Window aggregation is a core operation in data stream processing. Existing aggregation techniques focus on reducing latency, eliminating redundant computations, or minimizing memory usage. However, each technique operates under different assumptions with respect to workload characteristics such as properties of aggregation functions (e.g., invertible, associative), window types (e.g., sliding, sessions), windowing measures (e.g., time- or count-based), and stream (dis)order. In this paper, we present Scotty, an efficient and general open-source operator for sliding-window aggregation in stream processing systems, such as Apache Flink, Apache Beam, Apache Samza, Apache Kafka, Apache Spark, and Apache Storm. One can easily extend Scotty with user-defined aggregation functions and window types. Scotty implements the concept of general stream slicing and derives workload characteristics from aggregation queries to improve performance without sacrificing its general applicability. We provide an in-depth view on the algorithms of the general stream slicing approach. Our experiments show that Scotty outperforms alternative solutions by up to one order of magnitude.

CCS Concepts:
- Information systems → Stream management; Data streams; Data streaming; Query operators; Theory of computation → Streaming models.


ACM Reference Format:

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1 Introduction

The need for real-time analysis shifts an increasing number of data analysis tasks from batch to stream processing. To be able to process queries over unbounded data streams, users typically formulate queries that compute aggregates over bounded subsets of a stream, called windows. Examples of such queries on windows are average vehicle speeds per minute, monthly revenue aggregations, or statistics of user behavior for online sessions. The transformation from streams to windows is called stream discretization.

Large computation overlaps caused by sliding windows and multiple concurrent queries lead to redundant computations and inefficiency. Consequently, there is an urgent need for general and efficient window aggregation in industry [11, 56, 72]. In this paper, we contribute a general solution that not only improves performance but also widens the applicability with respect to window types, time domains, aggregate functions, and out-of-order processing. Our solution is generally applicable to all data flow systems that adopt a tuple-at-a-time processing model (e.g., Apache Storm [61], Apache Flink [2, 16], and other Apache Beam-based systems [1, 4]).

To calculate aggregates of overlapping windows, the database community has been working on aggregation techniques such as B-Int [5], Pairs [42], Panes [43], RA [59] and Cutty [17]. These techniques compute partial aggregates for overlapping parts of windows and reuse these partial aggregates to compute final aggregates for overlapping windows. We believe that these techniques are not widely adopted in open-source streaming systems for two main reasons: first, the literature on streaming window aggregation is fragmented and, second, every technique has its own assumptions and limitations. As a consequence, it is not clear for researchers and practitioners under which conditions which streaming window aggregation techniques should be used.

General purpose streaming systems require a window operator that is applicable to many types of aggregation workloads. At the same time, the operator should be as efficient as specialized techniques that support selected workloads only. In order to provide such an operator, we have implemented Scotty. Scotty is available as Open Source Project\(^1\) under the Apache 2.0 license and, right now, provides connectors for Apache Flink [16], Apache Storm [61], Apache Beam [1], Apache Samza [48], Apache Kafka Streams [40], and Apache Spark Continuous Processing [60, 75]. Scotty serves as general operator for many systems and provides extension points to make it easy to add new window types and aggregation functions.

In this paper, we discuss the core concept of Scotty: General Stream Slicing. To this end, we classify existing aggregation techniques with respect to their underlying concepts and their applicability (Section 3). We then identify and define the workload characteristics which may or may not be supported by existing specialized window aggregation techniques (Section 4). Those characteristics are: i) window types (e.g., sliding, session, tumbling), ii) windowing measures (e.g., time or tuple-count), iii) aggregate functions (e.g., associative, holistic), and iv) stream order.

We identify stream slicing as a concept on top of which window aggregation can be implemented efficiently. With Scotty, we contribute a general stream slicing technique (Section 5). Existing slicing-based techniques do not support complex window types such as session windows [42, 43], do not consider out-of-order processing [17], or limit the type of aggregation functions [17, 42, 43]. With Scotty, we provide a single, generally applicable, and highly efficient approach for streaming window aggregation. General stream slicing inherits the performance of specialized techniques that use stream slicing and generalizes stream slicing to support diverse workloads. Because we integrate all workloads into one general solution, we enable aggregate sharing among all queries with different window types (sliding, sessions, user-defined, etc.) and window measures (e.g., tuple-count or time).

\(^1\)Open-Source-Repository: https://github.com/TU-Berlin-DIMA/scotty-window-processor
Scotty breaks down slicing into three operations on slices, namely merge, split, and update. Specific workload characteristics influence the cost of each operation and how often operations are performed. By taking into account the workload characteristics, our slicing technique i) stores the tuples themselves only when it is required, which saves memory and ii) minimizes the number of slices that are created, stored, and recomputed. One can extend Scotty with additional aggregations and window types without changing the three core slicing operations. Thus, these core operations may be tuned by system experts while users can still implement custom windows and aggregations.

This paper is an extended version of two earlier publications presented at EDBT [65] and ICDE [64]. We integrate both publication into one consistent manuscript and make the following new contributions: We focus on the progress made in the open-source Scotty project and provide more detailed explanations and additional insights. We also add the new Sections 7, 8, and 9. Sections 7 and 8 provide an in-depth discussion and formal specification of the algorithms used in Scotty. Section 9 shows examples that illustrate how to use Scotty in different stream processing systems and how to extend Scotty with new aggregation functions and window types.

The remainder of this paper is structured as follows:

- We define terminology with respect to window types, stream order, timing, and data expiration, which we use throughout the paper (Section 2).
- We survey different window aggregation concepts and identify their limitations with respect to different workloads (Section 3).
- We identify the workload characteristics that impact the applicability and performance limitations of existing aggregation techniques (Section 4).
- We contribute general stream slicing, a generally applicable and highly efficient solution for streaming window aggregation in dataflow systems (Section 5).
- We take a close look on session windows and show how concurrent queries using session windows can benefit from general stream slicing (Section 6).
- We present the algorithms and optimizations used in the two main components of of Scotty, namely the Stream Slicer (Section 7) and the Slice Manager (Section 8).
- We show several examples that illustrate how one can use Scotty in different stream processing systems and how one can extend Scotty with new aggregation functions and window types (Section 9).
- We evaluate the performance implications of different workload characteristics and show that general stream slicing is generally applicable while offering better performance than existing approaches (Section 10).

2 Preliminaries

Streaming window aggregation involves special terminology with respect to window types, timing, stream order, and data expiration. This section revisits terms and definitions that are required for the remainder of this paper.

Window Types. A window type refers to the logic based on which systems derive finite windows from a continuous stream (stream discretization). There exist diverse window types ranging from common sliding windows to more complex data-driven windows [24]. We address the diversity of window types with a classification in Section 4.4. For now, we limit the discussion to tumbling (or fixed), sliding, and session windows (Figure 1) which we use in subsequent examples.

A tumbling window splits the time into segments of equal length \( l \). The end of one window marks the beginning of the next window. Sliding windows, in addition to the length \( l \), also define a slide step of length \( s \). This length determines how often a new window starts. Consecutive
windows overlap when \( l_s < l \). In this case, tuples may belong to multiple windows. A session window typically covers a period of activity followed by a period of inactivity [1]. Thus, a session window times out (ends) if no tuple arrives for some time gap \( l_s \). Typical examples of sessions are taxi trips, browser sessions, and ATM interactions.

**Notion of Time.** One can define windows on different measures such as times and tuple-counts. The event-time of a tuple is the time when an event was captured and the processing-time is the time when an operator processes a tuple [1, 16]. Technically, an event-time is a timestamp stored in the tuple and processing-time refers to a system clock. If not indicated otherwise, we refer to event-time windows in our examples because applications typically define windows on event-time.

**Stream Order.** Input tuples of a stream are in-order if they arrive chronologically with respect to their event-times, otherwise, they are out-of-order [1, 46]. In practice, streams regularly contain out-of-order tuples because of transmission latencies, network failures, or temporary sensor outages. We differentiate in-order tuples from out-of-order tuples and in-order streams from out-of-order streams. Let a stream \( S \) consist of tuples \( s_1, s_2, s_3, \ldots \) where the subscripts denote the order in which an operator processes the tuples. Let the event-time of any tuple \( s_x \) be \( t_e(s_x) \).

- A tuple \( s_x \) is in-order if \( \forall y : t_e(s_y) > t_e(s_x) \land y < x \).
- A stream is in-order iff all its tuples are in-order tuples.

**Punctuations, Watermarks, and Allowed Lateness.** Punctuations are annotations embedded in a data stream [68]. Systems use punctuations for different purposes: low-watermarks (in short watermarks) indicate that no tuple will arrive with a timestamp smaller than the watermark’s timestamp [1]. Many systems use watermarks to control how long they wait for out-of-order tuples before they output a window aggregate [4]. Window punctuations mark window starts and endings in the stream [21, 30]. The allowed lateness, specifies how long systems store window aggregates. If an out-of-order tuple arrives after the watermark, but in the allowed lateness, we output updated aggregates.

**Partial Aggregates and Aggregate Sharing.** The key idea of partial aggregation is to compute aggregates for subsets of the stream as intermediate results. These intermediate results are shared among overlapping windows to prevent repeated computation [5, 42, 73]. In addition, one can compute partial aggregates incrementally when tuples arrive [59]. This reduces the memory footprint if a technique stores few partial aggregates instead of all stream tuples in the allowed lateness. It also reduces the latency because aggregates are pre-computed when windows end. We say that a window ends when the systems has to output the aggregate for a window. When processing in-order streams, a window ends as soon as the time progresses beyond the end-timestamp of the window. When processing out-of-order streams, a window ends as soon as the watermark progresses beyond the end-timestamp of the window.
### 3 Window Aggregation Concepts

In this section, we survey concepts for streaming window aggregation and give an intuition for each solution’s memory usage, throughput, and latency. We provide a detailed comparison of all concepts in our experiments. Techniques which support out-of-order streams store values for an *allowed lateness* (see above). In the following discussion, we refer to allowed lateness only. Techniques that do not process out-of-order tuples, store values for the duration of the longest window. All presented concepts process a single input stream. However, one can merge (join) two or more data streams in a preceding operator and apply windowing on the merged stream. If windows depend on the stream from which a tuple originates, one can label tuples when merging streams.

Table 1 provides an overview of all techniques we discuss in the following subsections. We denote the number of values (i.e., tuples) as $|\triangledown|$, the number of slices as $|\triangledown|$, and the number of

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Legend: $\blacktriangle$ Tuple, $\blacklozenge$ Aggregate, $\triangledown$ Slice with Aggregate, $\square$ Bucket

Table 1. Memory Usage and Visualization of Aggregation Techniques.
3.1 Tuple Buffer
A tuple buffer (Table 1, Row 1) is a straightforward solution, which does not share partial aggregates. The throughput of a tuple buffer is fair as long as there are few or no concurrent windows (i.e., no window overlaps), and there are few or no out-of-order tuples. Window overlaps decrease the throughput because of repeated aggregate computations. Out-of-order tuples decrease the throughput because of memory copy operations that are required for inserting values in the middle of a sorted ring buffer. The latency of a tuple buffer is high because aggregates are computed lazily. Thus, all aggregate computations contribute to the latency when the window ends.

A tuple buffer stores all tuples for the allowed lateness, which is $|\text{win}| \cdot \text{size(\text{\square})}$. Thus, the more tuples we process per time, the higher the memory consumption and the higher the memory copy overhead for out-of-order tuples.

3.2 Aggregate Trees
Aggregate trees such as FlatFAT [59] and B-INT [5] store partial aggregates in a tree structure and share them among overlapping windows (Table 1, Row 2). FlatFAT stores a binary tree of partial aggregates on top of stream tuples (leaves) which roughly doubles the memory consumption. In-order tuples require $\log(|\text{\square}|)$ updates of partial aggregates in the tree. Thus, the throughput decreases logarithmically when the number of tuples in the allowed lateness increases. Out-of-order tuples decrease the throughput drastically: they require the same memory copy operation as in tuple buffers. In addition, they cause a rebalancing of the aggregate tree and the respective aggregate updates. The latency of aggregate trees is much lower than for tuple buffers because they can compute final aggregates for windows from pre-computed partial aggregates. Thus, only a few final aggregation steps remain when windows end [54].

3.3 Buckets
Li et al. introduce Window-ID (WID) [44–46], a bucket-per-window approach which is adopted by many systems with support for out-of-order processing [1, 4, 16]. Each window is represented by an independent bucket. A system assigns tuples to buckets (i.e., windows) based on event-times, independently from the order in which tuples arrive [46]. Buckets do not utilize aggregate sharing. Instead, they compute aggregates for each bucket independently. Systems can compute aggregates for buckets incrementally [59]. This leads to very low latencies because the final window aggregate is pre-computed when windows end.

