruse,  
26th June, 2017

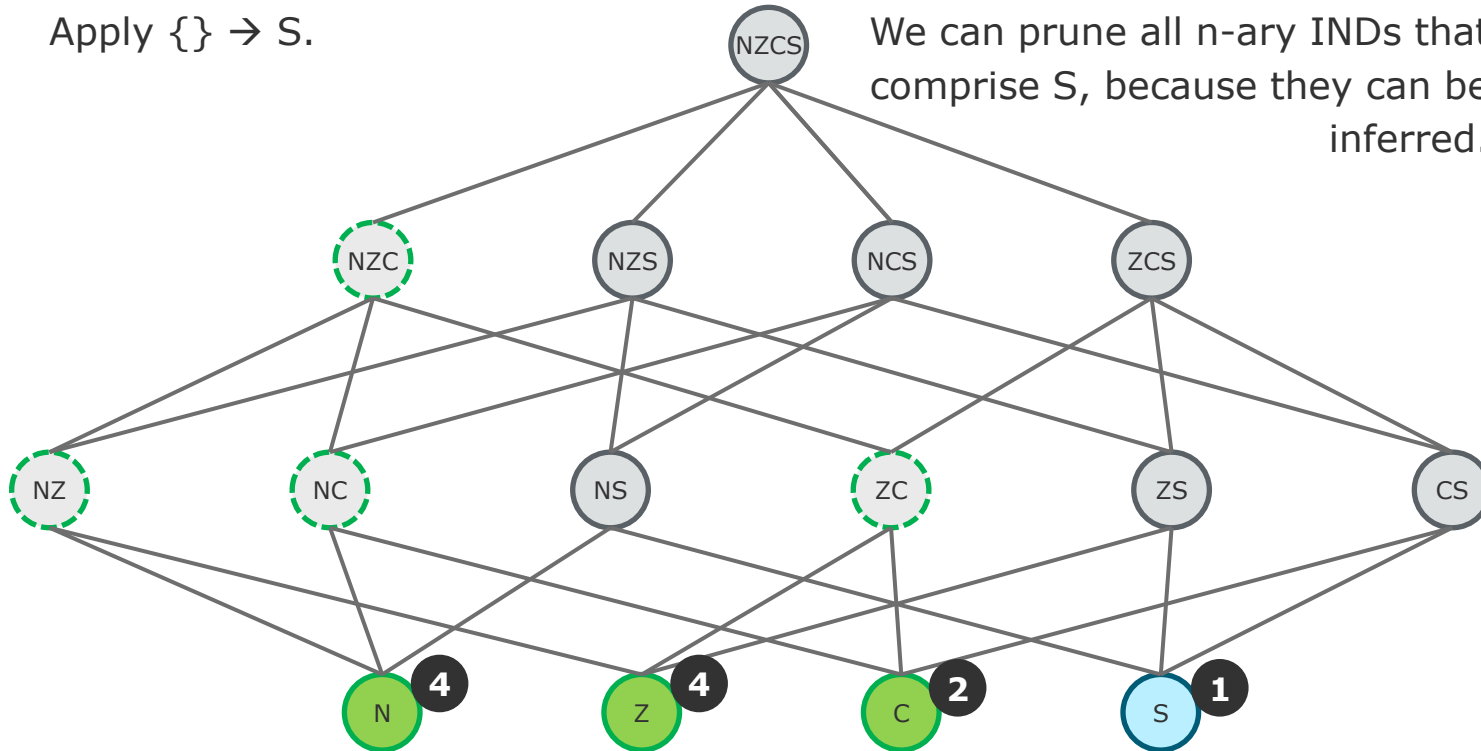
Chart 64



# Mixed IND and AR discovery

Apply  $\{\} \rightarrow S$ .

We can prune all n-ary INDs that comprise S, because they can be inferred.