We consider two versions of buckets. Tuple buckets keep individual tuples in buckets (Table 1, Row 4). This leads to data replication for overlapping buckets. Aggregate buckets store partial aggregates in buckets plus some overhead (e.g., start and end times), but no tuples (Table 1, Row 3). We prefer to store aggregates instead of individual tuples to reduce the memory footprint. However, some use-cases (e.g., holistic aggregates over count-based windows) require us to keep individual tuples in memory. Buckets process in-order tuples as fast as out-of-order tuples for most use-cases: they assign the tuple to buckets and incrementally compute the aggregate of these buckets. The throughput bottleneck for buckets are overlapping windows. For example, one sliding window with $l = 20s$ and $l_s = 2s$ results in 10 overlapping windows (i.e., buckets) at any time. This causes 10 aggregation operations for each input tuple.
3.4 Stream Slicing

Slicing techniques divide (i.e., slice) a data stream into non-overlapping chunks of data (i.e., slices) \[42, 43\]. The system computes a partial aggregate for each slice. When windows end, the system computes window aggregates from slices.

We show stream slicing with an example in Figure 2. Slicing techniques compute partial aggregates incrementally when tuples arrive (bottom of Figure 2). We show multiple intermediate aggregates per slice to illustrate the workflow. Partial aggregates (i.e., slices) are shared among overlapping windows which avoids redundant computations. In Figure 2, dashed arrows mark multiple uses of slices. In contrast to aggregate trees and buckets, slicing techniques require just one aggregation operation per tuple because each tuple belongs to exactly one slice. This results in a high throughput for in-order as well as out-of-order tuples.

Similar to aggregate trees, the latency of stream slicing techniques is low because only a few final aggregation steps are required when a window ends. We consider a lazy and an eager version of stream slicing. The lazy version of stream slicing stores slices including partial aggregates (Table 1, Row 5). The eager version stores a tree of partial aggregates on top of slices to further reduce latencies (Table 1, Row 6). Both variants compute aggregates of slices incrementally when tuples arrive. The term lazy refers to the lazy computation of aggregates for combinations of slices.

There are usually many tuples per slice (\(|\pi| \ll |\Delta|\)) which leads to huge memory savings compared to aggregate trees and tuple buffers. Some use-cases such as holistic aggregates over count-based windows require us to keep individual tuples in addition to aggregates (Table 1, Row 7 and 8). In these cases, stream slicing requires more memory than tuple buffers, but saves memory compared to buckets and aggregate trees.

We focus on stream slicing because it offers a good combination of high throughputs, low latencies, and memory savings. Moreover, our experiments show that slicing techniques scale to many concurrent windows, high ingestion rates, and high fractions of out-of-order tuples. We create slices such that they can be shared among all queries.

4 Workload Characterization

In this section, we identify workload characteristics that either limit the applicability of aggregation techniques or impact their performance. These characteristics are the basis for subsequent sections in which we generalize stream slicing.

4.1 Characteristic 1: Stream Order

Out-of-order streams increase the complexity of window aggregation, because out-of-order tuples can require changes in the past. For example, tuple buffers and aggregate trees process in-order tuples efficiently using a ring buffer (FIFO principle) \[59\]. Out-of-order tuples break the FIFO principle and require memory copy operations in buffers.

We differentiate whether or not out-of-order processing is required for a use-case. For techniques that support out-of-order processing, we study how the fraction of out-of-order tuples and the delay of such tuples affect the performance.
4.2 Characteristic 2: Aggregation Function

We classify aggregation functions with respect to their algebraic properties. Our notation splits the aggregation in incremental steps and is consistent with related works [17, 59]. We write input values as lower case letters, the operation that adds a value to an aggregate as $\oplus$, and the operation that removes a value from an aggregate as $\ominus$. E.g., if we compute a sum, $\oplus$ corresponds to the arithmetic $+$ and $\ominus$ corresponds to the arithmetic $-$. We first adopt three algebraic properties used by Tangwongsan et al. [59]. These properties focus on the incremental computation of aggregates:

1. Associativity: $(x \oplus y) \oplus z = x \oplus (y \oplus z) \forall x, y, z$
2. Invertibility: $(x \oplus y) \ominus y = x \forall x, y$
3. Commutativity: $x \oplus y = y \oplus x \forall x, y$

Stream slicing requires associative aggregate functions because it computes partial aggregates per slice which are shared among windows. This requirement is inherent for all techniques that share partial aggregates [5, 17, 42, 43, 59]. Our general slicing approach does not require invertibility or commutativity, but exploits these properties if possible to increase performance.

We further adopt the classification of aggregations in distributive, algebraic, and holistic [23]. Aggregations such as sum, min, and max are distributive. Their partial aggregates equal the final aggregates of partials and have a constant size. An aggregation is algebraic if its partial aggregates can be summarized in an intermediate result of fixed size. The final aggregate is computed from this intermediate result. For example, an average is algebraic because average = sum/count and partial aggregates can be represented by a tuple $\langle$sum, count$\rangle$. The remainder of aggregations, which have an unbounded size of partial aggregates, is holistic. An example are quantiles (e.g., the median) that require to store all input values as part of the intermediate result. General stream slicing is beneficial for distributive, algebraic, and many holistic aggregations.

4.3 Characteristic 3: Windowing Measure

Windows can be specified using different measures (also called time domains [12] or WATTR [44]). For example, a tumbling window can have a length of 5 minutes (time-measure), or a length of 10 tuples (count-measure). To simplify the presentation, we refer to timestamps in the rest of this paper. However, bear in mind that a timestamp can actually be a time, a tuple count, or any other monotonically increasing measure [17]:

- **Time-Based Measures**: Common time-based measures are event-time and processing-time as introduced in Section 2.
- **Arbitrary Advancing Measures** are a generalization of event-times. Typically, it is irrelevant for a stream processor if "timestamps" actually represent a time or another advancing measure. Examples of other advancing measures are transaction counters in a database, kilometers driven by a car, and invoice numbers.
- **Count-Based Measures** (also called tuple-based [44] or tuple-driven [12]) refer to a tuple counter. For example, a window can start at the 100th and end at the 200th tuple of a stream. Count-based measures cause challenges when combined with out-of-order processing: If tuples are ordered with respect to their event-times and a tuple arrives out-of-order, it changes the count of all other tuples that have a greater event-time. This changes the aggregates of all count-based windows that start or end after the out-of-order tuple.

If we process multiple queries that use different window-measures, timestamps are represented as vectors which contain multiple measures as dimensions. This representations allows for slicing the stream with respect to multiple dimensions (i.e., measures) while slices are still shared among all queries [13, 17].
4.4 Characteristic 4: Window Type

We classify window types with respect to the context (or state) which is required to know where windows start and end. We adopt the classification in context free (CF), forward-context aware (FCA), and forward-context free (FCF) introduced by Li et al. [44]. Here we present those classes along with the most common window types belonging to them.

- **Context Free (CF)**. A window type is context free if one can tell all start and end timestamps of windows without processing any tuples. Common sliding and tumbling windows are context free because we can compute all start and end timestamps a priori based on the parameters $l$ and $l_s$.

- **Forward Context Free (FCF)**. Windows are forward context free, if one can tell all start and end timestamps of windows up to any timestamp $t$, once all tuples up to this timestamp have been processed. An example are punctuation-based windows where punctuations mark start and end timestamps [21]. Once we processed all tuples up to $t$ (including out-of-order tuples), we also processed all punctuations before $t$ and, thus, we know all start and end positions up to $t$.

- **Forward Context Aware (FCA)**. The remaining window types are forward context aware. Such window types require us to process tuples after a timestamp $t$ in order to know all window start and end timestamps before $t$. An example of such windows are Multi-Measure Windows that define their start and end timestamps on different measures. For example, output the last 10 tuples (count-measure) every 5 seconds (time-measure) is forward context aware: we need to process tuples up to a window end in order to compute the window begin.

5 General Stream Slicing

We now present our general stream slicing technique that supports high-performance aggregation for multiple queries with diverse workload characteristics. General stream slicing replaces alternative operators for window aggregation without changing their input or output semantics. Our technique minimizes the number of partial aggregates (saving memory), reduces the final aggregation steps when windows end (reducing latency), and avoids redundant computation for overlapping windows (increasing throughput). The main idea behind our technique is to exploit workload characteristics (Section 4) and to automatically adapt aggregation strategies. Such adaptivity is a highly desired feature of an aggregation framework: current non-adaptive techniques fail to support multiple window types, process in-order streams only, cannot share aggregates among windows defined on different measures, lack support for holistic aggregations, or incur dramatically reduced performance in exchange for being generally applicable.

**Approach Overview.** Figure 3 depicts an overview of our general slicing and aggregation technique. Users specify their queries in a high-level language, such as a flavor of stream SQL or a functional API. The query translator observes the characteristics of a query (i.e., window type, aggregate...
function, and window measure) as well as the characteristics of input streams (in-order vs. out-of-order streams) and forwards them to our aggregator. Once those characteristics are given to our aggregator, our general slicing technique adapts automatically to the given workload characteristics. More specifically, general slicing detects if individual tuples need to be kept in memory (to ensure generality) or if they can be dropped after computing partial aggregates (to improve performance). We further discuss this in Section 5.1. Moreover, the stream slicing component automatically decides when it needs to apply our three fundamental slicing operations: merge, split, and update (discussed in Section 5.2). Queries can be added or removed from the aggregator and due to that, the workload characteristics can change. To this end, our aggregator adapts on the fly. In Section 5.3, we discuss the workflow for processing input tuples and introduce the required software components. General slicing has extension points that can be used to implement user-defined window types and aggregations (discussed in Section 5.4).

We structure the following sections such that we start from an abstract presentation of the concept and continue towards in-depth explanations of each component. Thus, Section 5 presents the concept of general stream slicing. Section 6 discusses how general stream slicing works with forward context aware windows on the example of session windows. The following Sections 7 and 8 then present the involved algorithms in detail, before Section 9 shows programming examples.

### 5.1 Storing Tuples vs. Partial Aggregates

Existing aggregation techniques achieve generality by storing all input tuples and by computing high-level partial aggregates [5, 59]. Specialized techniques, on the other hand, only store (partial) aggregates. A general slicing technique needs to decide when to store what, according to workload characteristics of each of the queries that it serves. In this section, we discuss how we match the performance of specialized techniques, by choosing on-the-fly whether to keep tuples or to store partial aggregates only.

For example, consider an aggregation function that is non-commutative ($\exists x, y : x \oplus y \neq y \oplus x$) defined over an unordered stream. When an out-of-order tuple arrives, we need to recompute aggregates from the source tuples, in order to retain the correct order of the aggregation. Thus, one would have to store the actual tuples for possible later use. Storing all tuples for the whole duration of the allowed lateness requires more memory, but allows for computing arbitrary windows from stored tuples. The decision tree in Figure 4 summarizes when storing source tuples is required depending on different workload characteristics.
**In-order Streams.** For in-order streams, we drop tuples for all context free (CF) and forward context free (FCF) windows but must keep tuples if we process forward context aware (FCA) windows. For such windows, forward context leads to additional window start or end timestamps. Thus, we must be able to compute partial aggregates for arbitrary timestamp ranges from the originally stored tuples.

**Out-of-order Streams.** For out-of-order streams, we need to keep tuples if at least one of the following conditions is true:

1. **The aggregation function is non-commutative.**
   An out-of-order tuple changes the order of the incremental aggregation, which forces us to recompute the aggregate using source tuples. For in-order processing, the commutativity of aggregation functions is irrelevant, because tuples are always aggregated in-order. Thus, there is no need to store source tuples in addition to partial aggregates.

2. **The window is neither context free nor a session window.**
   In combination with out-of-order tuples, all context aware windows require tuples to be stored. This is because out-of-order tuples change backward context, which can lead to additional window start or end timestamps. Such additional start and end timestamps require to split slices and to recompute the respective partial aggregates from the original tuples. Session windows are an exception, because they are context aware, but never require recomputing aggregates, as we will show in Section 6.

3. **The query uses a count-based window measure.**
   An out-of-order tuple (see definition in Section 2) changes the count of all succeeding tuples. Thus, the last tuple of each window shifts to its succeeding window.

### 5.2 Slice Management

Stream slicing is the fundamental concept that allows us to build partial aggregates and share them among concurrently running queries and overlapping windows. In this section, we introduce three fundamental operations which we can perform on slices.

**Slice Metadata.** A slice stores its start timestamp ($t_{\text{start}}$), its end timestamp ($t_{\text{end}}$), and the timestamp of the first ($t_{\text{first}}$) and last tuple it contains ($t_{\text{last}}$). Note that the timestamps of the first and last tuples do not need to coincide with the start and end timestamps of a slice. For instance, consider a slice $A$ that starts at $t_{\text{start}}(A) = 1$ and ends at $t_{\text{end}}(A) = 10$, but the first (earliest) tuple contained is timestamped as $t_{\text{first}}(A) = 2$ and its last/latest one as $t_{\text{last}}(A) = 9$. Note that the *timestamp* can refer not only to actual time, but to any measure presented in Section 4.3.