**Advanced IND detection methods**

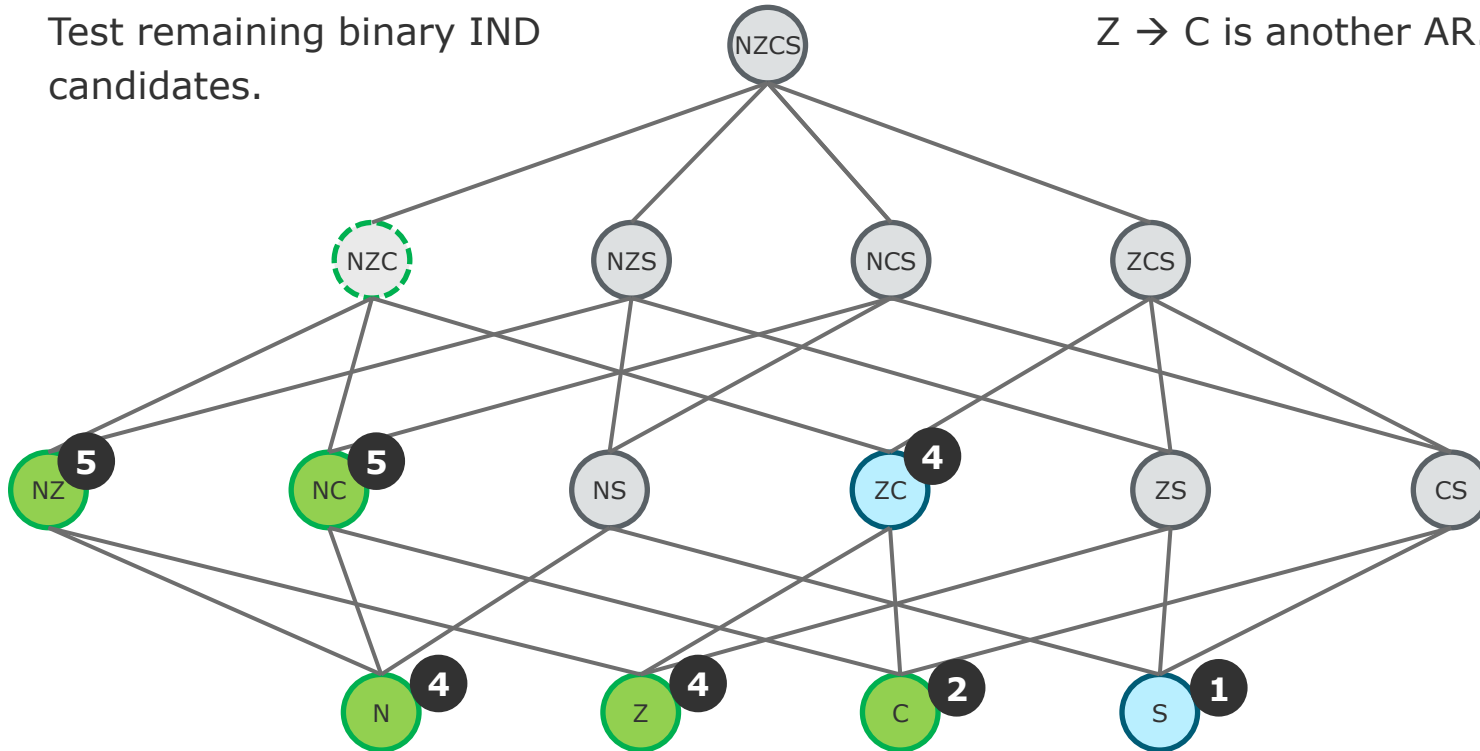
Sebastian Kruse,  
26th June, 2017

Chart 65

# Mixed IND and AR discovery

Test remaining binary IND candidates.

Z → C is another AR.



**Advanced IND detection methods**

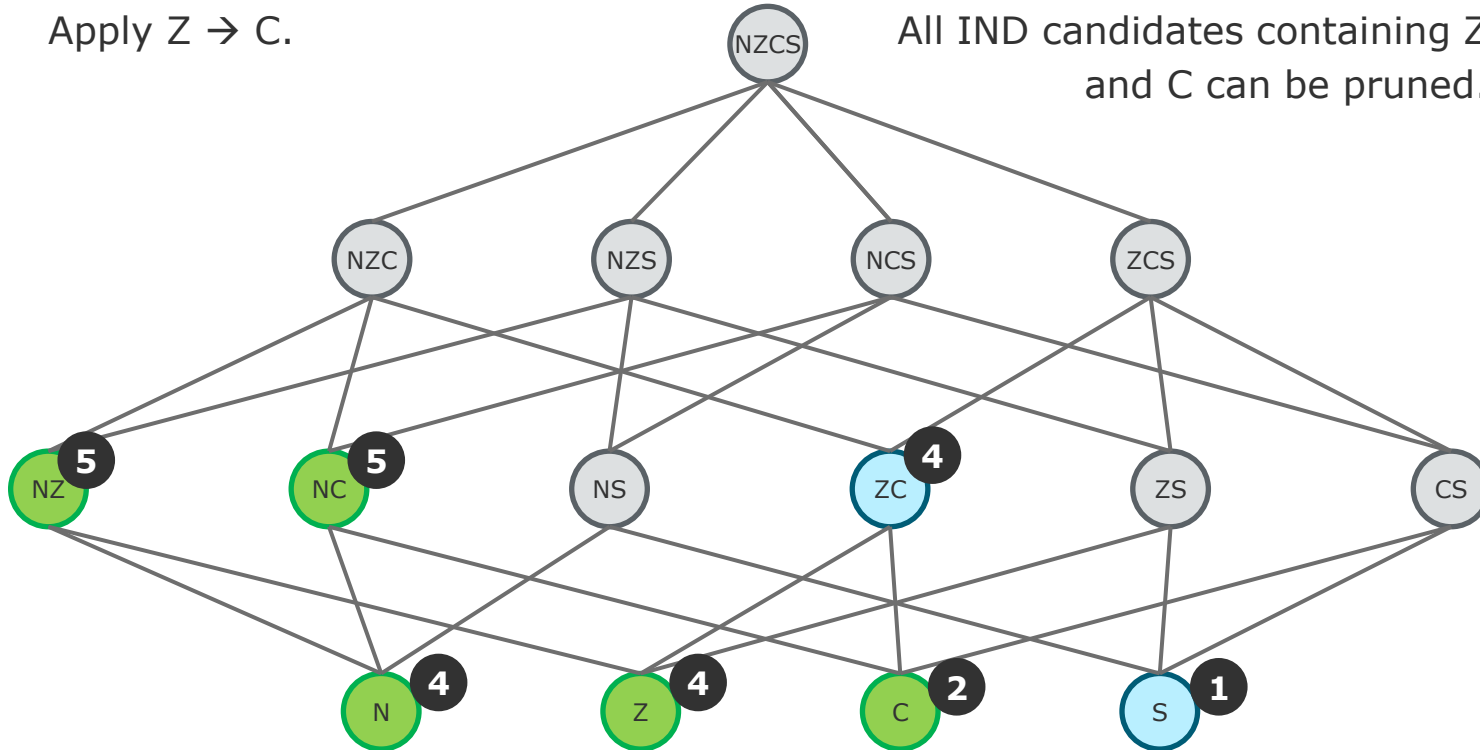
Sebastian Kruse,  
26th June, 2017

Chart 66

# Mixed IND and AR discovery

Apply  $Z \rightarrow C$ .

All IND candidates containing Z and C can be pruned.



**Advanced IND detection methods**

Sebastian Kruse,  
26th June, 2017

Chart 67

# Mixed IND and AR discovery

- Final result:
  - INDs:  $[Name', ZIP'] \subseteq [Name, ZIP], [Name', City'] \subseteq [Name, City]$
  - ARs:  $[ZIP'] \subseteq [ZIP] \rightarrow [City'] \subseteq [City], \{\} \rightarrow [Status'] \subseteq [Status]$
  
- Checked only 3 out of 11 (valid) IND candidates.

Name	Zip	City	Status
Tim	10627	Berlin	Student
Tom	10627	Berlin	Student
Tom	14482	Potsdam	Student
Sandy	10324	Berlin	Student
Inge	14469	Potsdam	Student

**Students**

Name'	Zip'	City'	Status'
Tim	10627	Berlin	Student
Tom	10627	Berlin	Student
Inge	14469	Potsdam	Student