We identify three fundamental operations which we perform on stream slices. These operations are i) **merging** of two slices into one, ii) **splitting** one slice into two, and iii) **updating** the state of a slice (i.e., aggregate and metadata updates). In the following paragraphs, we discuss merge, split, and update as well as the impact of our workload characteristics on each operation. We use uppercase letters to name slices and corresponding lower case letters for slice aggregates.

**Merge.** Merging two slices $A$ and $B$ happens in three steps:

1. Update the end of $A$ such that $t_{\text{end}}(A) \leftarrow t_{\text{end}}(B)$.
2. Update the aggregate of $A$ such that $a \leftarrow a \oplus b$.
3. Delete slice $B$, which is now merged into $A$.

Steps one and three have a constant computational cost. The complexity of the second step ($a \leftarrow a \oplus b$) depends on the type of aggregate function. For instance, the cost is constant for algebraic and distributive functions such as $\text{sum}$, $\text{min}$, and $\text{avg}$ because they require just a few basic arithmetic operations. Holistic functions such as quantiles can be more complex to compute. Except from the...
type of aggregation function, no other workload characteristics impact the complexity of the merge operation. However, stream order and window types influence when and how often we merge slices. We discuss this influence in Section 5.3.

**Split.** Splitting a slice $A$ at timestamp $t$ requires three steps:

1. Add slice $B$: $t_{\text{start}}(B) \leftarrow t + 1$ and $t_{\text{end}}(B) \leftarrow t_{\text{end}}(A)$.
2. Update the end of $A$ such that $t_{\text{end}}(A) \leftarrow t$.
3. Recompute the aggregates of $A$ and $B$.

Note that splitting slices is an expensive operation because it requires recomputing slice aggregates from scratch. Moreover, if splitting is required, we need to keep individual tuples in memory to enable the recomputation.

We show in Figure 5 when split operations are required. For in-order streams, only forward context aware (FCA) windows require split operations. For such windows, we split slices according to a window’s start and end timestamp as soon as we process the required forward context. In out-of-order data streams, all context aware windows can require split operations because out-of-order tuples contain backward context. We never split slices for context free windows such as tumbling and sliding ones.

**Update.** Updating a slice can involve adding in-order tuples, adding out-of-order tuples, removing tuples, or changing metadata ($t_{\text{start}}$, $t_{\text{end}}$, $t_{\text{first}}$, and $t_{\text{last}}$).

Metadata changes are simple assignments of new values to the existing variables. Adding a tuple to a slice requires one incremental aggregation step ($\oplus$), with the exception of processing out-of-order tuples with a non-commutative aggregation function. For this, we recompute the aggregate of the slice from scratch to retain the order of aggregation steps.

For some workloads we need to remove tuples from slices. Figure 6 depicts when and how we remove tuples from slices. Generally, a remove operation is required only if a window is defined on a count-based measure and if we process out-of-order tuples. An out-of-order tuple changes the count of all succeeding tuples. This requires us to shift the last tuple of each slice one slice further, starting at the slice of the out-of-order tuple. If the aggregation function is invertible, we exploit this property by performing an incremental update. Otherwise, we have to recomputed the slice aggregate from scratch. If the out-of-order tuple has a small delay, such that it still belongs to the latest slice, we can simply add the tuple without performing a remove operation.
5.3 Processing Input Tuples

The stream slicing and aggregation logic (bottom of Figure 3) consists of four components, which we show in Figure 7. The Aggregate Store is our shared data structure, which is accessed by the Stream Slicer to create new slices, by the Slice Manager to update slices, and by the Window Manager to compute window aggregates.

The input stream can contain in-order tuples, out-of-order tuples, and watermarks. Note that in-order tuples can either arrive from an in-order stream (i.e., one that is guaranteed to never contain an out-of-order tuple) or from an out-of-order stream (i.e., one that does not guarantee in-order arrival). If the stream is in-order (i.e., all tuples are in-order tuples), there is no need to ingest watermarks. Instead, we output windows directly, since there is no need to wait for potentially delayed tuples.

Step 1 - The Stream Slicer. The Stream Slicer initializes new slices on-the-fly when in-order tuples arrive [42]. In an in-order stream, it is sufficient to start slices when windows start [17]. In an out-of-order stream, we also need to start slices when windows end, to allow for updating the last slice of windows later on with out-of-order tuples. We call the beginnings and endings of windows window edges and the beginnings and endings of slices slice edges. We always keep the timestamp of the next upcoming window edge in memory and compare in-order tuples with this timestamp. As soon as the timestamp of a tuple exceeds the stored timestamp, we start a new slice and save the timestamp of the next edge. This is highly efficient because the majority of tuples do not end a slice and require just one comparison of timestamps.

The Stream Slicer does not process out-of-order tuples and watermarks but forwards them directly to the Slice Manager. This is possible because the slices for out-of-order tuples have already been initialized by previous in-order tuples.

Step 2 - The Slice Manager. The Slice Manager is responsible for triggering all split, merge, and update operations on slices.

First, the Slice Manager checks whether a merge or split operation is required. We always merge and split slices such that all slice edges match window edges and vice versa. This guarantees that we maintain the minimum possible number of slices [13, 17, 64].

In an out-of-order stream, context aware windows can cause merges or splits. In an in-order stream, only forward context aware windows can cause these operations. Context free windows never require merge or split operations, as the window edges are known in advance and slices never need to change.

In-order tuples can be part of the forward context that indicates window start or end timestamps earlier in the stream. When processing forward context aware windows, we check if the new tuple changes the context such that it introduces or removes window start or end timestamps. In such case, we perform the required merge and split operation to match the new slice and window edges. Out-of-order tuples can change forward and backward context, such that a merge operation or split operation are required.
If the new context causes new window edges and, thus, merge or split operations, we notify the Window Manager, which outputs window aggregates up to the current watermark.

Finally, the Slice Manager adds the new tuple to its slice and updates the slice aggregate accordingly. In-order tuples always belong to the current slice and are added with an incremental aggregate update [59]. For out-of-order tuples, we look up the slice that covers the timestamp of the out-of-order tuple and add the tuple to this slice. For commutative aggregation functions, we add the new tuple with an incremental aggregate update. For non-commutative aggregation functions, we need to recompute the aggregate from individual tuples to retain the correct order.

**Step 3 - The Window Manager.** The Window Manager computes the final aggregates for windows from slice aggregates.

When processing an in-order stream, the Window Manager checks if the tuple it processes is the last tuple of a window. Therefore, each tuple can be seen as a watermark which has the timestamp of the tuple. If a window ended, the window manager computes and outputs the window aggregate (final aggregation step).

For out-of-order streams, we wait for the watermark (see Section 2) before we output results of windows that ended before a watermark.

The Slice Manager notifies the Windows Manager when it performs split, merge, or update operation on slices. Upon such notification, the Window Manager performs two operations:

1. If an out-of-order tuple arrives within the allowed lateness but after the watermark, the tuple possibly changes aggregates of windows that were output before. Thus, the Window Manager outputs updates for these window aggregates.
2. If a tuple changes the context of context aware windows such that new windows end before the current watermark, the window manager computes and outputs the respective aggregates.

**Parallelization.** We parallelize stream processing with key partitioning, which is the common approach used in stream processing systems [32] such as Flink [16], Spark [6], and Storm [61]. Key partitioning enables intra-node as well as inter-node parallelism and, thus, results in good scalability. Since our generic window aggregation is a drop in replacement for the window aggregation operator, the input and output semantics of the operator remains unchanged. Thus, neither the query interface nor optimizations unrelated to window aggregations are affected.

### 5.4 User-Defined Windows and Aggregations

Our architecture decouples the general logic of stream slicing from the concrete implementation of window types and aggregation functions. This makes it easy to add window types and aggregation functions, as no changes are required in the slicing logic. In this section, we describe how we implement aggregation functions and window types.

#### 5.4.1 Implementing Aggregation Functions

We adopt the same approach of incremental aggregation introduced by Tangwongsan et al. [59]. Each aggregation type consists of three functions: lift, combine, and lower. In addition, aggregations may implement an invert function. We now discuss the concept behind these functions, and refer the reader to the original paper for an overview of different aggregations and their implementation.

**Lift.** The lift function transforms a tuple to a partial aggregate. For example, consider an average computation. If a tuple \( \langle t, v \rangle \) contains its timestamp \( t \) and a value \( v \), the lift function will transform it to \( (\text{sum} \leftarrow v, \text{count} \leftarrow 1) \), which is the partial aggregate of that one tuple.

**Combine.** The combine function \( (\oplus) \) computes the combined aggregate from partial aggregates. Each incremental aggregation step results in one call of the combine function.
Lower. The lower function transforms a partial aggregate to a final aggregate. In our example, the lower function computes the average from sum and count: \( \langle \text{sum}, \text{count} \rangle \mapsto \text{sum}/\text{count} \).

Invert. The optional invert function removes one partial aggregate from another with an incremental operation.

In this work, we consider holistic aggregation functions, which have an unbounded size of partial aggregates. A widely used holistic function is the computation of quantiles. For instance, windowed quantiles are the basis for billing models of content delivery networks and transit-ISPs [20, 33]. For quantile computations, we sort tuples in slices to speed up succeeding merge operations and apply run length encoding to save memory [52].

5.4.2 Implementing Different Window Types We use a common interface for the in-order slicing logic of all windows. We extend this interface with additional methods for context-aware windows. One can add additional window types by implementing the respective interface.

Context Free Windows. The slicing logic for context free windows depends on in-order tuples only. When a tuple is processed, the slicing core initializes all slices up to the timestamp of that tuple. Our interface for context free windows has two methods: The first method has the following signature:

\[
\text{long getNextEdge(long timestamp)}
\]

The method receives a timestamp as parameter and returns the next window edge (begin or end timestamp) after this timestamp. We use this method to retrieve the next window edge for on-the-fly stream slicing (Step 1 in subsection 5.3). For example, a tumbling window with length \( l \) would return \( \text{timestamp} + l - (\text{timestamp} \mod l) \).

The second method triggers the final window aggregation according to a watermark and has the following signature:

\[
\text{void triggerWin(Callback c, long prevWM, long currWM)}
\]

The Window Manager calls this method when it processes a watermark. \( c \) is a callback object, \( \text{prevWM} \) is the timestamp of the previous watermark and \( \text{currWM} \) is the timestamp of the current watermark. The method reports all windows that ended between \( \text{prevWM} \) and \( \text{currWM} \) by calling \( c.\text{triggerWin(long startTime, long endTime)} \).

This callback to the Window Manager triggers the computation and output of the final window aggregate.

Context Aware Windows. Context aware windows use the same interface as context free windows to trigger the initialization of slices when processing in-order tuples. In addition, context aware windows require to keep a state (i.e., context) in order to derive window start and end timestamps when processing out-of-order tuples. We initialize context aware windows with a pointer to the Aggregate Store. This prevents redundancies among the state of the shared aggregator and the window state. When the Slice Manager processes a tuple, it notifies context aware windows by calling

\[
\text{window.notifyContext(callbackObj, tuple)}
\]

This method can then add and remove window start and end timestamps through the callback object and the Slice Manager splits and merges slices as required to match window start and end timestamps. We detect whether or not a window is context aware based on the interface that is implemented by the window specification.
6 Stream Slicing for Session Windows

Recently, session windows evolved to a common window type supported by programming models such as Apache Beam [4] and the Dataflow Model [1]. Many systems implement these models and process session windows in addition to sliding and tumbling windows [3, 17, 75]. In this section, we take a close look on session windows and show that session window aggregation benefits from stream slicing. In the remainder of the paper, we use session windows as one example of a context aware window type.

6.1 Aggregate Sharing for Session Windows

We show an example for session window stream slicing in Figure 8. The example has four session windows with the minimum gaps $l_g = 3, 5, 6, 7$. We make five observations based on our example:

1. Multiple session window queries with different gaps can share slices and, thus, partial aggregates.
2. Session windows would also share slices with other types of windows.
3. Sessions of a single query have no overlap. Thus, a single session window query cannot benefit from aggregate sharing.
4. Slices can cover the gaps between sessions because gaps do not cover any tuples by definition. Respectively, a partial aggregate that covers a session and a gap is equal to an aggregate that covers the session only.
5. The slicing logic solely depends on one session window - the one with the smallest gap. All session windows with larger gaps are compositions of the slices made for the session window with the smallest minimum gap. In our example $\min(l_g) = 3$.

We utilize the observations above and create slices with respect to the session window with the smallest gap only. This allows for creating stream slices with a constant workload, which is independent from the number concurrent sessions.