**HPI Students**

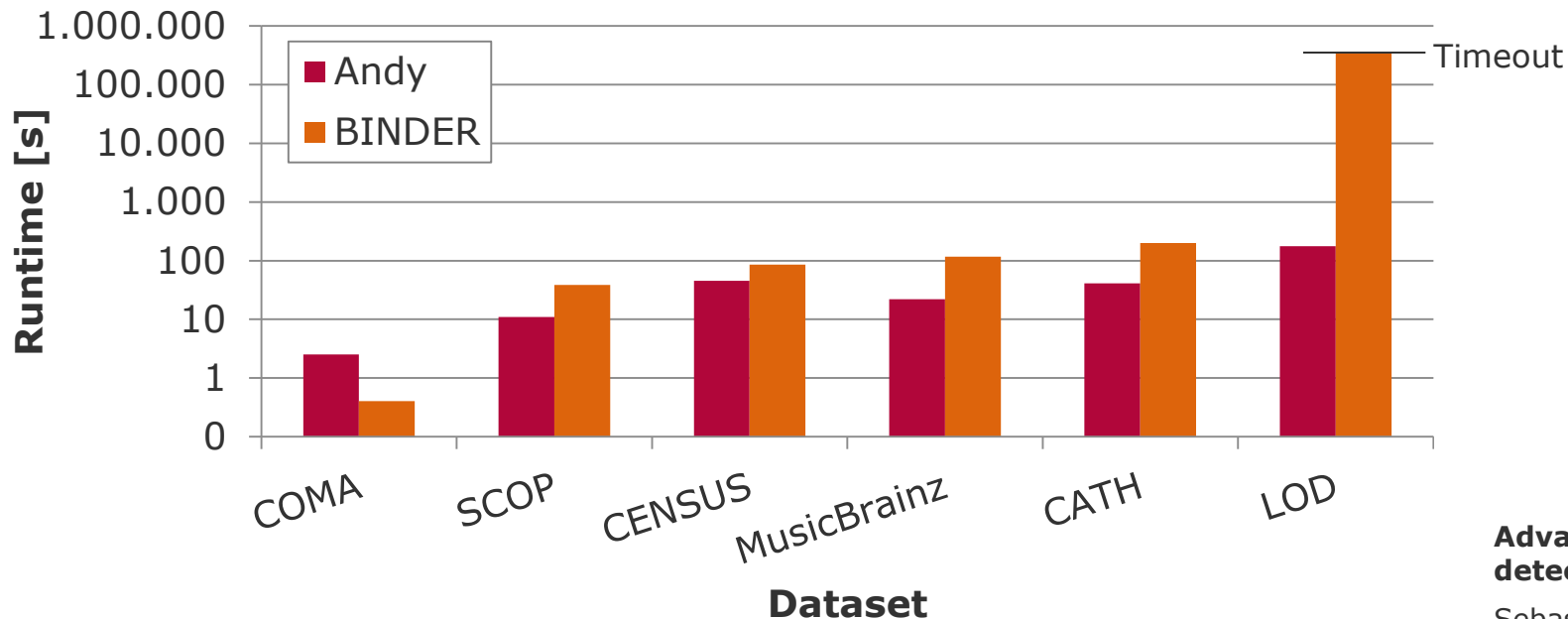
## Advanced IND detection methods

Sebastian Kruse,  
26th June, 2017

Chart **68**

# High-arity INDs - Andy

## Evaluation



- Andy uses SINDY-style candidate checking based on Flink. Both run on a single machine but ANDY uses 2 cores/4 threads.

**Advanced IND detection methods**

Sebastian Kruse,  
26th June, 2017

Chart 69



## Advanced IND detection methods

Sebastian Kruse  
Thorsten Papenbrock

- Papenbrock, T., Kruse, S., Quiané-Ruiz, J. A., & Naumann, F. (2015). Divide & conquer-based inclusion dependency discovery. *Proceedings of the VLDB Endowment*, 8(7), 774-785.
- Kruse, S., Papenbrock, T., & Naumann, F. (2015). Scaling Out the Discovery of Inclusion Dependencies. In *Proceedings of the Conference on Database Systems for Business, Technology, and Web* (pp. 445-454).
- De Marchi, F., & Petit, J. M. (2003). Zigzag: a new algorithm for mining large inclusion dependencies in databases. In *Proceedings of the International Conference on Data Mining* (pp. 27-34).
- Koeller, A., & Rundensteiner, E. A. (2003). Discovery of high-dimensional inclusion dependencies. In *Proceedings of the International Conference on Data Engineering* (pp. 683-685).
- Casanova, M. A., Fagin, R., & Papadimitriou, C. H. (1984). Inclusion dependencies and their interaction with functional dependencies. *Journal of Computer and System Sciences*, 28(1), 29-59.

## Advanced IND detection methods

Sebastian Kruse,  
26th June, 2017

Chart **71**