6.2 Session Windows on Out-Of-Order Streams

Stream slicing for session windows is more complex than for sliding or tumbling windows, because session windows are context aware. Thus, we do not know start and end positions of sessions up front. Instead, start and end positions of sessions depend on the gaps between the tuples we process.

Out-of-order tuples either belong to an existing session (update), fuse sessions (merge), or form new sessions (split). We show all cases in Figure 9. Interestingly, we can rewrite all required split operations to update operations. Thus, we completely prevent expensive slice splits and do not need to store tuples in additions to aggregates when processing session windows.
If an out-of-order tuple belongs to an existing session (Case 1.1) or extends a session at the session end (Case 1.2), we insert the tuple into the respective slice (one update). Thereby, the start and end times of slices remain unchanged.

If an out-of-order tuple extends a session at the session start (Case 1.3), we change session edges respectively and add the tuple (two updates).

An out-of-order tuple can also fuse two sessions. This is the case whenever the gap between sessions shrinks below the minimum session gap (Case 2). Fusing sessions also combines the slices of the sessions (one merge).

Finally, an out-of-order tuple can form a new session on its own if its gap on both sides is larger than the minimum session gap (Case 3). In this case, we split a slice between sessions (i.e., within the gap). Because gaps contain no data by definition, we can create a new slice that contains the out-of-order tuple and and update the end of the existing slice without changing its aggregate (one update).

7 The Stream Slicer
We introduced the architecture and the components of Scotty in Section 5.3 and Figure 7. In the following sections, we present the algorithms used in the Stream Slicer and the Slice Manager component of Scotty in detail to deepen the understanding of these components.

7.1 Notations and Terminology
We use the following notation in all algorithms presented in the remainder of the paper:

7.1.1 General Nomenclature
- $e$: An event, which can be an in-order tuple, out-of-order tuple, or a watermark.
- $t_e(e)$: The event-time of an event $e$. Note that this could also be any other window measure as discussed in Section 4.3.
- $l$: The length of a window as introduced in Figure 1.
- $l_s$: The slide step of sliding window as introduced in Figure 1.
- $gap$: The minimum gap which separates sessions as introduced in Section 6.1. If there are multiple session window queries running concurrently, then $gap$ is the smallest gap $l_g$ of all queries (see Figures 1 and 8).
7.1.2 Window Edges
Any beginning or ending of a window is a window edge. In Scotty, each window edge marks the start of a new slice. We determine upcoming window edges on-the-fly in the stream slicer.

In general, all event-times of upcoming window edges are known for context free windows. For example, a query with a tumbling window has two parameters which determine all window edges: the length \(l\) and the start time \(t_s\) of the query execution. At any time \(t_c\), we can compute time of the next window edge after \(t_c\) as \(t_c + l - (t_c - t_s) \mod l\). A sliding window has the additional parameter \(l_s\) defining the slide step. When determining window edges, a sliding window is equivalent with two tumbling windows: One tumbling window represents all starts of a sliding window (start \(t_s\) and length \(l_s\)) and the other all window ends (start \(t_s + l\) and length \(l_s\)).

For context aware windows, windows edges may or may not be known up front and can constantly change. We allow for declaring the next upcoming window edge in the stream slicer based on the processed in-order tuples. In addition, the slice manager can remove, shift, and add window edges for context aware windows.

7.1.3 Slice Separators
We manage window edges as slice separators. A slice separator is placed between two consecutive tuples and marks the ending of a slice. Thus, several window edges may stick to the same slice separator, e.g., if two windows end or start at the same time. We distinguish three types of separators:

- Fixed Slice Separators mark the edges of context free windows such as tumbling and sliding windows. These edges will never be shifted or removed.
- Flexible Slice Separators mark the edges of context aware windows such as session windows. These edges may be shifted or removed.
- Combined Slice Separators mark coinciding edges of context free and context aware windows, e.g., a session window and a tumbling window ending at the same time.

This differentiation increases the performance of the Slice Manager when processing out-of-order tuples later on as the type of slice separator determines the required actions independent of the underlying window types.

7.2 The Overall Slicing Algorithm
We show the overall algorithm of our Stream Slicer in Algorithm 1. The Stream Slicer operates based on in-order tuples and adds slice separators to start new slices.

Note that we present all algorithms on the example of sliding, tumbling, and session windows as representatives for context free and context aware windows. The presented algorithms generalize to any other window type as well, as they are based on the general concepts of window edges and slice separators introduced in Section 7.1.

As first step, we check in Line 4 if the current session has timed out. Then, we reset the session timeout depending on the event-time of the current tuple in Line 5 and continue with tumbling and sliding windows. The loop starting in Line 7 emits all fixed separators before \(t_c(e)\).

Possibly, we emit another slice separator at \(t_c(e)\) that can have any of the three types:

- If a session timed out and a sliding or tumbling window edge lies at \(t_c(e)\), we emit a combined separator at \(t_c(e)\) in Line 14.
- If only a sliding or tumbling window edge lies at \(t_c(e)\), we emit a fixed separator in Line 15.
- If only a session timed out, there will be a flexible separator at \(t_c(e)\) in Line 19.

Finally, after emitting all edge separators up to \(t_c(e)\), we forward \(e\) to the Slice Manager in Line 22.
Algorithm 1 Stream Slicing with Scotty.

State:
- next_edge: Next edge of a tumbling or sliding window.
- session_timeout: Timeout for session window.
- gap: Minimum session window gap.

1: upon event e do
2:   if e is in-order tuple then
3:     // Session window slicing
4:       flex_end ← (te(e) ≥ session_timeout);
5:       session_timeout ← te(e) + gap;
6:     // Tumbling and Sliding window slicing
7:       while te(e) > next_edge do
8:         emit fixed separator with time next_edge;
9:         next_edge ← next window edge after next_edge;
10:   end while
11:   // Emit remaining separator if needed
12:   if next_edge == te(e) then
13:     if flex_end then
14:       emit combined separator with time te(e);
15:     else emit fixed separator with time te(e);
16:     end if
17:     next_edge ← next window edge after next_edge;
18:   else if flex_end then
19:     emit flexible separator with time te(e);
20:   end if
21: end if
22: emit e; // Always forward e (after separators)
23: end

7.3 Optimizing the Stream Slicer

We incorporate several optimizations that reduce the per-tuple complexity and make slicing highly efficient:

7.3.1 Sessions Window Fusion. We consider the session window with the smallest gap only as discussed in Section 6.1. This avoids monitoring multiple gaps concurrently.

7.3.2 Tumbling and Sliding Window Fusion. We reduce the number of tumbling window queries with query fusion whenever the lengths of tumbling windows are multiples of each other. For example, assume two tumbling windows A and B with the lengths l_A and l_B and the query start times t_A^s and t_B^s for which l_B ≥ l_A. If l_B mod l_A = 0 and (t_B^s - t_A^s) mod l_A = 0, all edges of B coincide with an edge of A and we can slice based on A only. We apply the same fusion logic for sliding windows because we represent each sliding window with two tumbling windows (Section 7.1.2).

7.3.3 Windows Edges. We keep the timestamp of the next upcoming window edge in memory for each query (Algorithm 2). When a tuple arrives, we compare its event-time with the timestamp of the next window edge to decide if we need to insert a slice separator (Line 7 in Algorithm 1). This ensures that we compute the time of the next window edge after slice separators only, i.e., just once per slice, which allows for scaling to high throughputs and hundreds of queries because we bind the complexity to the number of slices instead of the number of tuples per time (throughput).
To prevent repeated computation, Scotty stores the next upcoming slice edge for each currently running query. This binds the size of the arrays used in Algorithm 2 to the number of active queries. We invoke Algorithm 2 in the Stream Slicer (Algorithm 1 in Line 9 and 17).

**Algorithm State:** The algorithm keeps three variables as state:

1. $t_{next}[:]$ is an array of edge times. It stores the time of the next upcoming edge for each tumbling or sliding window. Note that we represent each sliding window with two tumbling windows as described in Section 7.1.2.

2. $l[:]$ is an array which stores the length of each tumbling window. This allows for calculating the time of the next edge time given the time of the edge before.

3. next_id stores the the id of the minimum value in $t_{next}[:]$ in order to enable fast access to the time of the next upcoming edge.

**Adding Queries and Query Fusion:**

We add new window queries through the function ADD_WINDOW (see Algorithm 2). The function receives the start time of the query execution $t_s$ and the length of the tumbling window $l_W$ as parameters. Inside the function, we first check if we can fuse the new query with another one. If there exists a query that covers all edges of the new query already, we exit the function in Line 14 without a need to save the new query. If the new query covers all edges of a query added earlier,
we remove the previous query in Line 17. Finally, we add the new query (i.e., the new window) to the arrays in Lines 19 to 21. Thereby, we update \texttt{next\_id} accordingly if the new window causes the next edge.

\textbf{Proceeding to the Next Edge:}
Whenever we pass the event-time of an edge in the Stream Slicer, we invoke \texttt{NEXT\_EDGE} in Algorithm 2. This function returns the time of the next edge and updates the array of stored window edges \((l_{\text{next}})\). Within the function, we first remember the time of the current edge. Then, we update all edges in the array that have the same edge time by adding the lengths of the respective windows. Finally, we return the event-time of the next edge.

\section{The Slice Manager}

In this section, we present the Slice Manager of Scotty which has three purposes:

1. It creates new slices when receiving slice separators.
2. It adds all tuples to the correct slice.
3. It updates and creates past slices when processing out-of-order tuples.

The Slice Manager provides the slices to the Aggregate Store which is in charge of aggregating values for each slice.

\subsection{Notations and Terminology}

For the discussion of the Slice Manager, we define the following terminology in addition to the terminology introduce in Section 7.1. We visualize the terminology for the following discussion in Figure 10. Let \(S\) be a slice. We name the end time of the slice \(t_{\text{end}}(S)\) and call the maximum event-time of any tuple contained in the slice \(t_{\text{max}}(S)\). The event-time of a tuple \(e\) is \(t_e(e)\) as before.

\subsubsection{Active Slice vs. Past Slices}

The Slice Manager distinguishes between the \textit{active slice} and \textit{past slices}. The \textit{active slice} starts in the past but ends in the future. An event-time is in the \textit{past} if any event processed so far has a larger event-time. An event-time is in the \textit{future} if all events processed so far have a smaller event-time. All slices before the active slice are \textit{past slices}.

\subsubsection{Slice Types}

The Slice Manager operates based on slice types instead of window specifications. This decoupling is important for scalability because it allows for adding queries without increasing the per-tuple computation effort. We distinguish three types of slices which map to the types of slice separators introduced in Section 7.1.3:

- \textbf{Fixed Slices}: The end times of fixed slices are immutable. This guarantees that the Window Manager retains slice separations where context free windows (e.g., tumbling and sliding windows) start or end.
- \textbf{Flexible Slices}: The end times of flexible slices can change. Thus, the Window Manager can extend flexible slices, shrink them, and fuse them with their successors. This is required to
Algorithm 3 Slice Management in Scotty.

State:
\(s_c\): currently active slice.
\(gap\): minimum session window gap.

1: **upon event** \(e\) **do**
   2: if \(e\) is watermark then
      3: forward \(e\) to the Window Manager
   4: else if \(e\) is slice separator then
      5: set slice type of \(s_c\) to type of \(e\)
      6: store \(s_c\) in the Aggregate Store
      7: \(s_c\) ← new empty slice
   8: else if \(e\) is in-order tuple or \(e \in s_c\) then
      9: add \(e\) to \(s_c\)
   10: else if no session windows or \(e \in active\) session then
      11: add \(e\) to the slice which covers \(t_e(e)\)
   12: else // \(e\) is out-of-order tuple and we have sessions
      13: \(S\) ← session covering \(t_e(e)\) including succeeding gap
      14: if \(t_{end}(S) - t_e(e) > gap\) and \(t_e(e) - t_{max}(S) > gap\)
         // gaps on both sides of \(e\) ⇒ new session
         15: then split \(S\) at \(t_e(e)\) and add \(e\)
      16: else if \(t_{end}(S) - t_e(e) > gap\)
         // gap on the right of \(e\) ⇒ right or simple insert
         17: then add \(e\) to the slice which covers \(t_e(e)\)
      18: else if \(t_e(e) - t_{max}(S) > gap\)
         // gap on the left of \(e\) ⇒ left insert
         19: then move \(t_{end}(S)\) to \(t_e(e)\) (excl.) and add \(e\)
      20: else // no gap separates \(e\) ⇒ fuse sessions
         21: then fuse \(S\) with succeeding session and add \(e\)
      22: end if
   23: end if
   24: end if
   25: end

update slices when processing out-of-order tuples that change the context of context aware windows such as session windows.

- **Combined Slices:** Combined slices unite characteristics of fixed and flexible slices. They occur when the edge of a context free window coincides with the edge of a context aware window. End times of combined slices are immutable. However, a combined slice also marks the ending of a context aware window.

8.2 The Overall Slice Management Algorithm

We show the overall algorithm of the Slice Manager in Algorithm 3. The Slice Manager is independent from watermarks. Thus, we forward watermarks to the Window Manager in Line 3. In the following subsections, we discuss how we process slice separators, how we assign tuples to slices, and how we retain correct slices when tuples arrive out-of-order.

8.2.1 Processing Slice Separators.
The Stream Slicer marks the starts of new slices with slice separators. The Slice Manager processes slice separators in three steps: First, it sets the type of the currently active slice with respect to the separator type (fixed, flexible, or combined) in Line 5 of Algorithm 3. Second, after setting the
slice type, the Slice Manager stores the slice in the Aggregate Store which manages all past slices (Line 6). Finally, the Slice Manager resets the currently active slice with a new empty slice (Line 7).

8.2.2 Adding Tuples to Slices

In-order Tuples: In-order tuples always belong to the currently active slice because their event-time cannot be in the past by definition. Thus, we add all in-order tuples to the currently active slice in Line 9 of Algorithm 3. This has low computational costs because we add tuples to their slice without a lookup operation for finding the correct slice. Moreover, the costs are independent from the number of concurrent windows and queries which is crucial for scalability.

Out-of-order Tuples: The computation effort when processing a tuple out-of-order depends on the delay of the tuple. If a tuple has a small delay but still belongs to the currently active slice, we can add the tuple to the active slice just like an in-order tuple (Line 9). If the tuple has a larger delay, we lookup the slice that covers the event-time of the tuple and add the tuple to that slice (Line 11).

8.3 Changing Slices for Out-of-order Tuples

8.3.1 Tumbling and Sliding Windows
For tumbling and sliding windows, we know the times of all window edges a priori. Thus, the Stream Slicer always initiates the correct creation of all slices for these windows. The Slice Manager ensures to retain correct slices for tumbling and sliding windows when changing past slices. In the following, we discuss how out-of-order tuples affects context aware windows on the example of session windows.

8.3.2 Session Windows
When we process session windows, an out-of-order tuple might fuse sessions or add a new session in the past (Recall the discussion of Figure 9 in Section 6.2). Thus, the Slice Manager possibly adds or changes slices in the past before inserting the out-of-order tuple.

Analogue to the Stream Slicer, the Slice Manager operates based on a single session window query - the one with the smallest gap. This is sufficient to maintain all slices for session windows with larger gaps as well (recall Section 6.1).

An out-of-order tuple either belongs to an existing session, fuses sessions, or forms a new session on its own. We show all three cases with the corresponding slice changes in Figure 9.

- Insert in Existing Sessions: In case the out-of-order tuple $e$ belongs to an existing session, we insert the tuple in an existing slice. If $t_e(e)$ lies in the middle of a session (Case 1.1 in Figure 9) or extends a session at the session end (Case 1.2 in Figure 9), we insert the tuple in the slice $S$ which covers $t_e(e)$. In both cases, the start and end times of slices remain unchanged. If $e$ extends a session at the start of the session (Case 1.3 in Figure 9), we change $t_{end}(S)$ to $t_e(e)$ (exclusive) and add $e$ afterwards.
- Fusing Sessions: Adding $e$ can also fuse two sessions. This is the case whenever adding $e$ shrinks the gap between sessions below the minimum session gap (Case 2 in Figure 9). Fusing sessions also combines the slices of the sessions.
- Adding new Sessions: If the gap on both sides of $e$ is larger than the minimum session gap, $e$ forms a new session on its own. In this case we split the slice which covers $t_e(e)$ (Case 3 in Figure 9). The slice before the split ends at $t_e(e)$ (exclusive). The new slice (after the split) starts at $t_e(e)$ (inclusive) and ends at the former end of the slice that we split. We can split $S$ after $t_{max}(S)$ (i.e., within the gap) without changing the aggregate of $S$ because the gap cannot contain any tuples.

Formal Specification: We formalize the rules for all cases depicted in Figure 9 in Algorithm 3. First, we find the session $S$ which covers $t_e(e)$ in Line 13 (including the gap after the session). Then, we check if there are gaps larger than the minimum gap on both sides of $e$ in Line 14 (Case 3 in Figure 9). If this is not the case, we check the gap after $e$ in Line 17 (Cases 1.1 and 1.2 in Figure 9).
Fig. 11. Joint Processing for Multiple Queries.

(a) Splitting sessions.
(b) Fusing sessions.
(c) Left extend with \( t(e) \) at the session end.
(d) Left extend with flexible slices.
(e) Left extend with combined slices.

Fig. 12. Slice Management for Out-of-order Tuples with Multiple Sliding, Tumbling, and Session Windows.

Finally, we check the gap before \( e \) in Line 20 (Case 1.3 in Figure 9). If no gap remains larger than the minimum gap which separates sessions, we fuse sessions in Line 24 (Case 2 in Figure 9).

8.4 Joint Slice Management for all Window Types

In the following, we discuss how Scotty shares partial aggregates among multiple queries involving different window types.

8.4.1 Multiple Query Example

For example, consider Figure 11. We slice the stream with respect to a minimum session window gap of four. In addition, we process a tumbling window with a length of three. This results in slices of all types. Fixed slices (\( \bullet \)) mark the endings of tumbling windows and flexible slices (\( \bigcirc \)) the endings of sessions. Combined slices (\( \bigtriangleup \)) mark the coincidence of both.

In general, Algorithm 3 remains unchanged for multi query scenarios. However, \( S \) corresponds to the session which covers \( t(e) \) including the gap after the session. In contrast to the example in Figure 9, there is no one-to-one mapping between sessions and slices any more. Thus, the subroutines for fusing (Line 24), splitting (Line 14), and extending sessions (Line 20) change. We now discuss these subroutines.
Algorithm 4 Splitting a Session.

Parameter:
- $e$: Tuple to be inserted.
- $t_e(e)$: Event-time of $e$.

1: $S \leftarrow$ slice which covers $t_e(e)$;
2: if $S$ starts at $t_e(e)$ then
3: // Slice before $S$ must be fixed.
4: change the type of the slice before $S$ to combined;
5: add $e$ to $S$;
6: else // $S$ does not start at $t_e(e)$.
7: change $\text{end}(S)$ to $t_e(e)$ (excluding $t_e(e)$ from $S$);
8: change type of $S$ to flexible;
9: add slice in $[t_e(e), \text{former end}(S)]$ with former type of $S$.
10: add $e$ to the new slice.
11: end if

We visualize all cases with examples in Figure 12 and show a formal specification in the form of an algorithm for each action. The discussion presented here refers to session windows as one example of a context aware window type. In general, the Slice Manager is agnostic to the window specifications. Thus, it is irrelevant for the Slice Manager which windows require a slice.

**Virtual Session Slices:** We introduce the concept of virtual session slices to represent sessions including their succeeding gaps. Such slices are not stored, but we keep an index with their start and end times. This allows us to find the session which covers $t_e(e)$ with negligible latency.

8.4.2 Splitting Sessions

**Example:** In case an out-of-order tuple $e$ forms a new session on its own, we split a past session (Line 14 in Algorithm 3). We show the split logic in Figure 12a. We always split a session at $t_e(e)$. For $e_1$ and $e_2$, the event-times do not coincide with the start of an existing slice. Thus, we split the slice covering $t_e(e)$. The slice before $t_e(e)$ is flexible. The slice after $t_e(e)$ inherits the slice type of the slice we split (⇒⇒⇒⇒). For $e_3$, $t_e(e_3)$ already matches the start of a slice. Thus we do not need to split a slice. However the slice before $e_3$ becomes the end of a session and its type changes to combined (⇒⇒⇒⇒).

**Algorithm:** We show the logic for splitting sessions in Algorithm 4. The algorithm receives the out-of-order tuple $e$ and the event-time $t_e(e)$ of that tuple as parameters.

First, we find the slice which covers $t_e(e)$ and name it $S$ (Line 1). If $S$ starts at $t_e(e)$, there is a slice separation at $t_e(e)$ already and we do not need to split slices. However, we need to split the session by changing the slice types. The slice before $S$ must be a fixed slice because it is in the middle of a session where we cannot have combined or flexible slices. When we split the session, the slice before $S$ becomes the last slice of a session. Thus, we change the type of the slice before $S$ to combined (Line 4) and add $e$ to $S$ (Line 5).

If $S$ does not start at $t_e(e)$, we need to split $S$ at $t_e(e)$. Therefore, we first shrink $S$ by changing $\text{end}(S)$ to $t_e(e)$ (Line 7). Then, we change the type of $S$ to flexible, because $S$ marks the end of a session now (Line 8). Finally, we add a new slice in the gap between $t_e(e)$ and the former end of $S$ (Line 9) and add $e$ to this new slice (Line 10). Thereby, the new slice inherits the former type of $S$. 
Algorithm 5 Fusing Sessions.

Parameter:
- \( e \): Tuple to be inserted.
- \( t_e(e) \): Event-time of \( e \).
- \( S \): The session which is fused with its succeeding session.

1: \( S_L \leftarrow \text{last slice in } S \);
2: \( S_F \leftarrow \text{first slice in the session after } S \);
3: \text{if } \( S_L \) is a combined slice \text{ then}
   4: \quad \text{change type of } \( S_L \) to fixed;
   5: \text{else } // \( S_L \) is a flexible slice. \( \Rightarrow \) remove flexible separator
   6: \quad \text{fuse } S_L \text{ and } S_F \text{ keeping the type of } S_F;
   7: \text{end if}
8: \text{add } e \text{ to the slice covering } t_e(e);

8.4.3 Fusing Sessions

Example: When an out-of-order tuple fuses two sessions (Line 24 in Algorithm 3), we check the slice type of the last slice in the earlier session. The last slice of a session must be combined or flexible. If the slice is combined, we cannot fuse it with its succeeding slice because it also marks the ending of a sliding or tumbling window. Thus, we change the slice type from combined to fixed which removes the marker for the session end (1. fuse in Figure 12b; \( e \Rightarrow \)). If the slice is flexible, we fuse it with its successor. The fused slice inherits its type from the later slice (2. fuse in Figure 12b; \( \Rightarrow \Rightarrow \)).

Algorithm: We formalize the logic for fusing sessions in Algorithm 5. The algorithm receives the out-of-order tuple \( e \), the event-time \( t_e(e) \) of that tuple, and the session \( S \) (which is fused with its succeeding session) as parameters.

As first step, we find the last slice in the session \( S \) and name it \( S_L \) (Line 1). Then, we find the first slice in the session after \( S \) and name it \( S_F \) (Line 2). In order to fuse \( S \) with its succeeding session, we fuse \( S_L \) with \( S_F \). If \( S_L \) is a combined slice, we cannot remove the separation between \( S_L \) and \( S_F \) because \( S_L \) marks the start or end of a tumbling or sliding window. In this case, we fuse sessions by changing the slice type from combined to fixed (Line 4).

If \( S_L \) is not combined, it must be flexible. In this case, we fuse \( S_L \) with \( S_F \) (i.e., we merge them to one partial aggregate). Thereby, we keep the slice type of \( S_F \) (Line 6). Finally, we add \( e \) to the slice which covers \( t_e(e) \) (Line 8). Note that \( e \) does not necessarily belong to \( S_L \) or \( S_F \). \( t_e(e) \) possibly falls in another slice preceding \( S_L \) or succeeding \( S_F \).

8.4.4 Extending Sessions

Example: When we extend a session at its start (Line 20 in Algorithm 3), we check if the slice which covers \( t_e(e) \) is the last slice of a session. If so, we check if the slice is combined or flexible. If it is flexible, we can change its end time to \( t_e(e) \) (excluding) without changing the slice type (\( e_1 \) in Figure 12c). If the slice is combined, we cannot move its end and, thus, split it at \( t_e(e) \) in a flexible and a fixed slice (\( e_2 \) in Figure 12c; \( e \Rightarrow \)).

In Figure 12d and 12e, we consider the case were we extend a session at its start, but \( t_e(e) \) is not within the last slice of a session. In this case, we extend the session in two steps. First, we remove the former end of the session before the one we extend. Second, we mark the new end at \( t_e(e) \) (exclusive). In order to remove the former end of the session which covers \( t_e(e) \), we require the last slice of that session. If the last slice is flexible, we fuse it with its succeeding slice (Figure 12d). Thereby, the fused slice inherits the type of the later slice (\( \Rightarrow \Rightarrow \)). If the last slice is combined,
Algorithm 6 Extending a Session at its Start.

Parameter:
- $e$: Tuple to be inserted.
- $t_e(e)$: Event-time of $e$.
- $S$: The session which covers $t_e(e)$.

1: $S_e \leftarrow$ slice which covers $t_e(e);$  
2: $S_L \leftarrow$ last slice in $S$;  
3: // Simple case: No fixed slices are involved.  
4: if $S_e == S_L$ and $S_e$ is flexible then  
5: change $t_{end}(S_e)$ to $t_e(e)$ (exclusive);  
6: add $e$ to the slice succeeding $S_e$;  
7: else if $S_e == S_L$ then // $S_e$ is combined.  
8: change $t_{end}(S_e)$ to $t_e(e)$ (exclusive);  
9: add fixed slice in $[t_e(e), \text{former } t_{end}(S_e)]$;  
10: add $e$ to the new slice;  
11: else if $S_e$ and $S_L$ are not the same slice, $S_e$ is fixed.  
12: // Remove former end of $S$.  
13: if $S_L$ is flexible then  
14: fuse $S_L$ with succeeding slice (keep type of successor);  
15: else // $S_L$ is combined.  
16: change type of $S_L$ to fixed;  
17: end if  
18: // Add new end of $S$.  
19: if $S_e$ starts at $t_e(e)$ then // change slice type.  
20: change type of the slice before $S_e$ to combined;  
21: add $e$ to $S_e$;  
22: else // split slice.  
23: change $t_{end}(S_e)$ to $t_e(e)$ (exclusive);  
24: change type of $S_e$ to flexible;  
25: add slice (former type of $S_e$) in $[t_e(e), \text{former } t_{end}(S_e)]$;  
26: add $e$ to the new slice;  
27: end if  
28: end if

we cannot fuse it and just change its type to fixed (Figure 12e; $\Rightarrow \Rightarrow$). In order to set the new end of the session, we require the slice which covers $t_e(e)$. If this slice starts at $t_e(e)$, we mark the end of the session by setting the type of the preceding slice to combined ( $\Rightarrow \Rightarrow$). Otherwise, we split the slice which covers $t_e(e)$. The slice before the split is flexible and the one after the split inherits the type of the slice we split (Figure 12d; $\Rightarrow \Rightarrow \Rightarrow$).

Algorithm: We show the logic for extending a session in Algorithm 6. The algorithm receives the out-of-order tuple $e$, the event-time $t_e(e)$ of that tuple, and the session $S$ which covers $t_e(e)$ as parameters. Note that $S$ corresponds to the virtual session slice covering $t_e(e)$ before adding $e$. Thus, $S$ is the session before the one we extend.

As first step, we find the slice in the session $S$ which covers $t_e(e)$ and name it $S_e$ (Line 1). Then, we find the last slice in $S$ and name it $S_L$ (Line 2).

We check if $S_e$ and $S_L$ are the same slice. If so, we act depending on the type of $S_e$ (i.e., the type of $S_L$). Since we look at the last slice of a session, the slice can be flexible or combined. If it is flexible, we move the slice separation to extend the session after $S$ at its start. Therefore, we change $t_{end}(S_e)$ to $t_e(e)$ (exclusive) in Line 5. This automatically shifts the start of the session after $S$ to
$t_e(e)$ (inclusive). After extending the session, we add $e$ in Line 6. If $S_e$ is combined, we cannot shift the slice separation. Thus, we need to split $S_e$ at $t_e(e)$. Therefore, we change $t_{\text{end}}(S_e)$ to $t_e(e)$ in Line 8. Then, we add a new fixed slice between $t_e(e)$ and the former end of $S_e$ in Line 9. Finally, we add $e$ to the new slice in Line 10.

If $S_e$ and $S_L$ are not the same slice, $S_e$ must be a fixed slice that ends within the gap between two sessions. In this case, we extend the session after $S$ in two steps: First, we remove the former end of $S$. Then, we add the new earlier end of $S$ and, thereby, extend the session after $S$.

In order to remove the former end of $S$, we either fuse $S_L$ with its succeeding slice in Line 14 (if $S_L$ is flexible) or change the type of $S_L$ to fixed in Line 16 (if $S_L$ is combined).

When we add the new end of $S$ at $t_e(e)$, we first check if $t_e(e)$ coincides with a slice separation already. If so, we do not need to split slices. We just mark the end of the session $S$ by changing the type of the slice that ends at $t_e(e)$ from fixed to combined (Line 20) and add $e$ to $S_e$ (Line 21).

If no slice starts at $t_e(e)$, we split $S_e$ at $t_e(e)$. Therefore, we change the end of $S_e$ to $t_e(e)$ (exclusive) in Line 23 and add a new slice between $t_e(e)$ (inclusive) and the former end of $S_e$ (Line 25). Finally, we add $e$ to the new slice (Line 26).

9 Programming Examples

In this section, we show several examples which illustrate how one can use Scotty in different stream processing systems and how one can extend Scotty with new aggregation functions and window types.

9.1 Scotty in Different Stream Processing Systems

Based on the General Stream Slicing approach, we provide Scotty as a general purpose window operator implemented in Java. Scotty is independent of a specific stream processing system. In principle, every stream processing system can embed Scotty as an operator, which supports stateful user-defined processing functions in Java. Furthermore, it is important to note that the correctness guarantees of Scotty, depend on the deliver guarantees of the underlying system. Thus, exactly-once delivery semantics are required to guarantee correct processing results in a distributed stream processing system. Such delivery guarantees are regularly provided by stream processing systems: For example, Flink implements a solution based on asynchronous checkpoints [14, 15]. In case of failures, the operator state will be set back to a recent complete checkpoint and the stream will be replayed starting from that checkpoint. As a result, each tuple is reflected exactly-once in the operator state which yields correct results. Kafka Streams implements a tuple tracking based on change capture messages and special Kafka topics called changelog topics and offset topics [71]. In case of failures, operator state can be recovered from the messages stored under these topics. Storm implements a message tracking based on acknowledgments and allows for replaying a stream through its reliability API in case of failures [61].

For event-time processing, Scotty can either utilize a system provided timestamp and watermark or derive the event time from a tuple field. In both cases, the timestamp becomes a field of the tuple based on which tuples are assigned to slices and windows by Scotty. In this paper, we limit the discussion to Scotty to allow for discussing algorithms and implementations in detail. However, we provide pointers to related works in Section 11, which address the issue of distributed setups where no global (synchronized) timestamp service can be relied on.

Listing 1 shows the interface of the Scotty window operator, which defines two functions. ProcessElement() consumes a new record from the data stream with a corresponding timestamp (either, event time, or processing time). For each invocation, Scotty assigns the record to a slice, adapts the slices if necessary, and updates its corresponding partial aggregate in the aggregation store. ProcessWatermark() consumes a watermark timestamp and triggers all windows that...
Scotty: General and Efficient Open-Source Window Aggregation for Stream Processing Systems

Listing 1. Scotty Window Operator interface

```java
public class ScottyWindowOperator<InputType> {
    // Processes a new record with a specific timestamp
    public void processElement(InputType element, long ts) {...}
    // Processes a watermark and provide results for all windows that are triggered since the last watermark.
    public List<AggregateWindow> processWatermark(long watermarkTs) {...}
}
```

Listing 2. Scotty Embedding in Apache Beam

```java
PCollection<KV<Integer, Integer>> stream = ...
KeyedScottyWindowOperator<Integer, Integer> scottyWindowDoFn =
    new KeyedScottyWindowOperator<Integer, Integer>(0, new Sum());
// Adding three window definition for Tumbling, Sliding and Session windows.
scottyWindowDoFn.addWindow(new TumblingWindow(WindowMeasure.Time, 5000));
scottyWindowDoFn.addWindow(new SlidingWindow(WindowMeasure.Time, 2000, 1000));
scottyWindowDoFn.addWindow(new SessionWindow(WindowMeasure.Time, 2000));
// Apply Scotty Windowing
PCollection<WindowResults> windowAggregates = stream.apply(ParDo.of((scottyWindowDoFn)));
```

ended between the last received watermark timestamp and the current watermark timestamp. To support out-of-order events, Scotty delays the termination of windows by a fixed allowed lateness. In the future, we plan to integrate window refinements as defined by the Dataflow Model [1] and adaptive watermark delays [7] to minimize the windowing latency.

To integrate Scotty with a stream processing system, Scotty has to become an (user-defined) operator in the respective system which can then be used just like any other operator. To this end, one has to implement a connector class. Such a class is usually a wrapper class instantiating Scotty and implementing (or extending) the operator class of the stream processing system. Such a class is usually implemented as an interface or abstract class in Java. The complexity of implementing a connector depends on the respective stream processing system and its requirements for implementing a custom operator. First, one needs to implement the logic for passing input tuples to Scotty and results back to the system. Second, it is required to connect the state of Scotty to the state backup of the respective systems, to be able to recover from node failures. To ease the connection to different state backends, we made the entire Scotty window operator serializable. A careful study and implementation of state backups for individual systems can significantly reduce the overhead caused by state backups upon checkpoints and caused by state recovery upon failures.

The Scotty open-source project provides connectors for Apache Flink [16], Apache Storm [61], Apache Beam [1], Apache Samza [48], Apache Kafka Streams [40], and Apache Spark Continuous Processing [60, 75]. These connectors implement Flink’s KeyedProcessFunction, Storm’s BaseBasicBolt, Beam’s DoFn, Samza’s StreamTask, Kafka’s Processor, and Spark’s FlatMapFunction respectively. Using these connectors, Scotty can directly replace the native window operator of these stream processing systems. Listing 2 presents an Apache Beam stream processing pipeline using the Scotty operator. This example, demonstrates the definition of a window aggregation across multiple different concurrent windows. In line 3 to 9 we create a window operator, which performs a sum aggregation on three window definitions (i.e., a tumbling-, a sliding-, and a session-Window). Finally, the Scotty window operator is directly embedded into the Apache Beam pipeline as any native operator. All connectors expose the same Scotty API through their addWindow methods. To use Scotty, users first configure the Scotty operator using the same commands independent of the streaming system. Then, users add the Scotty operator to their processing pipeline just like any other operator of the respective system. We provide a demo for each system in the respective connector directory in the Scotty open source project.
Listing 3. Interface for User-defined Window Aggregations

```java
public interface AggregateFunction<InputType, PartialAggregateType, FinalAggregateType> {
    // Transforms a tuple to a partial aggregate
    PartialAggregateType lift(InputType inputTuple);
    // Computes the combined aggregate from partial aggregates
    PartialAggregateType combine(PartialAggregateType pAgg1, PartialAggregateType pAgg2);
    // Transforms a partial aggregate to a final aggregate
    FinalAggregateType lower(PartialAggregateType pAgg);
}
```

9.2 Extending Scotty with custom Window Aggregations and Types

The Scotty window operator provides several extension points, which allow users to define their own aggregation functions and window types. In principle, these extension points follow the description in Section 5.4. In the following we describe how users can use these extension points programmatically.

**Window Aggregations:** For the definition of a user-defined window aggregation function, Scotty provides the interface shown in Listing 3. Each aggregation function definition consists of a `lift`, `combine`, and `lower` function. Additionally, Scotty provides two interfaces to declare if an aggregation function is commutative or invertible. This allows for performing the different slicing decisions for arbitrary aggregation functions as defined in Section 5. Depending on the aggregation function, the `PartialAggregateType` stores different data. For a sum aggregation, it only stores a single number as the current partial window sum. In contrast, for a holistic aggregation, we must store all records assigned to a slice. Depending on the concrete implementation, this can be a simple buffer of all records, a tree structure to improve efficiency, or a compressed format to save memory.

**Window Types:** For the definition of user-defined window types, Scotty provides three interfaces, which correspond to the three abstract window types in Scotty (i.e., context-free, forward context-free, and forward context-aware). For forward context-free and forward context-aware windows, the user has to implement a window context. The window context can maintain arbitrary information about the window boundaries and content. For example, a session window maintains a list of all currently active windows. For each processed record, Scotty updates this window context and checks if it should fuse two windows, or it has to insert a new window. Consequently, it adapts the underlying slices according to the rules described in Section 6. Finally, Scotty uses the window context to trigger the windows if the watermark exceeds the window end. Beside the common window types (i.e., tumbling-window, sliding-window, and session-window), Scotty provides implementations for further window types, such as Fixed-band Window [51], Punctuation-based Windows [68], and Slide-By-Tuple Windows [44].

10 Evaluation

In this section, we evaluate the performance of general stream slicing and compare stream slicing with alternative techniques introduced in Section 3 and built-in techniques of different systems.

10.1 Experimental Setup

**Setup.** We implement all techniques on Apache Flink v1.3. We run our experiments on a VM with 6 GB main memory and 8 processing cores with 2.6 GHz.

**Metrics.** In our experiments, we report throughput, latency, and memory consumption. We measure throughput as in the Yahoo Streaming Benchmark implementation for Apache Flink [19, 69]. We determine latencies with the JMH benchmarking suite [49]. JMH provides precise latency measurements on JVM-based systems. We use the `ObjectSizeCalculator` of Nashorn to determine memory footprints [50].
**Baselines.** We compare an eager and a lazy version of general stream slicing with non-slicing techniques from Section 3: As representative for aggregate trees, we implement FlatFAT [59]. For the buckets technique, we use the implementation of Apache Flink [16]. For tuple buffers, we use an implementation based on a ring buffer array. We also include Pairs [42] and Cutty [17] as specialized slicing techniques where possible.

**Data.** We replay real-world sensor data from a football match [47] and from manufacturing machines [36]. The original data sets track the position of the football with 2000 and the machine states with 100 updates per second. We generate additional tuples based on the original data to simulate higher ingestion rates [26]. We add 5 gaps per minute to separate sessions. This is representative for the ball possession moving from one player to another. If not indicated differently, we show results for the football data. The results for other data sets are almost identical because the performance depends on workload characteristics rather than data characteristics.

**Queries.** We base our queries (i.e., window length, slide steps, etc.) on the workload of a live-visualization dashboard that is built for the football data we use [67]. If not indicated differently, we use the sum aggregation in Sections 10.2 and Section 10.3. In Section 10.4, we use the M4 aggregation technique [37] to compress the data stream for visualization. M4 computes four algebraic aggregates per window (i.e., minimum, maximum, first and last value of each window). We show in Section 10.3.2 how the performance differs among diverse aggregation functions. Because we do not change the input and output semantics of the window and aggregation operation, there is no impact on upstream or downstream operations. We ensure that windowing and aggregation are the bottleneck and, thus, we measure the performance of aggregation techniques.

We do not alternate between tumbling and sliding windows because they lead to identical performance: For example, 20 concurrent tumbling window queries cause 20 concurrent windows (1 window for each query at any time). This is equivalent to a single sliding window with a window length of 20 seconds and a slide step of one second (again 20 concurrent windows). In the following, we refer to concurrent windows instead of concurrent tumbling window queries. Sliding window queries yield identical results if they imply the same number of concurrent windows.

**Structure.** We split our evaluation in four parts. First, we compare stream slicing and alternative approaches with respect to their throughput, latency, and memory footprint (Section 10.2). Second, we study the impact of each workload characteristic introduced in Section 4 (Section 10.3). Third, we integrate general slicing in Apache Flink and show the performance gain for a concrete application (Section 10.4). Fourth, we compare Scotty with the built-in solutions for window aggregation on different systems (Section 10.5). Sections 10.2 and 10.3 focus on the performance per operator instance, Section 10.4 studies the parallelization, and Section 10.5 studies different systems.

### 10.2 Stream Slicing Compared to Alternatives

We now compare stream slicing with alternative techniques discussed in Section 3. We first study the throughput for in-order processing on context-free windows in Section 10.2.1. Our goal is to understand the performance of stream slicing compared to alternative techniques, including specialized slicing techniques. In Section 10.2.2, we evaluate how the throughput changes in the

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2The DEBS 2013 Grand Challenge defines ball possession as follows: “A player (and thereby his respective team) can obtain the ball whenever the ball is in his proximity and he hits it. A ball is in proximity of the player when it is less than one meter away from him. The distance of one meter applies to the distance between the sensor within the ball and any of the two sensors in the player’s shin guards. A ball is hit whenever its acceleration or velocity peaks. A ball will stay in the possession of a given player until another player hits it, the ball leaves the field, or the game is stopped. Specifically, a ball may leave the player’s proximity and will still remain in his possession.” [47]
presence of out-of-order tuples and context-aware windows. In Section 10.2.3, we evaluate the memory footprint and in Section 10.2.4 the latency of different techniques.

10.2.1 Throughput

Workload. We execute multiple concurrent tumbling window queries with equally distributed lengths from 1 to 20 seconds. These window lengths are representative of window aggregations that facilitate plotting line charts at different zoom levels (Application of Section 10.3). We chose Pairs [42] and Cutty [17] as example slicing techniques because Pairs is one of the first and most cited techniques and Cutty offers a high generality with respect to window types.

Results. We show our results in Figure 13. All three slicing techniques process millions of tuples per second and scale to large numbers of concurrent windows.

Buckets achieve orders of magnitude less throughput than slicing techniques and do not scale to large numbers of concurrent windows. The reason is that we must assign each tuple to all concurrent buckets (i.e., windows). Thus, tuples belong to up to 1000 buckets causing 1000 redundant aggregation steps per tuple. In contrast, slicing techniques always assign tuples to exactly one slice. Similar to buckets, the tuple buffer causes redundant aggregation steps for each window as we compute each window independently. Aggregate Trees show a throughput which is orders of magnitude smaller than the one of slicing techniques. This is because each tuple requires several updates in the tree.

Summary. We observe that slicing techniques outperform alternative concepts with respect to throughput and scale to large numbers of concurrent windows.

10.2.2 Throughput under Constraints

We now analyze the throughput under constraints, i.e., including out-of-order tuples and context-aware windows.

Workload. The workload remains the same as before but we add a time-based session window ($l_d = 1$ sec.) as representative for a context-aware window. We add 20% out-of-order tuples with random delays between 0 and 2 seconds.

Results. We show the results in Figure 14. Slicing techniques achieve an order of magnitude higher throughput than alternative techniques that do not use stream slicing. Moreover, slicing scales to large numbers of concurrent windows with almost constant throughput. This is because the per-tuple complexity remains constant: we assign each tuple to exactly one slice. Lazy Slicing has the highest throughput (1.7 Million tuples/s) because it uses stream slicing and does not compute an aggregate tree. Eager Slicing achieves slightly lower throughput than Lazy Slicing. This is due to out-of-order tuples that cause updates in the aggregate tree. Buckets show the same performance
increase as in the previous experiment. The performance decrease for the Tuple Buffer is intensified
due to out-of-order inserts in the ring buffer array. Aggregate Trees process less than 1500 tuples/s
with 20% out-of-order tuples. This is because out-of-order tuples require expensive leaf inserts
in the aggregate tree (rebalance and update of inner nodes). Eager slicing seldom faces this issue
because it stores slices instead of tuples in the aggregate tree. The majority of out-of-order tuples
falls in an existing slice, which avoids rebalancing. We exemplary show our results on two different
datasets for this experiment. Because the performance depends on workload characteristics rather
than data characteristics, the results are almost identical. We omit similar results for different data
sets in the following experiments and focus on the impact of workload characteristics.

**Summary.** For workloads including out-of-order tuples and context-aware windows, we observe
that general stream slicing outperforms alternative concepts with respect to throughput and scales
to large numbers of concurrent windows.

### 10.2.3 Memory Consumption

We now study the memory consumption of different techniques
with four plots: In Figures 15a and 15c, we vary the number of slices in the allowed lateness and
fix the number of tuples in the allowed lateness to 50 thousand. In Figures 15b and 15d, we vary
the number of tuples and fix the number of slices to 500. We experimentally compare time-based
and count-based windows. Our measurements include all memory required for storing partial
aggregates and metadata, such as the start and end times of slices.

**Results for Time-Based Windows.** Figures 15a and 15b show the memory consumption for time-
based windows, which do not require us to store individual tuples. For Stream Slicing and Buckets,
the memory footprint increases linearly with the number of slices in the allowed lateness. The
memory footprint is independent from the number of tuples. The opposite holds for Tuple Buffers
and Aggregate Trees. Slicing techniques store just one partial aggregate per slice, while buckets store
one partial aggregate per window. Tuple Buffers and Aggregate Trees store each tuple individually.
Results for Count-Based Windows. Figures 15c and 15d show the memory consumption for count-based windows, which require individual tuples to be stored. The experiment setup is the same as in Figures 15a and 15b. The memory consumption of all techniques increases with the number of tuples in the allowed lateness, because we need to store all tuples for processing count-based windows on out-of-order streams (Figure 15d). Starting from 1000 tuples in the allowed latency, the memory consumed by tuples dominates the overall memory requirement. Accordingly, all curves become linear and parallel. Buckets show a stair shape because of the underlying hash map implementation [70]. Slicing techniques start at roughly $10^5$ byte which is the space required to store 500 slices. The memory footprint of buckets also increases with the number of slices because more slices correspond to more window buckets (Figure 15c). Each bucket stores all tuples it contains which leads to duplicated tuples for overlapping buckets.
Summary. When we can drop individual tuples and store partial aggregates only (Figure 15a and 15b), the memory consumptions of slicing and buckets depends only on the number of slices in the allowed lateness. In this case, stream slicing and buckets scale to high ingestion rates with almost constant memory utilization. If we need to keep individual tuples (Figure 15c and 15d), storing tuples dominates the memory consumption.

10.2.4 Latency The output latency for window aggregates depends on the aggregation technique, the number of entries (tuples or slices) which are stored, and the aggregation function. In Figure 16, we show the latency for different situations.

Distributive and Algebraic Aggregation. For the sum aggregation (Figure 16a), Lazy Slicing and Tuple Buffer exhibit up to 1ms latency for $10^5$ entries (no matter if $10^5$ tuples or $10^5$ slices). Eager Slicing and Aggregate Trees show latencies below 5µs. Buckets achieve latencies below 30ns. Lazy aggregation has higher latencies because it computes final aggregates upon request. Eager Aggregation uses precomputed partial aggregates from an aggregate tree which reduces the latency. Buckets pre-compute the final aggregate of each window and store aggregates in a hash map which leads to the lowest latency.
Holistic Aggregation. The latencies for the holistic median aggregation (Figure 16c) are in the same order of magnitude and follow the same trends. Buckets exhibit the same latencies as before because they precompute the aggregate for each bucket. Thus, a more complex holistic aggregation decreases the throughput but does not increase the latency. The latency of slicing techniques increases for the median aggregation, because we combine partial aggregates to final aggregates when windows end. This combine step is more expensive for holistic aggregates than for algebraic ones.

Summary. We observe a trade-off between throughput and latency. Lazy aggregation has the highest throughput and the highest latency. Eager aggregation has a lower throughput but achieves microsecond latencies. Buckets provide latencies in the order of nanoseconds but have an order of magnitude less throughput.

10.3 Studying Workload Characteristics

We measure the impact of the workload characteristics from Section 4 on the performance of general slicing. For comparison, we also show the best alternative techniques.

10.3.1 Impact of Stream Order In this experiment, we investigate the impact of the amount of out-of-order tuples and the impact of the delay of out-of-order tuples on throughput (Figure 17). We use the same setup as for the throughput experiments in Section 10.2.2 with 20 concurrent windows.

Out-of-order Performance. In Figure 17a, we increase the fraction of out-of-order tuples. Slicing and Buckets process out-of-order tuples as fast as in-order tuples. The throughput of the other techniques decreases when processing more out-of-order tuples.

Slicing techniques process out-of-order tuples efficiently because they perform only one slice update per out-of-order tuple. Eager slicing also updates its aggregate tree. This update has a low overhead because there are just a few hundred slices in the allowed lateness and, accordingly, there are just a few tree levels that require updates. Aggregate Trees on tuples have a much larger number of tree levels because they store tuples instead of slices as leaf nodes.
Buckets have a constant throughput as in the previous experiments. Tuple Buffers and Aggregate Trees exhibit a throughput decay when processing out-of-order tuples. Tuple Buffers require expensive out-of-order inserts in the sorted buffer array. Aggregate Trees require inserting past leaf nodes in the aggregate tree. This causes a rebalancing of the tree and the respective re-computation of aggregates. Eager Slicing seldom faces this issue (see Section 10.2.2).

**Delay Robustness.** In Figure 17b, we increase the delay of out-of-order tuples. We use equally distributed random delays within the ranges specified on the horizontal axis.

All techniques except Tuple Buffers are robust against increasing delays. Slicing techniques always update one slice when they process a tuple. Small delays can slightly increase the throughput compared to longer delays if out-of-order tuples still belong to the most recent slice. In this case, we require no lookup operations to find the correct slice. The throughput of Buckets is independent of the delay because Flink stores buckets in a hashmap. The throughput of the tuple buffer decreases with increasing delay of out-of-order tuples, because the lookup and update costs in the sorted buffer array increase.

**Summary.** Stream slicing and Buckets scale with constant throughput to large fractions of out-of-order tuples and are robust against high delays of these tuples.

### 10.3.2 Impact of Aggregation Functions

We now study the throughput of different aggregation functions using the same setup as before (20 concurrent windows, 20% out-of-order tuples, delays between 0 and 2 seconds) in Figure 18. We differentiate time-based and count-based windows to show the impact of invertibility. We implement the same aggregation functions as Tangwongsang et al. [59]. The original publication provides a discussion of these functions and an overview of their algebraic properties. We additionally study the median and the 90-percentile as examples for holistic aggregation. Moreover, we study a naive version of the sum aggregation that does not use the invertibility property. This allows for making a deduction with respect to not invertible aggregations in general.

**Time-Based Windows.** For time-based windows, the throughput is similar for all algebraic and distributive aggregations with small differences due to different computational complexities of the aggregations. Holistic aggregations (median and 90-percentile) show a much lower throughput because they require to keep all tuples in memory and have a higher complexity.
Count-Based Windows. We observe lower throughputs than for time-based windows, which is because of out-of-order tuples. For count-based windows, an out-of-order tuple changes the sequence id (count) of all later tuples. Thus, we need to shift the last tuple of each slice to the next slice. This operation has low overhead for invertible aggregations because we can subtract and add tuples from aggregates. The operation is costly for not invertible aggregations because it requires the recomputation of the slice aggregate. Time-based windows do not require an invert operation because out-of-order tuples only change the sequence id (count) of later tuples but not the timestamps.

Impact of invertibility. There is a big difference between the performance for different not invertible aggregations on count-based windows. Although Min, Max, MinCount, MaxCount, ArgMin, and ArgMax are not invertible, they have a small throughput decay compared to time-based windows (Figure 18). This is because most invert operations do not affect the aggregate and, thus, do not require a recomputation. For example, it is unlikely that the tuple we shift to the next slice is the maximum of the slice. If the maximum remains unchanged, max, MaxCount, and ArgMax do not require a recomputation. In contrast, the sum w/o invert function shows the performance decay for a not invertible function that always requires a recomputation when removing tuples.

Impact of Holistic Aggregations. In Figure 18, we observe that holistic aggregations have a much lower throughput than algebraic and distributive aggregations. In Figure 19, we show that stream slicing still outperforms alternative approaches for these aggregations. The reason is that stream slicing prevents redundant computations for overlapping windows by sorting values within slices and by applying run length encoding. In contrast, Buckets and Tuple Buffer compute each window independently. The machine data set shows slightly higher throughputs because the aggregated column has only 37 distinct values compared to 84232 distinct values in the football dataset. Fewer distinct values increase the savings achieved by run length encoding. Aggregate trees (not shown) can hardly compute holistic aggregates. They maintain partial aggregates for all inner nodes of a large tree which is extremely expensive for holistic aggregations.

Summary. On time-based windows, stream slicing performs diverse distributive and algebraic aggregations with similarly high throughputs. Considering count-based windows and out-of-order tuples, invertible aggregations lead to higher throughputs than not invertible ones.
10.3.3 Impact of Window Types
The window type impacts the throughput if we process context-aware windows because these windows potentially require split operations. Note that context aware windows cover arbitrary user-defined windows which makes it impossible to provide a general statement on the throughput for all these windows. Thus, we evaluate the time required to recompute aggregates for slices of different sizes when a split operation is performed (Figure 20). Given a context aware window, one can estimate the throughput decay based on the number of split operations required and the time required for recomputing aggregates after splits. We show the sum aggregation as representative for an algebraic function and the median as example for a holistic function.

The processing time for the recomputation of an aggregate increases linearly with the number of tuples contained in the aggregate. If split operations are required to process a context aware window, a system should monitor the overhead caused by split operations and adjust the maximum size of slices accordingly. Smaller slices require more memory and cause repeated aggregate computation when calculating final aggregates for windows. In exchange, the aggregates of smaller slices are cheaper to recompute when we split slices.

10.3.4 Impact of Window Measures
We compare different window measures in Figure 21. We use the same setup as before (20% out-of-order tuples with delays between 0 and 2 seconds).

Time-Based Windows. For time-based windows, the throughput is independent from the number of concurrent windows as discussed in our throughput analysis in Section 10.2.2. The throughput for arbitrary advancing measures is the same as for time-based measures because they are processed identically [17].

Count-Based Windows. The throughput for count-based windows is almost constant for up to 40 concurrent windows and decays linearly for larger numbers. For up to 40 concurrent windows, most slices are larger than the delay of tuples. Thus, out-of-order tuples still belong to the current slice and require no slice updates. The more windows we add, the smaller our slices become. Thus, out-of-order tuples require an increasing number of updates for shifting tuples between slices which reduces the throughput. Tuple buffers are the fastest alternative to Slicing in our experiment. For 1000 concurrent windows, slicing is still an order of magnitude faster than tuple buffers.

Summary. The throughput of time-based windows stays constant whereas the throughput of count-based windows decreases with a growing number of concurrent windows.
10.4 Parallel Stream Slicing

In this experiment, we study stream slicing on the example of our dashboard application [67] which uses the M4 aggregation [37]. We vary the degree of parallelism to show the scalability with respect to the number of cores. We compare Lazy Slicing with Buckets, which are used in Flink.

Results. In Figure 22, we increase the number of parallel operator instances of the windowing operation (degree of parallelism). The throughput scales linearly up to a degree of parallelism of four (Figure 22a). Up to this degree, each parallel operator instance runs on a dedicated core with other tasks (data source operator, writing outputs, operating system overhead, etc.) running on the remaining four cores. For higher degrees of parallelism the throughput and the CPU load increase logarithmically, approaching the full 800% CPU utilization (Figure 22b). Slicing achieves an order of magnitude higher throughput than buckets, because it prevents assigning tuples to multiple buckets (cf. Section 10.2.1). The memory consumption scaled linearly with the degree of parallelism for both techniques.

Summary. We conclude that stream slicing and buckets scale linearly with the number of cores for our application.

10.5 Scotty in Different Stream Processing Systems

We evaluate the throughput of window aggregation on different stream processing systems in Figure 23. Since Apache Beam provides an API only, we evaluate the Beam API on Flink and Samza. We keep data, queries, and metrics as introduced in Section 10.2.1. We take the throughput of Scotty with one concurrent window as baseline (100% throughput) and compare it to the throughput of the respective built-in techniques. We show how each technique scales when increasing the number of concurrent windows.

We stick to relative numbers because our experiments are conducted with different hardware and software setups that impact the absolute throughput. For example, Samza requires to read data from Apache Kafka as message broker, which requires to also run Apache Zookeeper. The overhead of these two additional systems contributes to a lower throughput of Samza compared to Flink. The Beam API added a heavy overhead, which was analyzed in detail by Hesse et al. [29]. This leads to much lower throughput compared to the native APIs of Flink and Samza. We have a well maintained and tuned setup of Flink which contributes to Flink having the highest throughput in all experiments. In this paper, we focus on comparing techniques for window aggregation rather than streaming systems. Karimov at al. provide a solid comparison of systems, which addresses and carefully analyzes effects like the ones stated above [38].

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Results. Scotty outperforms the respective built-in techniques on all evaluated systems. The results also confirm Scotty’s scalability to large numbers of concurrent windows which we observed in previous experiments. For a single window, only Flink’s built-in solution (based on Buckets) achieves similar throughput than Scotty. However, the throughput of Buckets decreases drastically when we add more concurrent windows, which is also reflected in the results for Beam on Flink, Beam on Samza, and Kafka Streams. The built-in techniques of Spark and Storm did not exhibit such scalability issues. We do not show results for the built-in technique of Samza, because it did not produce correct results and our request to the mailing list was not answered.

Summary. Scotty provides higher throughput then built-in operators on all tested systems and scales to large numbers of concurrent windows. The built-in operators of Spark and Storm also scale to large numbers of concurrent windows but provide lower throughput than Scotty.

11 Related Work
In this section, we discuss additional related work that we did not cover in the previous sections. First, we summarize alternative approaches for optimizing window aggregations. Then, we discuss solutions that process streams in batches, before we summarize complementary techniques. Finally, we present follow-up works published after the short versions of this paper [64, 65].

Optimizing Window Aggregations. Our general slicing techniques utilizes features of existing techniques such as on-the-fly slicing [42], incremental aggregation [59], window grouping [27, 28], and user-defined windows [17]. However, general stream slicing offers a unique combination of generality and performance. One can extend other slicing techniques based on this paper to reach similar generality and performance. Existing slicing techniques such as Pairs [42] and Panes [43] are limited to tumbling and sliding windows. Cutty can process user-defined window types, but does not support out-of-order processing [17]. Several publications optimize sliding window aggregations focusing on different aspects such as incremental aggregation [10, 22, 59] or worst-case constant time aggregation [57]. Hirzel et al. conclude that one needs to decide on a concrete algorithm based on the aggregation, window type, latency requirements, stream order, and sharing requirements because each specialized algorithm addresses a different set of requirements [31]. Instead of alternating between different algorithms, we provide a single solution which is generally applicable and allows for adding aggregation functions and window types without changing the core of our technique. Our solutions can be integrated in open source streaming systems such as Apache Flink [16], Spark [75], and Storm [61].

Stream Processing in Batches. In contrast to our techniques, which adopts a tuple-at-a-time processing approach, several works split streams in batches of data which they process in parallel [8,
For example, D-Streams [74] processes mini-batches of data, which are combined to windows. This requires the slide step and range of sliding windows to be multiples of the batch size. SABER introduces window fragments to decouple slide and range of sliding windows from the batch size [39]. However, in contrast to our work, SABER does not consider aggregate sharing among queries. Balkesen et al. use panes to share aggregates among overlapping windows [8]. None of these works addresses the general applicability with respect to workload characteristics.

**Complementary Techniques.** Weaving optimizes execution plans to reduce the overall computation costs for concurrent window aggregate queries [27, 28, 53]. We use a similar approach to fuse window aggregation queries when window edges match. This optimization is orthogonal to the generalization of slicing which is the focus of this paper. Huebsch et al. study multiple query optimization when aggregating several data streams which arrive at different nodes [34]. General stream slicing complements this work with an increased per-node performance. Truviso proposes an alternative technique based on independent stream partitions to correct outputs when tuples arrive after the watermark [41]. While our work focuses on slicing streams and computing partial aggregations for slices, recent publications of Shein et al. further accelerate the final aggregation step which is required when windows end [54, 55]. Trill [18] is an analytics system that supports streaming, historical, and exploratory queries in the same system. Trill supports incremental aggregation and performs aggregations on snapshots, the state of the window at a certain time.

**Follow-Up Works.** The general stream slicing approach and Scotty have been recognized by several follow-up works. Benson et al. introduced a distributed window aggregation approach using an extended version of the Scotty library [9]. Their solutions extend Scotty with in-network aggregation and pre-aggregation at remote data sources. The NebulaStream platform for data management in the internet-of-things adopted general stream slicing to enable efficient stream processing on small devices [76]. Hirzel et al. proposed FiBA, a highly efficient sliding window aggregation algorithm that optimally handles streams of varying degrees of out-of-orderness [58]. They conclude that this algorithm could serve as a more efficient aggregation store in Scotty to combine the benefits of stream slicing with faster final aggregation. Furthermore, general stream slicing was attributed as a promising approach to further improve the processing efficiency of modern scale-up stream processing system [25, 77, 78].

Stream processing systems regularly receive tuples with event timestamps that have been assigned at the spots where the respective events have been recorded. For example, in a distributed processing setting such as the Internet of Things, timestamps may be assigned by sensor nodes such as smartphones, machines, or connected cars. In such a distributed processing setting, where no global (synchronized) timestamp service can be relied on, no central stream processing system can guarantee correctness, because events with the same timestamp may be recorded at different times due to unsynchronized clocks. We have addressed this issue with the SENSE system for gathering sensor data tuples with guaranteed time coherence [35, 63, 66]. We have further integrated SENSE and Scotty into an end-to-end stream processing pipeline [62].

**12 Conclusion**

Stream slicing is a technique for streaming window aggregation which provides high throughputs and low latencies with a small memory footprint. We contribute a generalization of stream slicing with respect to four key workload characteristics: Stream (dis)order, aggregation types, window types, and window measures. Our general slicing technique dynamically adapts to these characteristics, for example, by exploiting the invertibility of an aggregation or the absence of out-of-order tuples. We implemented our general stream slicing technique in Scotty, an open-source operator that provides efficient and general sliding-window aggregation for stream processing systems under

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the Apache 2.0 license. Scotty also allows for implementing user-defined aggregation functions and window types without changing the core operations of the technique.

Our experimental evaluation reveals that general slicing is highly efficient without limiting generality. It scales to a large number of concurrent windows and consistently outperforms state-of-the-art techniques in terms of throughput. Furthermore, it efficiently supports application scenarios with large fractions of out-of-order tuples, tuples with high delays, time-based and count-based window measures, context-aware windowing, and holistic aggregation functions. In general, stream slicing is beneficial whenever a slice contains at least a few records (≈10). Thus, it is not beneficial for count-based windows with a very small slide step (less than 10 records). We observed that the throughput scales linearly with the number of processing cores and that latency is in the order of microseconds. Techniques based on window buckets provide lower latency, but exhibit drastically lower throughput due to repeated computations for concurrent windows.

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References


